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Water Resources Research Report

Quantifying Uncertainties in the Modelled Estimates of Extreme Precipitation Events at the Upper Thames River Basin

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VERITAS ET UTILITAS

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Executive Summary

Assessment of climate change impact on hydrology at watershed scale incorporates downscaling of global scale climatic variables into local scale hydrologic variables and computations of risk of hydrologic extremes in future for water resources planning and management. Atmosphere-Ocean General Circulation (AOGCM) models are designed to simulate time series of future climate responses accounting for enthropogenically induced green house gas emissions. The climatological inputs obtained from several AOGCMs suffer the limitations due to incomplete knowledge arising from the inherent physical, chemical processes and the parameterization of the model structure. This study explores the methods available for quantifying uncertainties from the AOGCM outputs by considering fixed weights from different climate model means for the overall data lengths and provides an extensive investigation of the variable weight nonparametric kernel estimator based on the choice of bandwidths for investigating the severity of extreme precipitation events over the next century. The results of this study indicate that the variable width method is better equipped to provide more useful information of the uncertainties associated with different AOGCM scenarios. This study further indicates an increase of probabilities for higher intensities and frequencies of events. The applied methodology is flexible and can be adapted to any uncertainty estimation studies with unknown densities.

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Introduction

1.1 Problem Definition

Hydrologic research and modeling is largely dependent on climatological inputs due to the inextricable link of water with climate. Water is the most vulnerable resource to climate change (Minville et al., 2008; Srikanthan and McMohan, 2001; Xu and Singh, 2004) resulting in an increased evaporation due to higher temperatures, changes in amount, variability, and frequency of regional precipitation. Studies related to the impact of climate change on water resources have shown a significant impact on the mean annual discharge with changes in the intensity and frequency of precipitation (Whitfield and Cannon, 2000; Muzik, 2001), larger changes in reservoir storage because of a modest change in the natural inflow or even a changed effect in the energy production and flood control measure due to any effect in the hydrologic cycle (Xu and Singh, 2004).

Climate modeling studies involving anthropogenic increase in the concentration of greenhouse gases have suggested an increase in the frequency and intensity of climatic extremes in a warmer world (Cubasch et al., 2001). The evidence of an altered climate has already become noticeable. Recent studies related to the Canadian climate have indicated a 12% increase of precipitation in southern Canada during the twentieth century (Zhang et al., 2000; Vincent and Mekis, 2006). This provides the justification of over a decade long effort to determine the impacts of anthropogenic climate change in water resources. However, most efforts have focused on studying the changes of means, although extremes usually have the greatest and most direct impact on our everyday lives,

community and environment. Study on the detection of changes in extremes is limited and hence require further investigation.

Assessment of climate change impacts on hydrology incorporates projection of climate variables into a global scale, downscaling of global scale climatic variables into local scale hydrologic variables and computations of risk of future hydrologic extremes for purposes of water resources planning and management. Global scale climate variables are commonly projected by Coupled Atmosphere-Ocean Global Climate Models (AOGCMs), which provide a numerical representation of climate systems based on the physical, chemical and biological properties of their components and feedback interactions between these (IPCC, 2007). These models are currently the most reliable tools available for obtaining the physics and chemistry of the atmosphere and oceans and for deriving projections of meteorological variables (temperature, precipitation, wind speed, solar radiation, humidity, pressure, etc). They are based on various assumptions about the effects of the concentration of greenhouse gases in the atmosphere coupled with projections of CO_2 emission rates (Smith et al., 2009).

There is a high level of confidence that AOGCMs are able to capture large scale circulation patterns and correctly model smoothly varying fields, such as surface pressure, especially at continental or larger scales. However, it is extremely unlikely that these models properly reproduce highly variable fields, such as precipitation (Hughes and Guttorp, 1994), on a regional scale, let alone for small to medium watershed. Although confidence has increased in the ability of AOGCMs to simulate extreme events, such as hot and cold spells, the frequency and the amount of precipitation during intense events are still underestimated.

1.2 Definition and Types of Uncertainty

A proper understanding of the uncertainties resulting from human induced climate change will help decision makers to interpret different projected hydrologic impacts with confidence. Three broad areas of uncertainties have been identified by Colglazier (1991):

- Predicting future climate

- Predicting future impacts

- Assessing costs and benefits of policy responses

The first two areas, related to the present research, are described here.

Predictions of the timing and magnitude of any future global warming are associated with uncertainties in estimating future anthropogenic emissions of greenhouse gases; understanding the resulting changes in the carbon cycle, especially the uptake of carbon in the oceans; understanding the dynamic climatic response with all the relevant feedback mechanisms, such as those from clouds and Ocean currents; projecting regional variations; and estimating the frequency of severe events such as hurricanes and droughts (Colglazier, 1991). Although the basic theory of the enhanced green house gas effect is now well established, and the rise in carbon dioxide concentrations since the industrial revolution has also been well documented, there is still much debate regarding the timing and quantity of warming. For decades AOGCMs have been used to predict these values; however there is continued uncertainty even with the improvements of the resolution of GCMs.

The interpretation of uncertainties from climate models can be described from five sources. 'Forcing uncertainty' consists of using the future elements/aspects that are not a

part of the climate system, but have the potential to affect it. One possible form of forcing uncertainty arises from using climate model simulations based on different scenarios of future concentrations of atmospheric GHGs, which depend entirely on the actions taken to control the GHG emissions (Cubasch et al., 2001).

'Initial condition uncertainty' involves uncertainty arising from an initial state or ensemble of states (Stainforth et al., 2007) applied to the climate models. It can be 'macroscopic' and found in state variables with relatively large slowly mixing scales, such that the predicted distribution is effected by the imprecise knowledge of the current state of the system. 'Microscopic' uncertainty, on the other hand, has no significant effect on the targeted climate distribution; the effects are only identified during weather forecast.

'Model imperfection' describes the uncertainty that results from a limited understanding and ability to simulate the Earth's climate. It is sub-divided into two types: 'uncertainty' and 'inadequacy'. 'Model uncertainty' describes uncertainties in the most relevant parameter values to be used in the model (Murphy et al., 2004). It characterizes the impact of known uncertainties and can be large at regional scales. Climate models, in this respect, are considered rather complicated. Extending this from parameter values to parameterizations enables an improved representation of various processes within the model and makes model uncertainty an extended form of the 'parameter uncertainty'(Kennedy and O'Hagan, 2001). 'Model inadequacy' results from the limited ability of the climate models to represent natural systems. These models provide no information on important processes related to climate change on decadal to centennial time scales, such as the carbon cycle, atmospheric and oceanic chemistry and

stratospheric circulation. They further suffer from limited spatial resolution, inadequate representation of hurricanes, the diurnal cycle of tropical precipitation, characteristics of El Nino Southern Oscillation (ENSO) and the inter tropical convergence zone (Trenberth et al., 2003).

1.3 Organization of the Report

The report is organized as follows: literature relevant to the development of methods for assessing climate change impacts are presented in chapter 2. The development of proposed uncertainty estimation methodology is presented step by step in Chapter 3, including the model and parameter set up. Finally, the performances of the variable weight and fixed weight methods for quantification of AOGCM uncertainties in extreme precipitation events are presented. Finally, the findings of the results are discussed in Chapter 4.

2. Literature Review

In recent years, quantifying uncertainties from AOGCM choice and scenario selections used for impact assessments has been identified as critical for climate change and adaptation research. Climate change impact studies derived from AOGCM outputs are associated with uncertainties due to "incomplete" knowledge originating from insufficient information or understanding of the relevant biophysical processes, or a lack of analytical resources. Examples of uncertainty include the simplification of complex processes involved in atmospheric and oceanographic transfers, inaccurate assumptions about climatic processes, limited spatial and temporal resolution resulting in a disagreement between AOGCMs over regional climate change, etc. Uncertainties also emerge due to "unknowable" knowledge, which arises from the inherent complexity of the Earth system and from our inability to forecast future socio-economic and human behavioral patterns in a deterministic manner (New and Hulme, 2000; Allan and Ingram, 2002; Proudhomme et al., 2003; Wilby and Harris, 2006; Stainforth et al., 2007; IPCC, 2007, Buytaert et al, 2009). Selection of the most appropriate AOGCM for the realization of future climate depends on user's ability to assess the model's strengths and weaknesses, the inability of which is recognized as one of the major sources of uncertainty (Wilby and Harris, 2006, Ghosh and Mujumdar, 2007; Tebaldi and Smith, 2010). It has been established that the accuracy of AOGCMs decrease at finer spatial and temporal scales; a typical resolution of AOGCMs ranges from 250 km to 600 km, but the need for impact studies conversely increases at finer scales. The representation of regional precipitation is distorted due to this coarse resolution and thus it cannot capture the subgrid-scale processes required for the formation of site-specific precipitation

conditions. While some models are parameterized, details of the land-water distribution or topography in others are not represented at all (Widmann et al., 2003). Studies have found that the models failed to predict the high variability in daily precipitation and could not accurately simulate present-day monthly precipitation amounts (Trigo and Palutikof, 2001; Brissette et al., 2006).

2.1 Downscaling of AOGCM Outputs

In order to estimate uncertainties at smaller spatial scales, output from climate models are scaled down to a suitable level. Statistical and dynamic downscaling represents two common branches for the development of climate scenarios depending on regions, time periods and the variables of interest. The approaches for dynamic downscaling involve (i) running a regional scale limited area model with coarse GCM data as geographical or spectral boundary conditions, (ii) performing global-scale experiments with high resolution Atmosphere-GCM (AGCM), with coarse GCM data as initial (as partially and boundary) conditions, and (iii) the use of a variable-resolution global model with the highest resolution over the area of interest (Rummukainen, 1997). The most common technique for dynamic downscaling involves utilizing Regional Climate Models (RCMs), which perform at a much higher resolution and can simulate climatic variables more accurately for any region (Brissette et al., 2006). AOGCM output variables are used as boundary inputs for the RCMs, and provide a more accurate representation of the local climate than the coarsely gridded AOGCM data alone. The works of Vidal and Wade (2008), Wood et al. (2004) and Schmidli et al. (2006) compared dynamic downscaling to other methods. A limitation of the dynamic approach is the scale of RCM's (approximately 40 km x 40 km according to Brissette et al., 2006), which is still too

coarse for application to smaller basins. The computational effort required for the dynamic approach makes it impractical where several AOGCMs and emissions scenarios are used (Maurer, 2007). Furthermore, RCMs have only been produced for selected areas; moving to a slightly different region requires repeating the experiment (Kay and Davies, 2008).

The second approach, namely statistical downscaling, is more popular in climate change impact assessments due to its computational ease and its ability to produce synthetic datasets of any desired length. In statistical downscaling statistical relationships are developed to transfer large-scale features of the predictors (AOGCM) to regional scale predictands (variables). Hewitson and Crane (1992) pointed out three underlying assumptions related to statistical downscaling: (i) the predictors are variables of relevance and are realistically modeled by the host AOGCM; (ii) the empirical relationship is also valid under altered climate conditions; and (iii) the predictors employed fully represent the climate change signal.

Several methods of statistical downscaling can be broadly divided into three categories: Transfer function, weather typing and weather generator. Transfer functions rely on the direct quantitative relationship between the global large scale and local small scale variables obtained from different choices of mathematical transfer functions, predictors or statistical fitting processes. Applications of neural networks, regression based methods, least square methods, support vector machines, empirical orthogonal functions (Zorita and von Storch, 1999), etc., fall in this category.

Weather typing involves grouping local meteorological variables with respect to different classes of atmospheric circulation. Future regional climate scenarios are constructed either by resampling from the observed variable distribution or by first generating synthetic sequences of weather patterns using Monte Carlo techniques and resampling from the generated data. The relative frequencies of the weather classes are weighted to derive the mean or frequency distribution of the local climate. Climate change is then determined from the changes of the frequency of the weather classes.

Stochastic weather generators simulate weather data to assist in the formulation of water resource management policies. They are essentially complex random number generators, which can be used to produce a synthetic series of data. This allows the researcher to account for natural variability when predicting the effects of climate change. Weather generators have an advantage over other downscaling methods because by producing long duration rainfall series, it is possible to examine rare events and extremes in the river basin (Brissette et al., 2007; Diaz-Nieto and Wilby, 2005; Wilks and Wilby, 1999). The underlying assumption of weather generator is that the past (control experiment) would be a representative of the future. It is, however, difficult to guarantee that the statistical relationship derived from current climate will remain same for future in the presence of climate change (Hewitson and Crane, 1996; Schulze, 1997; Joubert and Hewitson, 1997).

Parametric, empirical or semi-parametric, and non-parametric (Brissette et al., 2007) weather generators are commonly used by the scientific community. In most parametric weather generators, a Markov chain is used to determine the probability of a wet or dry day and a probability distribution is assumed to determine the amount of precipitation

(Kuchar, 2004; Hanson and Johnson, 1998). Most of the parametric weather generators are extensions of Richardson's WGEN, which was developed in 1981 (Richardson, 1981). Some examples of the parametric weather generators successfully employed using the Richardson approach are CLIGEN, WGENK, GEM, WXGEN, and SIMMENTO (Kuchar, 2004; Schoof et al., 2005; Hanson and Johnson, 1998; Soltani and Hoogenboom, 2003). Hanson and Johnson (1998) compared outputs from GEM to historical data using the means and standard deviations. Results from that study showed that simulated total precipitation values were significantly underestimated for some months, and annual precipitation values were considerably less than the historical record (Hanson and Johnson, 1998). A study employing the SIMMENTO weather generator found that the variability (standard deviations) of wet fractions and amounts were significantly overestimated by the synthetic historical series (Elshamy et al., 2006). A major drawback of the parametric approach is that the Markov chain does not take into account the previous days' weather. As a result of this, the rare events, such as droughts or wet spells are not adequately produced (Sharif and Burn, 2007; Semenov and Barrow, 1997; Dibike and Coulibaly, 2005). Another limitation of the parametric weather generators is that an assumption must be made about the probability distribution of precipitation amounts, and different distributions do not give similar results (Sharif and Burn, 2007). Furthermore, the weather generators cannot be easily transferred to other basins as their underlying probability assumptions would change (Sharif and Burn, 2006). The computational effort is also significantly higher than other methods since many parameters must be estimated and statistically verified (Mehrotra et al., 2006). Parametric

weather generators are less easily applied to multiple sites as simulations occur independently and thus spatial correlations would have to be assumed.

Semi-Parametric or Empirical weather generators include LARS-WG and the Wilks model, SDSM (Semenov and Barrow, 1997; Wilks and Wilby, 1999). LARS-WG differs from the parametric approaches described above because it employs a series-approach in which the wet and dry spells are determined by taking into account the observed values and assuming mixed-exponential distributions for dry/wet series as well as precipitation amounts (Semenov and Barrow, 1997). The wet/dry day status is first chosen, and then the amount is chosen conditional on the status. As such, the LARS-WG was able to satisfactorily reproduce wet and dry spells, unlike the parametric weather generators (Dibike and Coulibaly, 2005). Wilks (1998) improved on the parametric models of Richardson (1981) by introducing Markov-chains of higher order that have a better "memory" of the preceding weather. The Richardson (1981) model was further extended for multi-site applications by using a collection of single site models in which a conditional probability distribution is specified and thus spatially correlated random numbers can be generated (Mehrotra, 2006; Wilks, 1998). A drawback to these empirical approaches is that there is still a subjective assumption about the type of probability distribution for precipitation amounts and spell lengths, and the spatial correlation structure is empirically estimated for use with multiple sites.

Non-parametric weather generators are computationally simple and do not require any statistical assumptions to be made. They work by using a nearest-neighbor resampling procedure known as the K-NN approach (Sharif and Burn, 2007; Brandsma and Buishand, 1998; Beersma et al., 2002; Yates et al., 2003). The nearest neighbor

algorithm works by searching the days in the historical record that have similar characteristics to those of the previously simulated day, and then randomly selecting one of these as the simulated value for the next day (Beersma et al., 2002). This approach is easily used in multi-site studies because the values are simulated concurrently, thus spatial correlation is preserved (Mehrotra et al. 2006). The K-NN algorithm has been successfully used for multi-site hydrological impact assessments in the Rhine Basin, accurately preserving spatial correlation and climatic variability (Beersma et al., 2002; Brandsma and Buishand, 1998). Apipattanavis et al. (2007) compared a K-NN to a semi-parametric weather generator. Box plots of wet-spell lengths showed that for some months the semi-parametric model could not reproduce maximum wet spell lengths, and average spell lengths were underestimated for the traditional K-NN model. A major limitation to the K-NN approach is that the values are merely reshuffled, thus no new values are produced (Sharif and Burn, 2007). Climatic extremes are essential in predicting flooding events in response to climate change, thus Sharif and Burn (2007) modified the K-NN algorithm to produce unprecedented precipitation amounts by introducing a perturbation component in which a random component is added to the resampled data points (Sharif and Burn, 2007). Monthly total precipitation and total monthly wet day box plots were used to evaluate the performance of the Modified K-NN algorithm. The algorithm was able to satisfactorily reproduce the statistics of the original dataset while adding variability, which is crucial in hydrologic impact assessments (Sharif and Burn, 2007). Prodanovic and Simonovic (2006) altered the Modified K-NN algorithm of Sharif and Burn (2007) to account for the leap year. In order to allow for more variables for an improved selection of nearest neighbor, principal components are

added in the weather generator (WG-PCA). With the inclusion of more variables and perturbations, the updated model is expected to more accurately define both present day climate conditions and also to produce estimates of future climate scenarios.

However, studies have indicated that the task of downscaling can sometimes become challenging due to the absence of proper station measurements. Gridded databases, such as the National Center for Environmental Prediction – National Center for Atmospheric Research (NCEP-NCAR) Global Reanalysis – NNGR (Kalnay et al., 1996) and the North American Regional Reanalysis – NARR (Mesinger et al., 2006) can be viable alternatives for alleviating these limitations of missing data and spatial bias resulting from uneven and unrepresentative spatial modelling (Robeson and Ensor, 2006; Ensor and Robeson, 2008). The reanalysis data are advantageous in impact studies because they are based on the AOGCMs with a fixed dynamic core, physical parameterizations and data assimilation systems (Castro et al., 2007).

Global (NNGR) and regional (NARR) reanalysis databases are also gaining use in uncertainty assessment studies. In many of their applications, however, the NNGR resolution (250 km × 250 km) is not satisfactory, especially in regions with a complex topography (Choi et al., 2009; Tolika et al, 2006; Rusticucci and Kousky, 2002; Haberlandt and Kite, 1998; Castro et al., 2007). The NARR dataset (Mesinger et al., 2006) is a major improvement upon the global reanalysis datasets in both resolution and accuracy. Literature related to an inter-comparison between the global and regional datasets (Nigam and Ruiz-Barradas, 2006; Woo and Thorne, 2006; Castro et al., 2007; Choi et al., 2007 and 2009) shows better agreement of NARR data. More recently, Solaiman and Simonovic (2010a) conducted a rigorous assessment of the NARR and

NNGR database for application in the Upper Thames river basin (Ontario, Canada), for hydrological modeling and/or climate change impact studies.

2.2 Multi-Model Ensembles for Uncertainty Research

In most of the climate change impact assessment studies, single AOGCMs have been used for predicting future climate. It is well understood that in the current context of huge uncertainties, the utilization of a single AOGCM may only represent a single realization out of a multiplicity of possible realizations, and therefore cannot be representative of the future. So, for a comprehensive assessment of future changes in climate conditions, it is important to use collective information by utilizing all available models and by synthesizing the projections and uncertainties in a probabilistic manner.

Studies that used multiple climate model information are, however, cannot be found in abundance. Of the literatures available, one of the common approaches is the use of reliability estimates to multi-model ensembles. The earliest research, to our knowledge, to consider a multimodel ensemble approach was conducted by Raisanen and Palmer (2001), who treated the ensemble members as equally probable realizations and determined probabilities of climate change by computing the fraction of ensemble members in which the differential properties of models, such as bias and rate of convergence, were disregarded.

Giorgi and Mearns (2003) confronted the approach undertaken in Raisanen and Palmer by introducing the "Reliability Ensemble Averaging (REA)" technique, which considered the reliability-based likelihood of realization by models to calculate the

probability of regional temperature and precipitation change. They found this technique to be more flexible in the assessment of risk and cost in regional climate change studies.

Tebaldi et al. (2004; 2005) used Bayesian statistics to estimate a distribution of future climates through the combination of past observational data and the corresponding AOGCM simulated climates. This technique was motivated by the assumption that an AOGCM ensemble represents a "sample of the full potential climate model space compatible with the observed climate using probability distributions (PDFs)" at a regional scale.

Recently, Smith et al. (2009) extended the work of Tebaldi et al. by introducing the univariate approach to consider one region at a time. They are still using a multivariate approach, including cross validation, to confirm the resemblance of the Bayesian predictive distributions. Other literature on Bayesian methods in multi-model ensembles includes work from Allan et al. [2000], Benestad [2004], Stone and Allan [2005], and Jackson et al. [2004].

Another class of new but promising uncertainty estimation methods incorporates the downscaling of AOGCM scenarios and quantifying uncertainties by separately weighting outputs from different AOGCMs in each time step based on their performances. The results can be presented in a probabilistic framework. Wilby and Harris [2006] developed a probabilistic framework to combine information from four AOGCMs, two greenhouse scenarios where the AOGCMs were weighted to an index of reliability for downscaled effective rainfall. A Monte Carlo approach was adopted to explore components of uncertainty affecting projections for the river Thames for 2080s. The resulting cumulative

distribution functions appeared to be most sensitive to uncertainty in (i) the selection of climate change scenarios, and (ii) the downscaling of different AOGCMs.

Ghosh and Mujumdar (2007) used NNGR to develop a methodology capable of assessing AOGCM uncertainty due to different AOGCMs by considering different probability density functions for each time step. They used the information on uncertainty in examining future drought scenarios in a nonparametric manner. Samples of drought indicators were generated with results from downscaled precipitation using a statistical regression approach from available AOGCMs and scenarios. The severity of droughts was presented in a nonparametric kernel estimation and orthonormal approach.

The implications of uncertainties in estimating the severity of extreme precipitation events is an area of research not yet fully explored. The present study aims to compare the uncertainties of precipitation change on a watershed scale by using two very different methods: the Bayesian Reliability Ensemble Average (BA-REA) by Tebaldi et al. (2004; 2005) and the nonparametric kernel estimator. A classification scheme for investigating the severity level of extreme precipitation indices is addressed. Finally, the nonparametric data driven kernel density estimation methods are investigated to quantify uncertainties associated with AOGCM and scenario outputs for extreme precipitation events.

3. Methodology

3.1 Study Area

The Upper Thames River (UTR) basin (Figure 1) ($42^0 35'24''$N, $81^0 8'24''$W), located in Southwestern Ontario, Canada, is a 3,500 km^2 area nested between the Great Lakes of Huron and Erie. The basin often experiences major hydrologic hazards, such as floods and droughts. The basin has a well documented history of flooding events dating back to the 1700s (Prodanovic and Simonovic 2006).

Figure 1: The Upper Thames River Basin

High flows mostly take place in early March after snowmelt, and again in July and August as a result of summer storms. Khaliq et al (2008) reported that in the Canadian regime, low flow conditions follow a seasonal behavioral pattern: summer low flow occurs between June to November and winter low flow during the December and May periods. The UTR basin experiences frequent low flow conditions between June and September (Prodanovic and Simonovic 2006).

The population of the basin is approximately 450,000 (2006), of which 350,000 are the residents of the City of London. The Thames river basin consists of two majors tributaries of the river Thames: the North Branch (1,750 km^2), flowing southward through Mitchell and St. Mary's, and eventually into London, and the South Branch (1,360 km^2), flowing through Woodstock, Ingersoll, and east London. The Upper Thames River basin receives about 1,000 mm of annual precipitation, 60% of which is lost through evaporation and/or evapotranspiration, stored in ponds and wetlands, or recharged as groundwater (Prodanovic and Simonovic 2006).

3.2 Database

3.2.1 Selection of Predictors

Daily precipitation and temperature are the most important atmospheric forcing parameters required for any hydrologic impact study for a larger river basin (Salathe Jr., 2003). However, climate models do not resolve important mesoscale and surface features that control precipitation in an area. The choice of appropriate predictors or characteristics from the large-scale atmospheric circulation is one of the most important steps in downscaling. Rainfall can be related to air mass transport and thus related to

atmospheric circulation, which is a consequence of pressure differences and anomalies (Bardossy, 1997). Mean sea level pressure is the basis of derived variables such as surface vorticity, airflow strength, meridional and zonal flow components and divergence (Wilby and Wigley, 2000). Specific humidity is recognized as significant for AOGCM precipitation schemes (Hennessy et al., 1997). Considering all the above factors, predictor variables mentioned in Table 1 are initially chosen to generate precipitation in this study.

Table 1: Definition of Predictor Variables

Predictors	Abbreviations
Precipitation (mm/day)	Precip
Maximum temperature (^{0}C)	Tmax
Minimum temperature (^{0}C)	Tmin
Mean sea level pressure (Pa)	MSL
Specific humidity (Kg/ Kg)	SPFH
Zonal (eastward) wind velocity component (m/s) at 10 m	UGRD
Meridional (northward) wind velocity component (m/s) at 10 m	VGRD

Daily observed precipitation (precip), maximum and minimum temperature (Tmax and Tmin) data from 22 stations covering the UTR basin for the period of 1979-2005 is collected from Environment Canada (http://www.climate.weatheroffice.gc.ca/climateData/canada_e.html) (Table 2).

The rest of the atmospheric variables are collected from the NARR reanalysis dataset for the period of 1979 – 2005. Precipitation values less than 0.5 mm day^{-1} are considered zero as suggested by Reid et al. (2001) and Choi et al. (2007). NARR data for this study has been made available through the Data Access Integration of the Canadian Climate Change Scenarios Network of Environment Canada.

Table 2: Weather Stations used for Uncertainty Estimation

| Serial | Station Name | Location | | | Correlation |
		Latitude (^{0}N)	Longitude (^{0}W)	Elevation (m)	
1	Blyth	43.72	81.38	350.50	0.42
2	Brantford	43.72	81.38	196.00	0.65
3	Chatham	42.38	82.20	180.00	0.49
4	Delhi	42.87	80.55	231.70	0.66
5	Dorchester	43.00	81.03	271.30	0.79
6	Embro	43.25	80.93	358.10	0.70
7	Exeter	43.35	81.50	262.10	0.57
8	Fergus	43.73	80.33	417.60	0.56
9	Foldens	43.02	80.78	328.00	0.73
10	Glen Allan	43.68	80.71	400.00	0.57
11	Hamilton A	43.17	79.93	237.70	0.67
12	Ilderton	43.05	81.43	266.70	0.70
13	London A	43.03	80.15	278.00	0.56
14	Petrolia Town	42.86	82.17	201.20	0.52
15	Ridge Town	42.45	81.88	205.70	0.68
16	Sarnia	43.00	82.32	180.60	0.63
17	Stratford	43.37	81.00	345.00	0.61
18	St. Thomas	42.78	81.17	209.10	0.68
19	Tilsonburg	42.86	80.72	213.40	0.73
20	Waterloo A	43.46	81.38	317.00	0.72
21	Woodstock	43.14	80.77	281.90	0.49
22	Wroxeter	43.86	81.15	335.00	0.42

Data source: National Climate Data and Information Archive of Environment Canada

(http://climate.weatheroffice.ec.gc.ca/climateData/canada_e.html, Retrieved 14/11/2007)

3.2.2 Future Climate Change Scenarios

The Canadian Climate Change Scenarios Network (CCCSN) provides access to several AOGCM models and emissions scenarios. The website allows the user to specify the range of geographical co-ordinates required, as well as the climatic variable and time period of interest. For the purpose of this study, the time slices collected were 1960-1990 (baseline), 2011-2040 (2020's) and 2071-2100 (2080s). Seven variables were chosen: minimum temperature, maximum temperature, precipitation, specific humidity, northward wind component, southward wind component and mean sea level pressure. Six AOGCM models were collected, each with two to three emissions scenarios, as specified by the IPCC's Special Report on Emissions Scenarios (Nakicenovic et al, 2000). Full descriptions of the emissions scenarios can be found in Appendix A. Table 3 lists the AOGCM's along with the emissions scenarios available and their origin. Appendix B provides descriptions of each AOGCM.

Both NARR and the AOGCM datasets are processed to conform to the station's grid points.

3.3 Multi-Model Uncertainty Estimation Methods

Two approaches based on fundamentally different assumptions are applied to estimate uncertainty in climate model projections of future precipitation under different forcing scenarios. First, a Bayesian statistics approach is applied to estimate a distribution of future climates from the combination of past observed and corresponding AOGCM-simulated data. Next, a methodology combining statistical downscaling using a PCA-based weather generator approach and nonparametric kernel density estimation technique is developed to quantify the uncertainties from AOGCMs. The difference between these

two approaches lies in the fact that the BA-REA method combines uncertainties from different AOGCMs based on its mean bias, so a single weight for different models is present; whereas the nonparametric kernel estimator is capable of providing weights for any point of interest.

Table 3: AOGCM Models and Emission Scenarios used for Uncertainty Estimation

GCM Models	Sponsors, Country	SRES Scenarios	Atmospheric Resolution	
			Lat	Long
CGCM3T47, 2005	Canadian Centre for Climate Modelling and Analysis, Canada	A1B, A2, B1	3.75°	3.75°
CGCM3T63, 2005		A1B, A2, B1	2.81°	2.81°
CSIROMK3.5, 2001	Commonwealth Scientific and Industrial Research Organization (CISRO) Atmospheric Research, Australia	A2, B1	1.875°	1.875°
GISSAOM, 2004	National Aeronautics and Space Administration (NASA)/ Goddard Institute for Space Studies (GISS), USA	A1B, B1	3°	4°
MIROC3.2HIRES, 2004	Centre for Climate System Research (University of Tokyo), National Institute for Environmental Studies, and Frontier Research Centre for Global Change (JAMSTEC), Japan	A1B, B1	1.125°	1.125°
MIROC3.2MEDRES, 2004		A1B, A2, B1	2.8°	2.8°

Data source: Canadian Climate Change Scenario Network Website, (http://cccsn.ca/?page=dd-gcm, Retrieved 9/20/2008)

3.3.1 The Bayesian Reliability Ensemble Average (BA-REA) Method

The methodology developed by Tebaldi et al. (2004; 2005) consists of a formal Bayesian implementation and extension of the reliability ensemble averaging (REA) approach of Giorgi and Mearns (2002; 2003). It combines data from observations and a multi-model ensemble of AOGCMs to compute PDFs of future temperature and precipitation change over large regions under different forcing scenarios. Three components constitute the model structure: prior, likelihood, and posterior. The assumption is that the variability of present and future climate from different AOGCMs are random quantities and have different variances which are priori unknown. Although uninformative prior distribution has been chosen, both model-generated and observational data are applied for calculating meaningful posterior distributions.

The choice of an uninformative prior distribution has the advantage of selecting parameter estimates similar to non-Bayesian approaches, such as maximum likelihood. In cases where there is no sufficient agreement between experts to determine a specific prior and no data from previous studies could be incorporated, (a situation similar to wide range of future climate scenarios), selection of an uninformative prior is justified.

The choice of the likelihood or distribution of the data as a function of any random parameters constitutes the second parameter. The AOGCM responses are assumed to have a symmetric distribution whose center is the 'true value' of the variable of interest, but maintains an individual variability to be a measure of how well each AOGCM depicts the natural variability.

The prior and posterior distributions are combined into a joint posterior distribution using the Bayes' theorem. The empirical estimate of the posterior distribution is obtained

using the Markov Chain Monte Carlo (MCMC) simulation by simulating samples from the posterior distribution.

Likelihoods

The likelihoods for the observations of current mean precipitation (X_0), simulations of present (X_j) and future (Y_j) mean precipitation by the ith model can be written as:

$X_0 \sim N[\mu, (\lambda_0)^{-1}]$, the likelihood of the observations of current climate

Or

alternately,

$X_o = \mu + \epsilon_o$

$X_i \sim N[\mu, (\lambda_i)^{-1}]$ (3.1)

Or alternately,

$X_i = \mu + \eta_i$ (assuming a common Gaussian distribution for the error terms)

$Y_i \sim N[\nu + (\theta\lambda_i)^{-1}]$

Or alternately,

$Y_i = \nu + \beta_x(X_i - \mu) + \xi_i/\sqrt{\theta}$ (assuming a common Gaussian distribution for the error

terms)

Where, μ and ν are random variables presenting the (unknown) true present and future mean precipitations respectively. $(\lambda_0)^{-1}$ and $(\lambda_i)^{-1}$ can be considered as a measure of ith AOGCM precision, and the estimates of natural observed variability, which

depends on the season, region and time average of the observation. The parameter λ_0 is fixed as the reciprocal of the squared value of the standard deviation of the observations. Random variable θ allows for the possibility of the future and present precipitations having different variances by a multiplicative factor and is common to all AOGCMs.

The alternate forms of equation 3.1 links X_i and Y_i through a linear regression equation equivalent to assuming that (X_i, Y_i) are jointly normal when parameter values are given and the correlation coefficient is relaxed to vary between -1 and + 1. For $\beta_x \neq 0$, the modified equation for Y_i will create a direct (if positive) or inverse (if negative) relation between $X_i - \mu$ and $Y_i - \nu$. The value of β_x is also significant for representing the correlation: a value of 1 denotes the conditional independence of the signal of precipitation change produced by any AOGCM and $X_i - \mu$, the model bias for current precipitation. Values greater or smaller than 1 imply a positive or negative correlation between them.

Prior Distribution

The prior distributions are chosen for the following precision parameters:

$\lambda_i = 1,2,3, \dots .6$ have Gamma prior densities (Ga(a,b)):

$$\frac{b^a}{\Gamma(a)} \lambda_i^{a-1} exp^{-bx} \tag{3.2}$$

Where, a and b are known. Similarly for θ, c, d are assumed to be known. For the model, $a = b = c = d = 0.001$ are chosen.

The true climate means μ and ν for present and future precipitation have uniform prior densities so that even in case of improper priors (do not integrate to one) they are assumed to have a proper posterior density function.

Posterior Distribution

Bayes' theorem is applied to the likelihood and propers. The resulting joint posterior distribution is given by:

$$\prod_{i=1}^{15}\left[\lambda_i^{a-1}e^{-b\lambda_i}\lambda_i\theta^{1/2}exp\left\{-\frac{\lambda_i}{2}(X_i-\mu)^2+\theta(Y_i-\nu)^2\right\}\right].\theta^{c-1}e^{-d\theta}.exp\left\{-\frac{\lambda_0}{2}(X_0-\mu)^2\right\}$$

(3.3)

The above distribution does not represent any specific known parameter family. The posterior distribution fixes the parameters and considers a conditional posterior for others to synthesize the data and the prior assumptions. For example, the distribution of μ for fixing all other parameters is Gaussian with

Mean:

$$\tilde{\mu}=\left(\sum_{i=0}^{15}\lambda_iX_i\right)\Big/\left(\sum_{i=0}^{15}\lambda_i\right)$$

(3.4)

Variance:

$$\left(\sum_{i=0}^{15}\lambda_i\right)^{-1}$$

(3.5)

Similarly, the conditional distribution of ν is Gaussian with

Mean:

$$\tilde{v} = \left(\sum_{i=0}^{15} \lambda_i Y_i\right) \Big/ \left(\sum_{i=0}^{15} \lambda_i\right) \tag{3.6}$$

Variance:

$$\left(\theta \sum_{i=0}^{15} \lambda_i\right)^{-1} \tag{3.7}$$

Equations 3.4 and 3.6 are comparable to the REA results as the weighted means of the 15 different AOGCMs with their scenarios and the observation with weights $\lambda_1, \ldots \ldots \lambda_{15}, \lambda_0$, respectively. These weights are derived by assuming parameters with random quantities and hence can be used for uncertainty estimation. This uncertainty will inflate the width of the posterior distributions of v, μ and also the precipitation change, ΔP.

The mean of the posterior distribution of the $\lambda_i s$ for $i = 1, 2, \ldots 15$ is approximated as:

$$E(\lambda_i | \{X_0, , \ldots \ldots, X_{15}, Y_1, \ldots, Y_{15}\}) \approx \frac{a+1}{b + \frac{1}{2}((X_i - \tilde{\mu})^2 + \theta(Y_i - \tilde{v})^2)} \tag{3.8}$$

Equation 3.8 expresses how the bias and convergence criteria are built into the model implicitly since the precision parameter or the weights λ_i for each AOGCM are large provided the bias $|X_i - \mu|$ and convergence $|Y_i - v|$ or the distance of the ith model future response from the overall average response are small. So the results are strictly constrained by their convergence into future projections determined by the weighted

ensemble of mean. For this study, *a=b=0.001* is chosen as per Tebaldi et al. (2004, 2005) to ensure that the contribution of the prior assumption to equation 3.8 is negligible.

Using the approximation similar to equation 3.1 the posterior mean can be written as:

$$E(\lambda_i | \{X_0, , \ldots \ldots, X_{15}, Y_1, \ldots, Y_{15}\})$$

$$\approx \frac{a+1}{b + \frac{1}{2}\left((X_i - \tilde{\mu})^2 + \theta\left(Y_i - \tilde{v} - \beta_x(X_i - \tilde{\mu})\right)^2\right)} \tag{3.9}$$

Next, the marginal posterior distribution is derived using the MCMC approach. A large number of sample values are generated by applying the Gibbs Sampler using equation 3.3 for all parameters.

MCMC Approach: The Gibbs Sampler

The joint posterior distribution derived from assuming different distributions such as Gaussian, Uniform and Gamma in different stages, does not represent any known parametric family of distributions. Because they are conjugate, they allow for a closed-form deviation of all full conditional distributions.

Auxiliary randomization parameters s_i and $t_i, i = 1,2,3, \ldots \ldots .15$ are used to ensure an efficient simulation from student's t distribution within the Gibbs sampler. Fixing $s_i = t_i = 1, \beta_x = 0$, returns the full conditionals to the prior parameters.

$$\lambda_i | \ldots \ldots \ldots \sim Ga\left(a + 1, b + \frac{s_i}{2}(X_i - \mu)^2 + \frac{\theta t_i}{2}\{Y_i - v - \beta_x(X_i - \mu)\}^2\right) \tag{3.10}$$

$$s_i | \ldots \ldots \ldots \ldots \ldots . \sim Ga\left(\frac{\phi+1}{2}, \frac{\phi+\lambda_i(X_i-\mu)^2}{2}\right) \tag{3.11}$$

$$t_i | \ldots \ldots \ldots \ldots \ldots . \sim Ga\left(\frac{\phi+1}{2}, \frac{\phi+\theta\lambda_i\{Y_i-\nu-\beta_x(X_i-\mu)\}^2}{2}\right) \tag{3.12}$$

$$\mu | \ldots \ldots \ldots \ldots \ldots . \sim N\left(\tilde{\mu}, \left(\sum s_i\lambda_i + \theta\beta_x^2\sum t_i\lambda_i + \lambda_0\right)^{-1}\right) \tag{3.13}$$

$$\nu | \ldots \ldots \ldots \ldots \ldots . \sim N\left(\tilde{\nu}, \left(\theta\sum t_i\lambda_i\right)^{-1}\right) \tag{3.14}$$

$$\beta_x | \ldots \ldots \ldots \ldots \ldots . \sim N\left(\widetilde{\beta_x}, (\theta\sum t_i\lambda_i + (X_i-\mu)^2)^{-1}\right) \tag{3.15}$$

$$\theta | \ldots \ldots \ldots \ldots \ldots . \sim Ga(c+\frac{N}{2}, d+\frac{1}{2}\sum t_i\lambda_i\{Y_i-\nu-\beta_x(X_i-\mu)\}^2) \tag{3.16}$$

Simplifying,

$$\tilde{\mu} = \frac{\sum s_i\lambda_iX_i - \theta\beta_x\sum\lambda_it_i(Y_i-\nu-\beta_xX_i) + \lambda_0X_0}{\sum s_i\lambda_i + \theta\beta_x^2\sum\lambda_it_i + \lambda_0} \tag{3.17}$$

$$\tilde{\nu} = \frac{\sum t_i\lambda_i\{Y_i - \beta_x(X_i-\mu)\}}{\sum t_i\lambda_i} \tag{3.18}$$

$$\widetilde{\beta_x} = \frac{\sum t_i \lambda_i \{(Y_i - \nu)(X_i - \mu)\}}{\sum t_i \lambda_i (X_i - \mu)^2} \tag{3.19}$$

From this sequence of full conditional distributions, the Gibbs sampler is coded to simulate iteratively. After a series of iterations, the MCMC process ignores the arbitrary set of initial values for parameters. Values sampled at each iteration represents a draw from the joint posterior distribution of interest, and any summary statistic can be computed to a degree of approximation that is a direct function of the number of the sampled values available, and an inverse function of the correlation between successive samples.

The reliability of any AOGCM is measured by two criteria to form the shape of the posterior distribution as a consequence of assumptions formulated in the statistical model: mean bias of present climate and rate of convergence of the future climate models to weighted ensemble mean.

Model parameters

For this study, the area averaged precipitation response from all 15 AOGCMs and scenarios, averaged for the London station, is considered to compare with the PDFs generated by the methodology presented in Section 3.3.1.

Data and model setup

To generate PDF of precipitation affected by climate change, simulated present (1961-1990) and future (2041-2070) precipitation (X_i, Y_i) are considered for the winter (December-January-February) and summer (June-July-August) seasons. The outputs

from 15 different sets of experiments and from 6 AOGCMs for the two time slices are extracted for the 22 stations and averaged for the London station using the nearest neighbor approach. The natural variability is expressed as the inverse of the variance of observed precipitation for 1961-1990 (X_0). It is calculated as the inter-annual variance on the basis of the observed record (X_0). The computer codes used in this study can be downloaded from the website of the National Centre for Atmospheric Research (*http://www.image.ucar.edu/~nychka/REA/*).

3.3.2 Nonparametric Kernel Estimators

Downscaling

Stochastic weather generators simulate weather data to assist in the formulation of water resource management policies. The basic assumption for producing synthetic sequences is that the past will be representative of the future. These sequences are essentially complex random number generators, which can be used to produce a synthetic series of data. This allows the researcher to account for natural variability when predicting the effects of climate change.

In order to reduce multi-dimensionality and collinearity associated with the large number of input variables, a principal component analysis has been integrated within the weather generator. The process requires selecting the appropriate principal components (PCs) that will adequately represent most of the information of the original dataset.

The WG-PCA algorithm with p variables and q stations works through the following steps:

1) Regional means of p variables for all q stations are calculated for each day of the

observed data:

$$\bar{X}_t = \lfloor \bar{x}_{1,t}, \bar{x}_{2,t}, \dots \bar{x}_{p,t} \rfloor \qquad \forall t = \{1,2, \dots . T\} \qquad (3.20)$$

Where,

$$\bar{x}_{i,t} = \frac{1}{q} \sum_{j=1}^{q} x_{i,t}^{j} \qquad \forall t = \{1,2, \dots . p\} \qquad (3.21)$$

2) The user-set parameters are as follows: potential neighbors, L days long where $L = (w + 1) \times (N - 1)$ for each of p individual variable with N years of historic record, and a temporal window of size w. The days within the given window are all potential neighbors to the feature vector. N data which correspond to the current day are deleted from the potential neighbors so the value of the current day is not repeated.

3) Regional means of the potential neighbors are calculated for each day at all q stations.

4) A covariance matrix, C_t of size $L \times p$ is computed for day t.

5) The first time step value is randomly selected for each of p variables from all current day values in the historic record.

6) Next, using the variance explained by the first principal component, Mahalanobis distance is calculated with equation 3.33.

$$d_k = \sqrt{(PC_t - PC_k)^2 / Var(PC)} \qquad \forall k = \{1,2, \dots . K\} \qquad (3.22)$$

where,

PC_t is the value of the current day;

PC_k is the nearest neighbor transferred by the Eigen vector.

$Var(PC)$ is the variance of the first principle component is for all K nearest neighbors.

7) The selection of the number of nearest neighbors, K, out of L potential values using $K = \sqrt{L}$.

8) The Mahalanobis distance d_k is put in order of smallest to largest, and the first K neighbors in the sorted list are selected (the K Nearest Neighbors). A discrete probability distribution is used that weights closer neighbors highest in order to resample out of the set of K neighbors. Using equations 3.34 and 3.35, the weights, w, are calculated for each k neighbor.

$$w_k = \frac{\frac{1}{k}}{\sum_{i=1}^{k}\frac{1}{i}} \qquad \forall k = \{1, 2, \dots, K\} \qquad (3.23)$$

Cumulative probabilities, p_j, are given by:

$$p_j = \sum_{i=1}^{j} w_i \qquad\qquad (3.24)$$

9) A random number $u(0,1)$ is generated and compared to the cumulative probability calculated above in order to select the current day's nearest neighbor. If $p_1 < u < p_k$, the day j for which u is closest to p_j is selected. However, if $p_1 > u$, then the day that corresponds to d_1 is chosen. For $u = p_k$, the day that corresponds to day d_k is selected. Upon selecting the nearest neighbor, the K-NN algorithm chooses the weather of the selected day for all stations in order to preserve spatial correlation in the data (Eum et al,

2009).

10) In order to generate values outside the observed range, perturbation is used. A conditional standard deviation σ for K nearest neighbors is estimated. For choosing the optimal bandwidth of a Gaussian distribution function that minimizes the asymptotic mean integrated square error (AMISE), Sharma et al. (1997) reduced Silverman's (Silverman 1986, pp. 86-87) equation of optimal bandwidth into the following form for a univariate case:

$$\lambda = 1.06\sigma K^{-\frac{1}{5}} \qquad (3.25)$$

Using the mean value of the weather variable $x_{i,t}^{j}$ obtained in step 9 and variance$(\lambda\sigma_i^j)^2$, a new value $y_{i,t}^j$ can be achieved through perturbation (Sharma et al. 1997).

$$y_{i,t}^j = x_{i,t}^j + \lambda\sigma_i^j Z_t \qquad (3.26)$$

where,

z_t is a random variable, distributed normally (zero mean, unit variance) for day t. Negative values are prevented from being produced for precipitation by employing a largest acceptable bandwidth (Sharma and O'Neil, 2002):

$$\lambda_a = x_{*,t}^j \Big/ 1.55\sigma_*^j \qquad (3.27)$$

where,

* refers to precipitation.

If again a negative value is returned, a new value for z_t is generated (Sharif and Burn, 2006).

Kernel based Nonparametric Uncertainty Estimator

A practical approach to deal with AOGCM and scenario uncertainties initiating from inadequate information and incomplete knowledge should: (1) be robust with respect to model choice; (2) be statistically consistent in a uniform application across different area scales such as global, regional or local/watershed scales; (3) be flexible enough to deal with the variety of data; (4) obtain the maximum information from the sample; and (5) lead to consistent results. Most parametric methods do not meet all these requirements.

The Probability Density Function (PDF) is commonly used to describe the nature of data. In applications an estimate of the unknown $PDF = f(\ )$ based on random sample $x_1, x_2, \ldots \ldots x_n$ from $f(\ )$ is calculated in the form of $\widehat{PDF} = \hat{f}(\ )$. Probability distribution functions estimated by any nonparametric method without prior assumptions are suitable for quantifying AOGCM and scenario uncertainties. Several approaches, such as kernel methods, orthogonal series methods, penalized-likelihood methods, k-nearest neighbor methods, Bayesian-spline methods, and maximum-likelihood or histogram like methods, are used throughout the the relevant literature (Adamowski, 1985).

A Kernel density estimation method has been widely used as a viable and flexible alternative to parametric methods in hydrology (Sharma et al., 1997; Lall, 1995), flood frequency analysis (Lall et al., 1993; Adamowski, 1985), and precipitation resampling (Lall et al., 1996) for estimating a probability density function.

A kernel density estimate is formed through the convolution of kernels or weight functions centered at the empirical frequency distribution of the data. A kernel density estimator involves the use of the kernel function (K(x)) defined by:

$$\int_{-\infty}^{\infty} K(x)dx = 1 \tag{3.28}$$

A PDF can thus be used as a kernel function. The Parzen-Rosenbalt kernel density estimate $f_n(x)$ at x, from a sample of $\{x_1, \ldots, x_i, \ldots, x_n\}$ of sample size n is given by:

$$\widehat{f_h}(x) = \frac{1}{n}\sum_{i=1}^{n}\frac{1}{h}K_h\left(\frac{x - x_i}{h}\right) \tag{3.29}$$

Where $t = \left(\frac{x-x_i}{h}\right)$ and $k_h(t)$ is a weight or kernel function required to satisfy criteria such as symmetry, finite variance, and integrates to unity. Successful application of any kernel density estimation depends more on the choice of the smoothing parameter or bandwidth *(h)* than it does on the type of kernel function *K(.)*, to a lesser extent.

The bandwidth for kernel estimation may be evaluated by minimizing the deviation of the estimated PDF from the actual one. Assuming a normal distribution for the bandwidth estimation, the optimal bandwidth for a normal kernel can be given by (Polansky and Baker, 2000):

$$h_n = (1.587)\hat{\sigma}n^{-\frac{1}{3}} \tag{3.30}$$

Where $\hat{\sigma}$ is the sample standard deviation measured by Silverman [1986]:

$$\hat{\sigma} = min \left\{ S, \frac{IQR}{1.349} \right\} \tag{3.31}$$

Where S is the sample standard deviation and IQR is the interquartile range.

This methodology is applied to derive the PDF of the mean monthly precipitation at different time steps.

Data preprocessing and experimental setup

A schematic of estimating the PDFs combining uncertainties using downscaling technique is presented in Figure 2. For this study, daily input variables from NARR, as indicated in Table 2, are collected at the nearest grid points and spatially interpolated to the stations (Table 1) surrounding the Upper Thames River basin.

While the direct downscaling of minimum and maximum temperature has produced good results, precipitation values are not well reproduced directly from AOGCM data
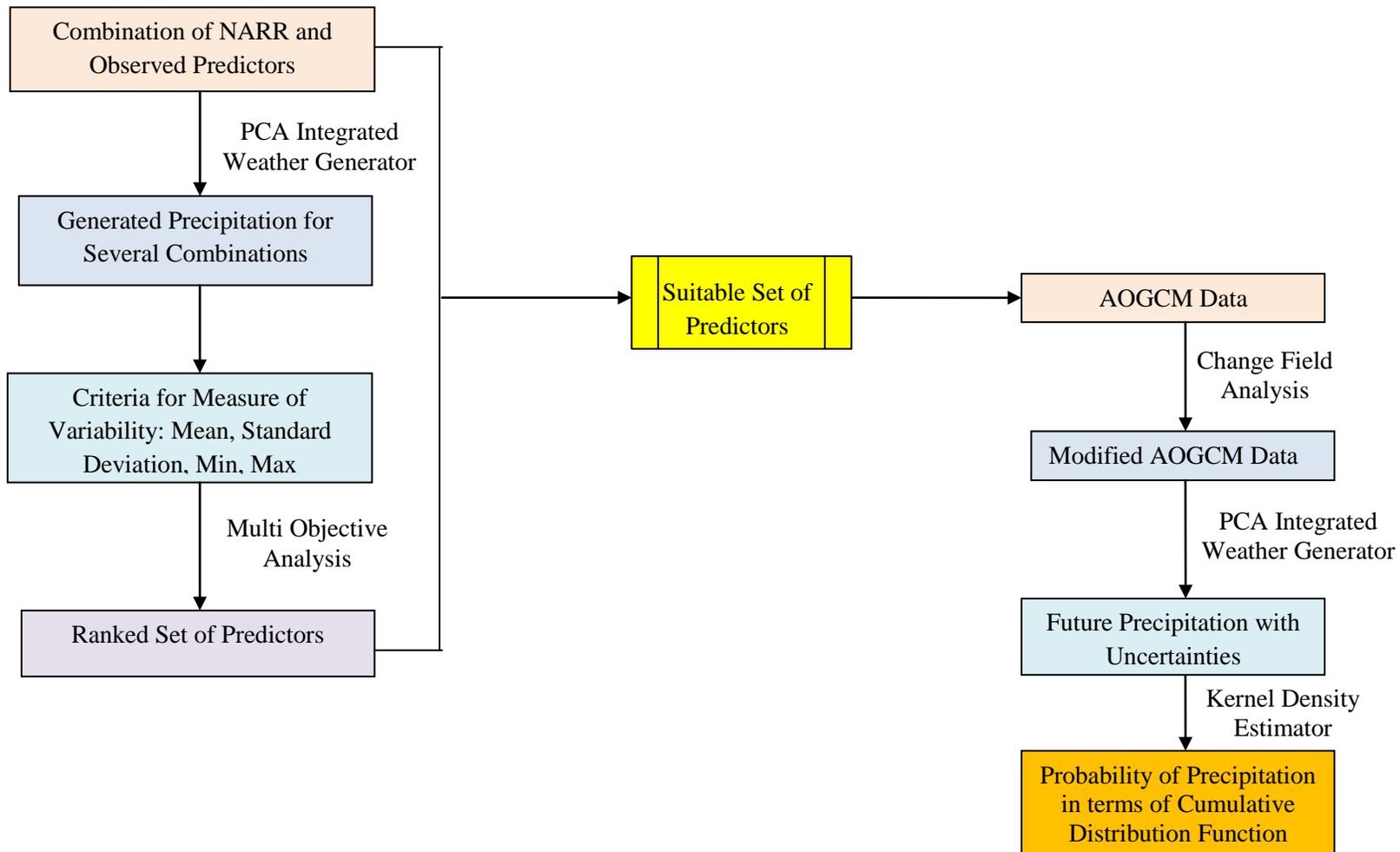
Figure 2: Flow Chart of Uncertainty Estimation using Nonparametric Method

(Brissette et al., 2006). For selection of appropriate conditioning variables, several combinations of predictors, which are listed in Table 3, are used to generate synthetic versions of the historic dataset. A multi-objective Compromise Programming tool is then used to find an optimal set of predictors. Assessment of trade-offs between different combinations of variables (considered as alternatives) is done according to four variability measures (considered as criteria): mean, standard deviation, maximum and minimum values for each month. The rank of each combination is measured by the compromise programming distance metric, which is calculated as the distance from the ideal solution for each alternative. Table 4 presents the ranks obtained for each combination of predictors. It is clear that a combination of all seven predictors is closest to the ideal solution in most months, and is therefore selected for the purposes of further analysis.

Table 4: Rank Table of Different Combinations of Predictors

Cases	Months						
	1 2	3 4	5 6	7 8	9 10	11	12
P, Tmax, Tmin, PRMSL	7 6	5 6	3 1	1 5	7 4	6	1
P, Tmax, Tmin, PRMSL, SPFH	4 1	7 5	4 2	7 7	6 1	3	7
P, Tmax, Tmin, PRMSL, SPFH, UGRD, VGRD	**5 2**	**2 4**	**2 4**	**3 3**	**1 6**	**4**	**2**
P,Tmax,Tmin,PRMSL,UGRD,VGRD	6 4	1 7	7 5	2 1	4 2	5	6
P, Tmax, Tmin, SPFH	3 7	4 1	5 3	6 2	5 3	7	4
P, Tmax, Tmin, SPFH, UGRD, VGRD	2 3	6 3	1 7	5 6	3 5	2	5
P, Tmax, Tmin, UGRD, VGRD	1 5	3 2	6 6	4 4	2 7	1	3

* P: Precipitation, Tmax: Maximum temperature, Tmin: Minimum temperature, PRMSL: Mean sea level pressure, SPFH: Specific humidity, UGRD: Eastward wind component, VGRD: Northward wind component

Next, the monthly information from each of the AOGCM emission scenarios (Table 3) is collected for four time slices: 1961-1990, 2011-2040, 2041-2070 and 2071-2100. Because of the limited quality and unavailability of daily inputs from many AOGCMs, monthly inputs should be used. Climate variables taken from the nearest grid points are interpolated to provide a dataset for each of the stations of interest in the same way as the NARRs. In order to generate future climate data, the difference between the base climate and the AOGCM outputs (2041-2070 or 2050s) are computed for all predictors. The change factors are then used to modify the historic dataset collected for each station, thereby creating a future dataset. The differences between current and future climate are used to calculate the monthly change factor and then added to the predictors to generate a modified time series. This modified dataset is used as input into the weather generator to produce synthetic datasets of any length for the time period of interest.

In order to reduce multi-dimensionality and collinearity associated with the large number of input variables, a principal component analysis is integrated with the weather generator. The process requires the selection of the appropriate principal components (PCs) that will adequately represent most information in the original dataset. It is found that the first PC is able to explain over 95% of the variations associated with the inputs. Hence, only the first PC is considered for the weather generator.

The daily future data, downscaled using WG-PCA, are averaged to a monthly value in order to draw a PDF for comparison with the BA-REA approach. The average monthly total values for winter (DJF) and summer (JJA) for each scenario are considered. Values from each AOGCM for any specific year are considered as an independent set of realization and are used to draw PDFs.

3.4 Indexing Extreme Precipitation Events

Simulation of extreme precipitation is dependent on resolution, parameterization and the selected thresholds. Sun et al. (2006) found that most AOGCM models tend to produce light precipitation (<10mm day^{-1}) more often than observed, too few heavy precipitation events and much less precipitation during heavy events (>10 mm day^{-1}) (Randall et al., 2007). The situation gets worse in the absence of any extreme precipitation indices. In the IPCC (2007), several indices explaining extreme temperature and precipitation are proposed but most literature reports investigations of percent change in the occurrences of such indices without any acceptable definition of their severity level.

Three precipitation indices have been used for comparing the performance of the AOGCMs in generating extreme precipitation amounts. These indices describe precipitation frequency, intensity and extremes. The highest 5 day precipitation, number of very wet days and the number of heavy precipitation days express extreme features of precipitation. For very wet days, the 95th percentile reference value has been obtained from all non-zero total precipitation events for the base climate. Heavy precipitation days are those days that experience more than 10 mm of precipitation.

For Canada, due to large variation of precipitation intensities in various regions, a fixed threshold may not be good to assess the severity level (Vincent and Mekis, 2006). Accordingly, in this study an attempt has been made to classify the severity level of these indices based on percentile values. The percentile method has several advantages. It is simple and computationally inexpensive. It is completely data driven and does not follow any specific distribution, so can be used at any location with different precipitation

patterns. Table 5 presents the classification scheme used for the summer and winter season. They can be easily used to assess the impact of climate change on extreme precipitation events.

Table 5: Classification of Extreme Precipitation Indices based on Percentile Approach

Serial	Description
1	<= 25th percentile of 1961-1990 observed precipitation
2	25th – 50th percentile of 1961-1990 observed precipitation
3	50th –75th percentile of 1961-1990 observed precipitation
4	75th – 95th percentile of 1961-1990 observed precipitation
5	>95th percentile of 1961-1990 observed precipitation

3.5 Extended Kernel Estimators

Nonparametric estimators are erroneously considered to be less accurate with small sample sizes (Lall et al., 1993). With the increase in sample size, the choice of estimator selection (parametric or nonparametric) can only be more accurately identified. Nonparamtric kernel estimators based on (i) normal kernel estimator (Silverman, 1986), and (ii) the Orthonormal method (Efromovich, 1999) have been applied by Ghosh and Mujumder (2007) for assessing AOGCM and scenario uncertainties of future droughts. In the present study, the application of a normal kernel estimator is extended with the commonly used bandwidth selection methods for estimating densities and addressing model choice and scenario choice uncertainties.

3.5.1 Definition

The nonparametric kernel density estimation described in section 3.3.2 is based on the conventional method of assuming a normal distribution function for unknown PDFs. Because of an uncertain future climate, it is not justifiable to assume a normal distribution of the PDFs. Allowing an extension for the kernel estimator by replacing the normal bandwidth for a data-driven procedure can better quantify the inherent uncertainties arising from different AOGCMs.

The behavior of the estimator (equation 3.28) may be analyzed mathematically under the assumption that the data sets represent independent realizations from a probability density $f(x)$. The basic methodology of the theoretical treatment aims to discuss the closeness of estimator $\hat{f}$ to the true density, f. Successful application of the estimator depends mostly on the choice of a kernel and a smoothing parameter or bandwidth. the relevant literature shows that the choice of bandwidth is more critical. A change in kernel bandwidth can dramatically change the shape of the kernel estimate (Efromovich, 1999). For each x, $\hat{f}(x)$ can be thought as a random variable because of its dependence on $X_1, X_2, \ldots \ldots X_n$. Except otherwise stated, $\sum$ will refer to a sum for $i = 1 \; to \; n$ and $\int$ to an integral over the range $(-\infty, \infty)$.

The discrepancy of the density estimator $\hat{f}$ from its true density f can be measured by mean square error (MSE):

$$MSE_x(\hat{f}) = E[(\hat{f}(x) - f(x)]^2 \tag{3.32}$$

By standard elementary properties of mean and variance,

$$MSE_x(\hat{f}) = \{E[(\hat{f}(x) - f(x)]^2\} + var \; \hat{f}(x) \tag{3.33}$$

The sum of the squared bias and the variance at x. In many applications a trade-off is applied between the bias and the variance in equation 3.32; the bias can be reduced by increasing the variance and vice versa by adjusting the degree of smoothing. It can be obtained by minimizing the mean integrated squared error (MISE), a widely used measure of global accuracy of $\hat{f}$ as an estimator of f (Rosenblatt, 1956; Adamowski, 1985; Scott et al., 1981, Jones et al., 1996) and defined as:

$$MISE\left(\hat{f}\right) = E \int [(\hat{f}(x) - f(x)]^2 dx \qquad (3.34)$$

Or in alternative forms,

$$MISE(\hat{f}) = \int MSE_x(\hat{f}) dx$$

$$= E \int [(\hat{f}(x) - f(x)]^2 dx + \int var\,(\hat{f}) dx \qquad (3.35)$$

which gives the *MISE* as the sum of the integrated square bias and the integrated variance.

Asymptotic analysis provides a simple way of quantifying how the bandwidth h works as a smoothing parameter. Under standard assumptions, MISE is approximated by the asymptotic mean integrated squared error (AIMSE) (Jones et al., 1996):

$$AMISE(h) = n^{-1}h^{-1}R(K) + h^4 R(f'')\left(\int x^2\,K/_2\right)^2 \qquad (3.36)$$

Where $R(\varphi) = \int \varphi^2(x) dx$ and $\int x^2 K = \int x^2 K(x) dx$, n is sample size, h is bandwidth. The first term (integrated variance) is large when h is too small, and the second term (integrated squared bias) is large when h is too large.

The minimizer of $AIMSE(h)$ is easily calculated as:

$$AMISE(h) = \left[\frac{R(k)}{nR(f")(\int x^2 K)^2}\right]^{1/5} \tag{3.37}$$

3.5.2 Methods for Bandwidth Selection

Data driven estimation methods are broadly classified as first generation and second generation methods by Jones et al (1996).

First Generation Methods

First generation methods used for the selection of smoothing parameter include those proposed before 1990. These include the rule of thumb, least square cross validation and biased cross validation methods.

The most basic method is the 'rule of thumb' used by Silverman (1986). The idea involves replacing the unknown part of h_{AMISE}, $R(f")$, in equation 3.34 with an estimated value based on a parametric family such as a normal distribution $N(0, \sigma^2)$. However, this method is known to provide an over-smoothed function (Terrell and Scott, 1985; Terrell, 1990) and has been proven to be unrealistic in many applications. In the present study, h_{ROT} is used to denote the bandwidth based on the standard deviation in Silverman (1986).

The idea of 'least squared cross validation', first used by Bowman (1984) and Rudemo (1982), incorporates integrated squared error (ISE) as

$$ISE(h) = \int (\widehat{f}_h - f)^2 = \int \widehat{f}_h^2 - 2\int \widehat{f}_h f + \int f^2 \tag{3.38}$$

The minimizer of the ISE is the same as the minimizer of the first two terms of the final form. The first term is known while the second term can be estimated by $-2n^{-1}\sum_{i=1}^{n}\hat{f}_h(X_i)$, where $\hat{f}_i$ is the leave-out kernel density estimator with X_i removed. The largest minimizer is denoted by h_{CV} Hall and Marron (1991).

The biased cross validation (BLCV) proposed by Scott and Terrell (1987) seeks to directly minimize the AMISE by estimating the unknown $R(f'')$ in equation 3.34. It proceeds by selecting another bandwidth treated as the dummy variable of minimization. The smallest local minimizer of

$$BLCV(h) = n^{-1}h^{-1}R(K) + h^4 \times \left[R\left(\hat{f}_a{}'' - \frac{R(K'')}{mh} \right) \right]\left(\int x^2 K/2 \right)^2 \tag{3.39}$$

is denoted by h_{BCV}.

Second Generation Method

Second generation methods comply with those developed after 1990, such as the solve-the-equation-plug-in approach, the smoothed bootstrap approach, etc. In this study, only the solve-the-equation-plug-in approach is used, and hence is described below.

The main thought behind the 'solve the equation plug in' approach is to plug an estimate of the unknown $R(f'')$ in the equation 3.40. The major challenge is to estimate a pilot bandwidth. The 'solve the equation' approach proposed by Hall (1980), Sheather (1983, 1986) and later refined by Sheather and Jones (1991) is used in this study. The smallest bandwidth, $h_{SJPI,}$ is considered as the solution of the fixed point equation

$$h = \left[\frac{R(K)}{nR(\hat{f}_{g(h)}'')(\int x^2 K)^2} \right]^{\frac{1}{5}} \tag{3.40}$$

The major difference between the *BLCV* and *SJPI* approaches lies in the expression of the form $g(h)$, which provides a better representation of $R(f'')$. It is done by estimating an analogue of h_{AMISE} for estimating $R(f'')$ by $R(\hat{f}_g'')$.

The minimizer of the asymptotic mean squared error (AMSE) is expressed as:

$$g_{AMSE} = C_1\{R(f''')\}C_2(K)n^{\frac{-1}{7}}$$
(3.41)

for suitable functional C_1 and C_2. The expression of g in terms of h comes from solving the representation of h_{AIMSE} for n and substituting to get

$$g(h) = C_3\{R(f''), R(f''')\}C_4(K)h^{\frac{5}{7}}$$
(3.42)

For appropriate functionals C_3, C_4. The unknowns $R(f'')$ and $R(f''')$ are estimated by $R(\hat{f}'')$ and $R(\hat{f}''')$, with bandwidths chosen by reference to a parametric family, as for h_{ROT}.

While many variations have been tested for the treatment of $R(\hat{f}'')$ and $R(\hat{f}''')$, the major contribution has been to try to reduce the influence of the normal parametric family even further by using pilot kernel estimates instead of normal interference (Jones et al., 1996). Park and Marron (1992) has shown the improvements in terms of the asymptotic rate of convergence up to a certain point.

4. Results and Discussion

The performances of all methods and comparison results described in Chapter 3 are presented here. First, the BA-REA method and non-parametric weather generator are evaluated for assessing AOGCM uncertainties. The indices for estimating the severity of extreme precipitation events are developed and compared for future climate. Finally, the probabilities of extreme precipitation events are assessed with associated AOGCM and scenario uncertainties.

4.1 Fixed Weight (BA-REA) Method

The performance of the Bayesian reliability method can be assessed by model bias and convergence. Table 6 presents the values of the bias from six different AOGCMs. Bias is calculated as the difference between each AOGCM's response to the present climate and the present climate as generated by the model.

Table 6: Biases from AOGCM Responses to Present Climate (1961-1990) in London

Season	Model Bias (%)					
	CGCM3 T47	CGCM3 T63	CSIRO MK3.5	GISS AOM	MIROC 3.2HIRES	MIROC 3.2MEDRES
Summer	22.50	-2.12	6.50	12.07	-14.92	-14.10
Winter	2.18	-1.68	11.46	-0.04	-26.24	-5.64

Figure 3 presents posterior distributions of precipitation change ΔP for London during the winter and summer seasons. For purposes of reference, the response of 15 models and the scenarios' individual responses $Y_i - X_i$, for *i=1, 2, ...,15*, are plotted

Figure 3: Posterior Distributions of **DP= ν – μ** in London for Winter and Summer

along the x axis (dots) together with the REA estimate of mean change (triangles). A measure of convergence can be assessed using the relative position of the individual responses. The relative position is used in the identification of the outlier models and the models that reinforce each other. The comparison of densities in Figure 3 and the bias measure in Table 7 identify the models that provide higher biases (Table 7) and act as outliers (Figure 3). Models with smaller biases receive larger weights. The cases that respect both criteria are the ones where the probability density is concentrated.

Table 7: Relative Weighting of the 15 AOGCM Scenarios (2050s) for London

Models/Scenarios	DJF	JJA
CGCMT47_A1B	2.22	4.07
CGCMT47_A2	1.11	1.09
CGCMT47_B1	7.76	2.80
CGCMT63_A1B	4.30	31.83
CGCMT63_A2	11.06	36.56
CGCMT63_B1	1.32	0.41
CSIROMK35_B1	2.46	1.10
CSIROMK35_A2	3.37	2.77
GISSAOM_A1B	18.21	2.66
GISSAOM_B1	24.25	4.10
MIROC32HIRES_A1B	0.07	4.28
MIROC32HIRES_B1	0.09	4.51
MIROC32MEDRES_A1B	8.75	1.26
MIROC32MEDRES_B1	8.44	0.69
MIROC32MEDRES_A2	6.57	1.86

Figure 4 summarizes the posterior distributions for the precision parameters λ_j. It is considered as a random variable. The scoring of the AOGCM scenarios should be evaluated through the relative position of the boxplots, rather than by comparing point estimates. Comparison of their distributions across the models for a single region and any specific season provides the ordered performances of those scenarios in simulating future climate. Large λ_j values indicate that the distributions of the AOGCM responses are more concentrated to the true climate response, i.e. the posterior distributions which are shifted towards right indicate AOGCM's better performances than those shifted to the left. However, large overlaps among these distributions are evident indicating substantial uncertainty in the relative weighting of the models.
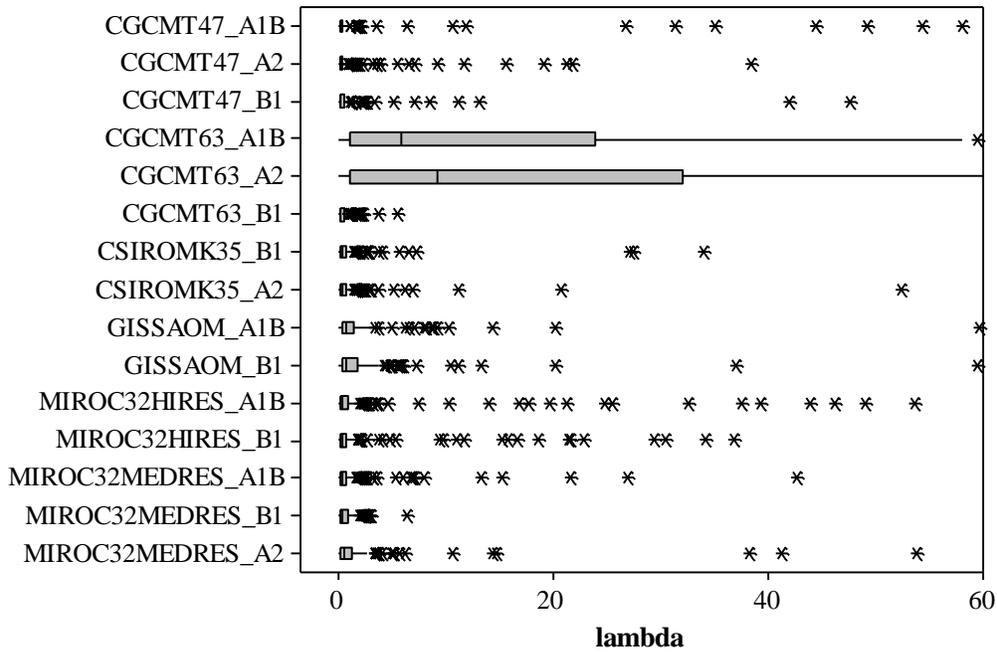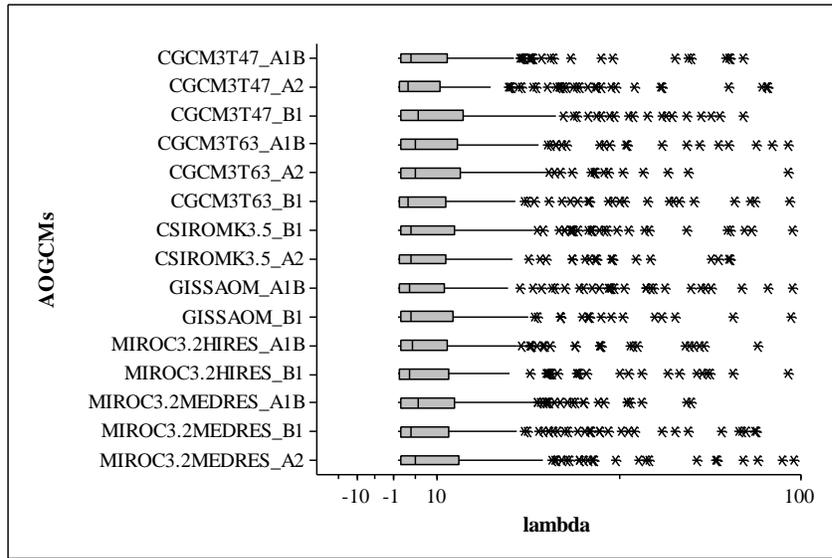
Figure 4: Posterior Distribution of λj , the Precision Parameter for Winter (Top) and Summer (Bottom)

So the posterior mean of each λ_j is calculated and the results are presented as percentages in Tables 6 and 7. The tables clearly indicate the varying result of the model

performances for different seasons, thereby suggesting a differential skill in reproducing present day climate and a different level of agreement among the models for different signals of precipitation change. Table 7 presents an overall measure of reliability for the AOGCMs by summing up the weights from each model through relative weighting. The results are ranked based on performances for summer (JJA) and winter (DJF) seasons separately. A difference in the relative weighting of the AOGCMs and scenarios can be seen.

Next, the posterior distribution of the inflation/deflation parameter θ is presented in Figure 5 to compare the simulations of the present day to future climate scenarios. A value below one represents a deterioration of the degree of the precision of the model performances.
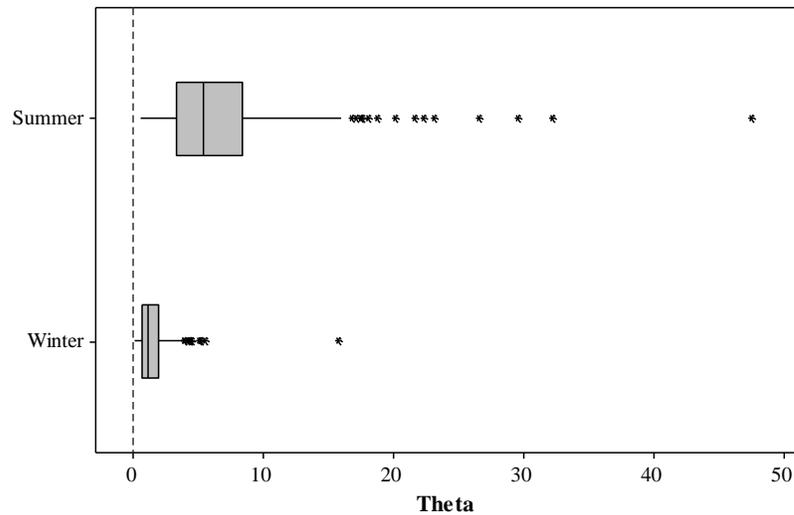
Figure 5: Posterior Distribution of θ, the Inflation/Deflation Parameter

From Figure 5, it is seen that for summer and winter, the models and scenarios show improved performances, however with varying degree; the agreements are better represented during summer than winter. The figure presents an overall degree of

performance for the REA method by considering a common value for all AOGCMs, which can limit the real representation of future climate.

4.2 Variable Weight (Kernel Estimator) Method

The variable weight method involves downscaling the AOGCM responses for future climate scenarios and estimating the uncertainties using nonparametric density estimator by considering different weights at each time interval.

This study uses 22 stations for the period of 1979-2005 (N=27) to simulate precipitation scenarios using seven meteorological variables. Employing the temporal window of 14 days (w=14) and 27 years of historic data (N=27), 404 days are considered as potential neighbors *(L=(w+1) x N-1=404)* for each variable. 12 different runs, each comprising 27 years of daily precipitation are generated. Errors in the estimates of mean and variance of generated precipitation are evaluated using a statistical hypothesis test at 95% confidence level.

The performance of WG in representing the present climate is tested by using the nonparametric Wilcoxon-rank test and Levene's test (Levene, 1980). Table 8 presents the statistical significance test results (*p* values) in the estimate of daily precipitation for summer (JJA) and winter (DJF) for 1979-2005 in London. The *p* values at 95% confidence level for all runs are above the threshold (*0.05*), which clearly indicates that there is no evidence of different means between the observed and generated precipitations. The results of the Levene's test for the equality of variances of observed and simulated precipitation at 95% confidence level are presented in Table 8. The *p* values appear above 0.05 thresholds, indicating equal variability of the simulated

precipitation with the observed precipitation. So, the observed and the simulated precipitation can be assumed to have equal variances.

Table 8: Test Results (*p* values) of the Wilcoxon Rank Test and Levene's Test

Runs	Wilcoxon Rank Test		Levene's Test	
	Summer	Winter	Summer	Winter
1	0.46	0.48	0.61	0.55
2	0.76	0.61	0.72	0.58
3	0.64	0.67	0.56	0.99
4	0.93	0.37	0.98	0.18
5	0.60	0.98	0.87	0.59
6	0.59	0.53	0.96	0.99
7	0.91	0.95	0.64	0.20
8	0.91	0.95	0.64	0.20
9	0.76	0.67	0.98	0.84
10	0.48	0.63	0.91	0.19
11	0.77	0.80	0.41	0.66
12	0.76	0.29	0.76	0.30

Frequency distributions of wet-spell lengths for winter and summer months are plotted in Figure 6. A comparison of observed and simulated values for wet-spell lengths shows very close agreement between the frequency distributions. The frequency of wet-spell lengths in the simulated data for summer is almost identical to the observed values, except for the one day lengths where the simulated data show a slight overestimation. The same is the case for the winter months. The performance of the weather generator in reproducing wet-spell lengths is very good.

Using the synthetic data set created from the change factors from several AOGCMs, 324 years of data set is generated for each case. In order to investigate the intensity of wet
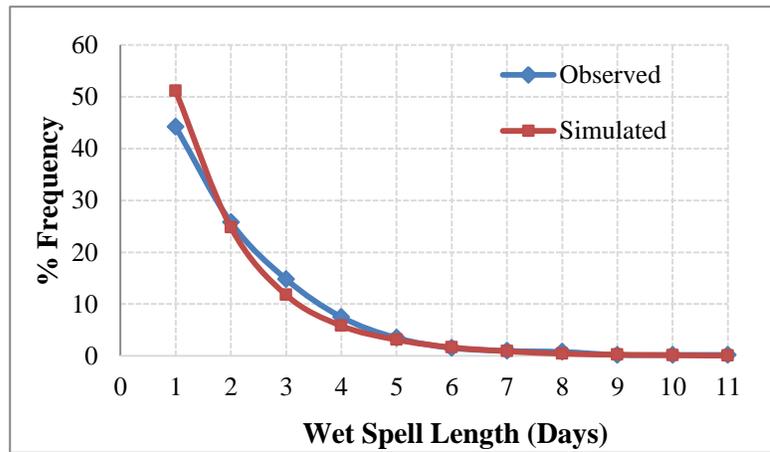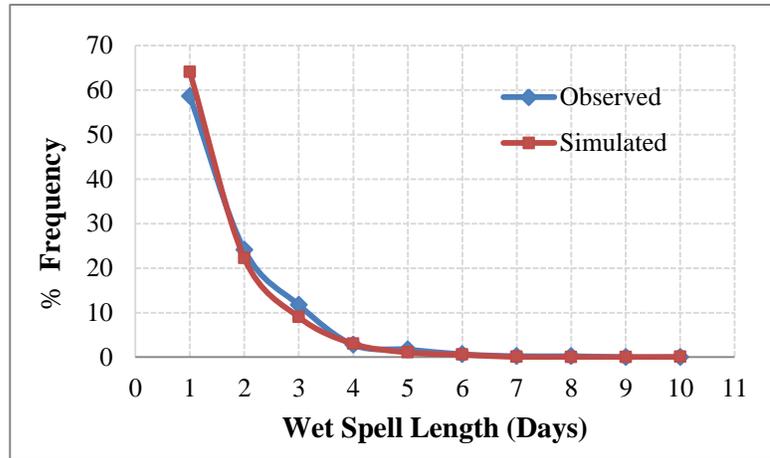
Figure 6: Frequency Plots of Wet Spell Lengths for Summer (Top) and Winter (Bottom)

spells for future climate, bar charts are made showing the percent change in wet spell intensity from the historical values to the future values. Intensities are calculated using the total amount of rain that fell during the spell over the length of the spell. The percent changes in wet spell intensities are determined for 3, 5 and 7 day wet spells. The plots are made for summer (June, July, August) and winter (December, January February) in both time periods. Figures 7 (a), (b) and (c) show the bar charts for the summer and winter

months of the 2050s, respectively.
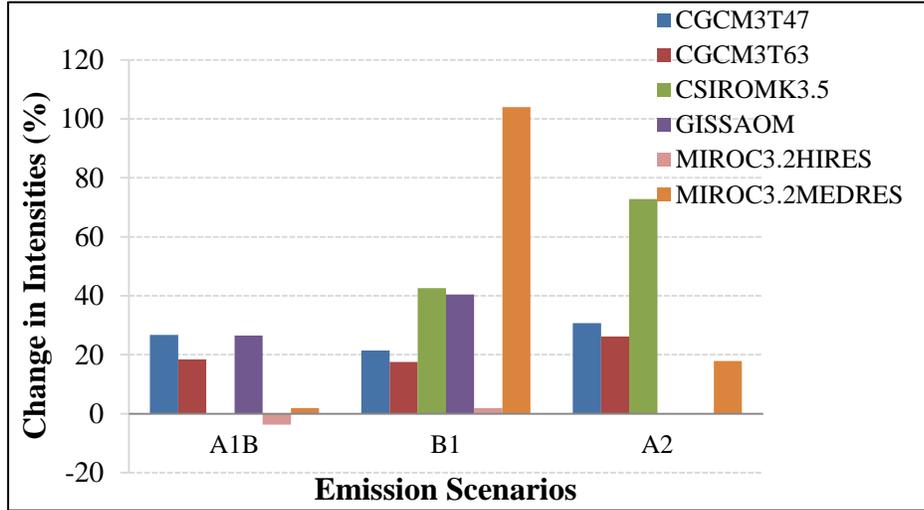
Figure 7 (a): Change in 3-Day-Spell Intensities for Summer, 2041-2070
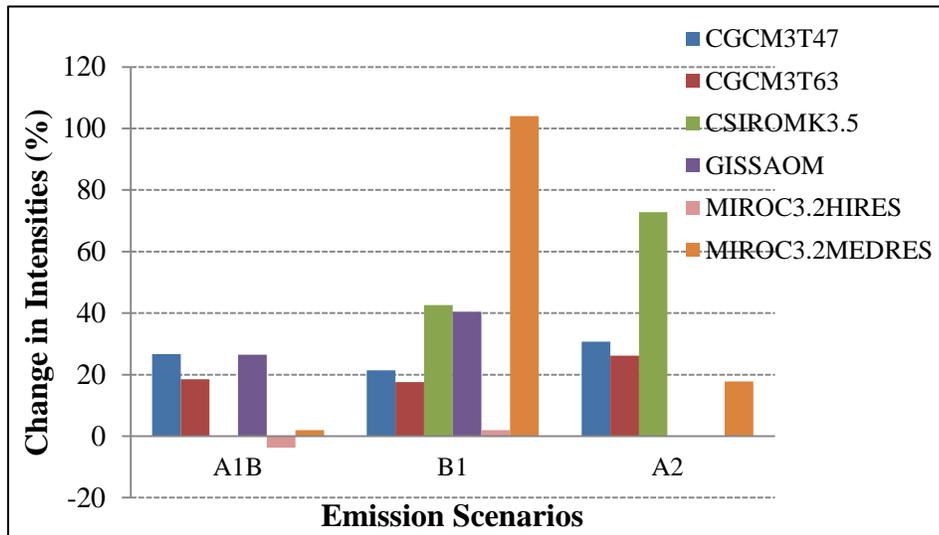
Figure 7 (b): Change in 5-Day-Spell Intensities for Summer, 2041-2070

For summer wet spells, all models, except the MIROC3.2HIRES A1B, project an increase in 3-day intensities. The most significant increase in intensity is predicted by MIROC3MEDRES A2 (100%) and CSIROMK3.5 A2 (47%). For 5-day wet spells, all models predict an increase, with CSIROMK3.5 A2 and MIROC3MEDRES B1 predicting the highest intensities over 100%. The smallest increase is predicted by

MIROC3.2MEDRES A1B and MIROC3HIRES A1B with below 20% of changes. The average change from all the models and scenarios is approximately between 35-70%.
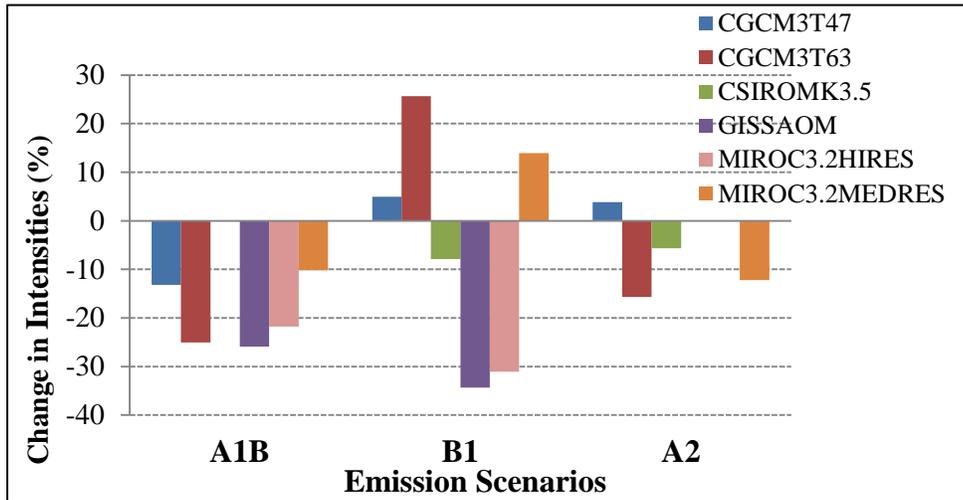
Figure 7 (c): Change in 7-Day-Spell Intensities for Summer, 2041-2070

Except for CGCM3T63 B1, CGCM3T47 B1 and A2, and MIROC3MEDRES B1, most models predict a decrease in intensity for 7-day spells. Increases of 6-25% are predicted by these models. The remaining models predict a decrease in intensity of 7 to 38% for the 2050s, with the highest being generated by GISSAOM B1. Overall, the general trend for summer in the future as predicted by several AOGCM's is that shorter wet-spell intensities will increase as longer wet-spell intensities decrease.

In the next section, a comparison between both uncertainty estimation methods is presented. The mean precipitation obtained from each AOGCM and scenario is assumed to be an independent realization of future. Using this concept, climate density curves are generated by combining the information from all AOGCMs during the 2050s, the results

of which are presented in section 4.3.

4.3 Fixed vs. Variable Weight Method

This section presents a comparison of uncertainty estimation methods explained in sections 3.3.1 and 3.3.2 using density estimators. Figures 8 (a) and (b) present density estimates of precipitation change for the winter and summer seasons with the results obtained from the WG combined kernel density estimates and the BA-REA method for London station using 2050s (2041-2070) time slice.
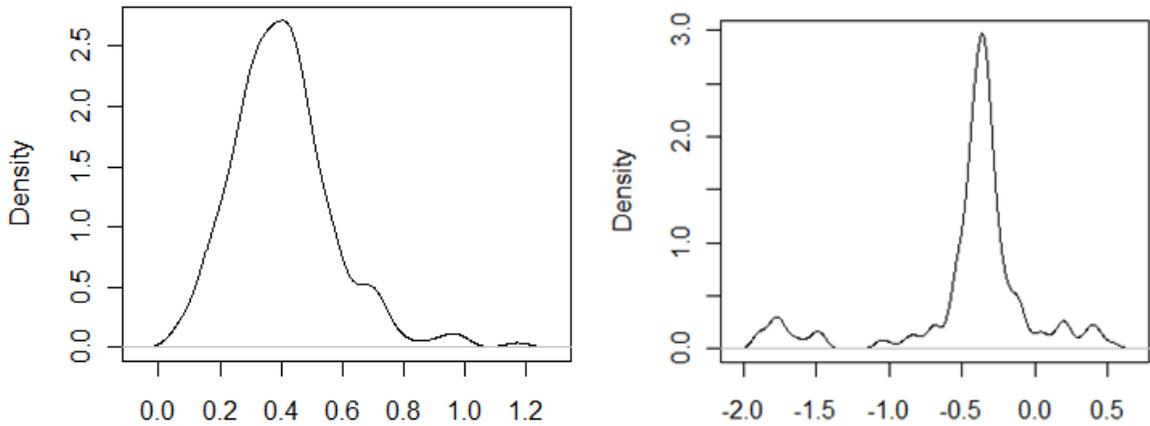
Figure 8 (a): Density Estimate of the Mean Precipitation Change in London using BA-REA Method for Winter and Summer

The density estimate of the posterior distribution of the precipitation change during summer using BA-REA method is under-smoothed, many spurious bumps especially at the tails for both winter and summer can be seen which makes it harder to understand the structure of the data. The estimates calculated by the kernel estimator show evidence of a smoothed structure.

The extended benefit of kernel estimators is that unlike BA-REA, the generated outputs can be modified into indices of interest and the probabilities can be calculated for any frequency of data, monthly, daily, or yearly, while the BA-REA method only

provides the mean change by combining the AOGCM scenarios. Moreover, the BA-REA method does not provide a single relative weight applicable to the overall data length. Instead, the weight/kernel function (*K(.)*) in equation 3.29 can be calculated at any points of interest within the range of data.
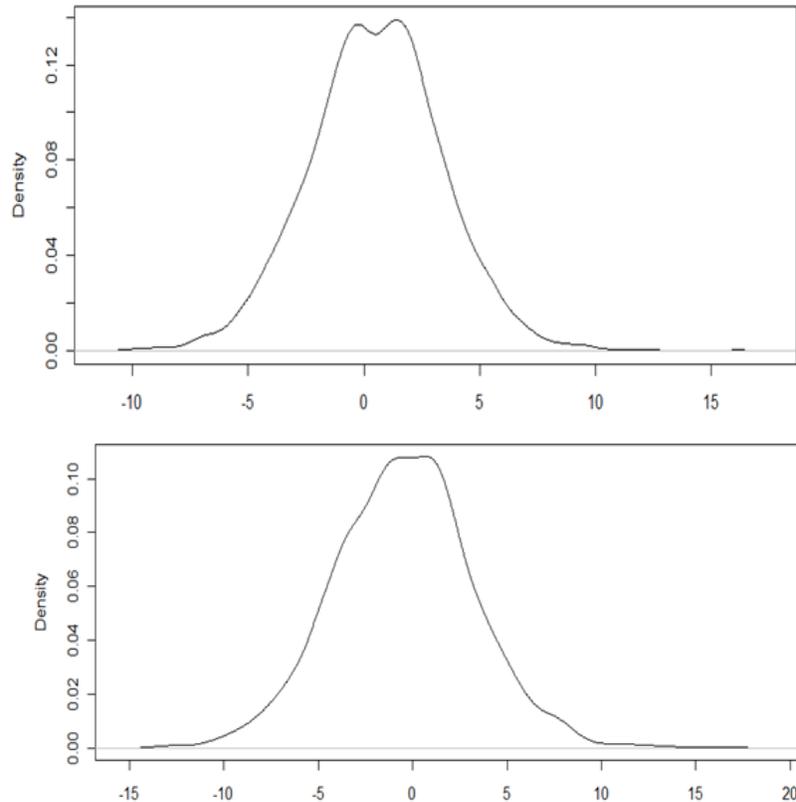
Figure 8 (b): Density Estimate of the Mean Precipitation Change using Kernel Estimator for Winter (Top) and Summer (Bottom)

4.4 Uncertainty Estimation of Extreme Precipitation Events

4.4.1 Changes in Future Extreme Precipitation Events

Changes in the precipitation indices compared to the historic observed 1979-2005 values are computed from the downscaled precipitation for three time slices (2020s, 2050s, and 2080s) and presented in Table 9. Both summer and winter show different

changing patterns. For summer, half of the scenarios show a decrease in number of heavy precipitation and very wet days for all three time slices, while most models show an increase in 5 day maximum precipitation amount.

Table 9: Percent Changes in Extreme Precipitation Events for 2020s, 2050s and 2080s

Models/Scenarios	Heavy Precip Days			Very Wet Days			5 Day Precip		
	2020	2050	2080	2020	2050	2080	2020	2050	2080
Summer									
CGCM3T47_A1B	3.89	2.86	1.37	8.19	5.96	1.87	5.64	0.75	2.49
CGCM3T47_A2	1.87	3.45	-2.51	5.34	5.07	-1.33	5.88	3.03	-0.55
CGCM3T47_B1	7.26	-2.93	-1.56	13.97	0.44	5.87	8.27	1.96	2.45
CGCM3T63_A1B	-2.38	-6.56	-1.18	6.23	-3.91	2.05	12.17	-2.54	1.16
CGCM3T63_A2	-10.78	3.30	-1.56	-11.57	9.70	-0.71	-4.73	6.70	5.25
CGCM3T63_B1	-7.51	-6.85	-7.50	-5.60	-6.85	-7.12	-2.80	2.83	-4.70
CSIROMK3.5_A2	18.44	29.73	26.84	39.68	57.92	52.05	26.98	37.51	35.18
CSIROMK3.5_B1	5.61	19.57	16.37	14.77	39.68	29.00	9.81	30.38	18.45
GISSAOM_A1B	1.03	6.38	15.91	3.56	14.59	32.38	3.64	9.59	20.15
GISSAOM_B1	5.06	5.57	8.15	11.92	16.01	22.42	8.76	9.19	16.53
MIROC3HIRES_A1B	-25.84	-24.38	-26.72	-35.32	-38.26	-39.59	-19.41	-23.08	-26.93
MIROC3HIRES_B1	-14.55	-25.70	-16.82	-18.68	-31.94	-24.82	-11.64	-19.30	-15.91
MIROC3MEDRES_A1B	-13.31	-23.24	-33.12	-16.28	-31.58	-41.28	-12.08	-20.45	-27.70
MIROC3MEDRES_A2	-13.09	-12.50	-40.01	-15.75	-16.81	-56.41	-14.01	-9.18	-38.89
MIROC3MEDRES_B1	-14.85	-20.38	-15.57	-17.53	-27.05	-20.82	-10.23	-17.58	-13.58
Winter									
CGCM3T47_A1B	26.15	38.60	47.13	40.00	59.88	76.66	19.40	27.09	29.02
CGCM3T47_A2	28.88	32.80	60.11	43.08	48.13	91.86	23.07	20.54	38.96
CGCM3T47_B1	25.31	48.85	45.16	33.38	73.36	66.94	21.49	27.87	25.75
CGCM3T63_A1B	19.57	23.31	35.05	22.77	26.50	54.55	10.54	9.52	20.76
CGCM3T63_A2	10.07	26.04	33.66	12.77	40.45	47.66	9.82	15.14	20.14
CGCM3T63_B1	20.32	7.21	19.52	16.62	5.65	29.00	11.21	1.30	10.26
CSIROMK3.5_A2	22.44	31.12	38.55	30.00	40.45	62.55	12.24	24.71	26.66
CSIROMK3.5_B1	20.04	39.51	21.30	23.54	60.51	21.17	12.65	25.41	12.75
GISSAOM_A1B	6.87	10.70	27.38	6.31	4.08	41.54	5.80	-0.94	15.45
GISSAOM_B1	17.03	11.66	18.71	19.23	16.62	23.05	12.55	5.30	6.26
MIROC3HIRES_A1B	-4.80	6.73	6.10	-9.38	7.22	11.76	-0.15	2.02	-2.13
MIROC3HIRES_B1	-4.09	-2.91	18.66	-18.92	-5.64	18.97	-7.27	-7.47	2.61
MIROC3MEDRES_A1B	-7.67	0.64	-0.41	-14.77	-11.12	-2.35	-9.68	-7.52	-1.02
MIROC3MEDRES_A2	-6.26	-1.61	5.58	-12.31	-7.67	10.35	-8.40	-5.01	-0.84
MIROC3MEDRES_B1	-9.64	-2.95	6.63	-16.92	-11.91	-0.15	-5.64	-10.02	-3.02

This clearly indicates a higher intensity of precipitation during extreme precipitation events. However, ranges of change are very high, indicating higher uncertainties in model projections during summer. For winter, most of the models are in

agreement over the increasing trend of extreme precipitation indices for three time slices. In this case also, the uncertainty range is higher.

4.4.2 Distribution Fitting

In the presence of uncertainties in AOGCM models, there is still concern over the choice of a unique distribution for the future climate responses. The comparison of the optimal distribution of different AOGCM data based on probability plots and goodness of fit test provides an insight into the level of inherent uncertainties. The performances of different distributions during summer and winter are evaluated using three goodness-of – fit-tests: Kolmogorov-Smirnov test, Anderson-Darling estimate, and Chi-Squared test.

Kolmogorov-Smirnov Test

The Kolmogorov-Smirnov test is used to decide whether the sample comes from a hypothesized continuous distribution. The samples $x_1, x_2, \ldots \ldots, x_n$ are assumed to be random, originating from some distribution with Cumulative Distribution Function (CDF) $F(x)$. The Kolmogorov-Smirnov statistic (D) is based on the largest vertical difference between the theoretical and the empirical CDF:

$$D = \max_{1 \leq i \leq n} \left(F(x_i) - \frac{i-1}{n}, \frac{i}{n} - F(x_i) \right) \tag{4.1}$$

Anderson-Darling Estimate

The Anderson-Darling procedure compares the fit of an observed CDF to an expected CDF. The method provides greater weight to the tail distribution than the Kolmogorov-Smirnov test. The Anderson-Darling statistic A^2 is expressed as:

$$A^2 = -n - \frac{1}{n} \sum_{i=1}^{n} (2i - 1) \cdot \left[lnF(X_i) + \ln\left(1 - F(X_{n-i+1})\right) \right] \qquad (4.2)$$

Chi Squared Test

The Chi –squared test is used to determine if a sample comes from a specific distribution. The test statistic is expressed as:

$$\chi^2 = \sum_{i=1}^{k} \frac{(O_i - E_i)^2}{E_i} \qquad (4.3)$$

where,

O_i is the observed frequency;

E_i is the expected frequency calculated by:

$$E_i = F(x_2) - F(x_1)$$

Where,

F is the CDF of the probability distribution being tested; and

$x_1 \ and \ x_2$ are the limits of the ith bin.

In terms of hypothesis tests, the distributional form is rejected at the chosen significance level α if the test statistic is greater than the critical value defined as: $\chi^2_{1-\alpha,k-1}$, representing the Chi-squared inverse CDF with $k - 1$ degrees of freedom and a significant level of α.

The performance of any specific distribution is ranked based on the goodness of fit values. The optimum parameters for the best fitted distribution function are summarized in Appendix C. From the tabulated results it can be observed that for extreme precipitation events, most models are fitted with the Generalized Extreme Value distribution with varying value of the shape (k), location (μ) and scale (σ) parameters.

However, the distribution of wet days with $>95^{th}$ percentile precipitation during the winter season fits a well defined Frechet distribution, indicating a distribution different than the historical perturbed/no change scenario.

The GEV distribution unites the type I, type II and type III extreme value distributions into a single family, thereby allowing a continuous range of possible shapes. For $k < 0$, the GEV is equivalent to the type III extreme value (Weibull). For $k > 0$, the GEV is equivalent to type II distribution (Frechet). As k approaches 0, the GEV becomes the type I (Gumbel). Although most of the models and scenarios show the best fit with extreme value distributions, to be more precise, with the Type II (Frechet) and Type III (Weibull) distributions with shape parameters greater and smaller than 0 respectively, the shape parameter values (k) appear close to 0. However, the differences in the k values show extent of the variations among the distributions for each index. The tables further point out the limitations of the parametric methods for quantification of uncertainties assuming any specific distribution and parameter values.

4.4.3 Comparison of Extended Kernel Estimators

Selection of bandwidth

To measure how well the bandwidth selection methods perform, this section proceeds with the comparison of various bandwidth selectors by applying them in the assessment of extreme precipitation indices. Figure 9 presents kernel density estimates with statistics constructed using several bandwidth selectors: (i) the rule of thumb (ROT; by Silverman, 1986) as explained in section 3.3.2), (ii) likelihood cross validation (LCV), which searches for bandwidth based on likelihood (by Terrell and Hall, 1990, as explained in section 3.5) and (iii) the plug in estimator that selects the bandwidth using the pilot

estimator of the derivatives refined by Sheather and Jones, 1991 (SJPI; named after Sheather-Jones plug in estimator (section 3.5)).

The choice of kernel is strictly limited to examining two of the most widely used types: Gaussian and Epanetchnikov kernels, the functions of which are expressed as:

$$\text{Gaussian:} \qquad K(u) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}u^2}$$

$$\text{Epanechnikov:} \qquad K(u) = \frac{3}{4}(1 - u^2)$$

The 'original' estimate is created by mixing the inputs, and 1000 samples are generated from the mixtures without any estimation of bandwidth. It is created for assessing how different techniques respond to the original data type. By comparing the generated estimators, it can be seen that the density estimate using ROT is highly oversmoothed, which may have missed important features of the generated data. For both kernel types, it failed to capture the multimodality. In the case of LCVs, there are suggestions of multiple modes in the density curve. However, it is still severely undersmoothed; the small bumps occurring from the uncertainties of different AOGCM types make it harder to understand the structure of real data. The bandwidth by SJPI seems to be in a better agreement with the 'original' estimate and provides a strong indication of multimodal distribution. From Figure 9, it is also evident that the choice of kernel merely plays a role in the estimation of density. So, for the present study the Gaussian kernel with Sheather-Jones plug in estimator was used to calculate the bandwidth for estimating density of the extreme precipitation indices.
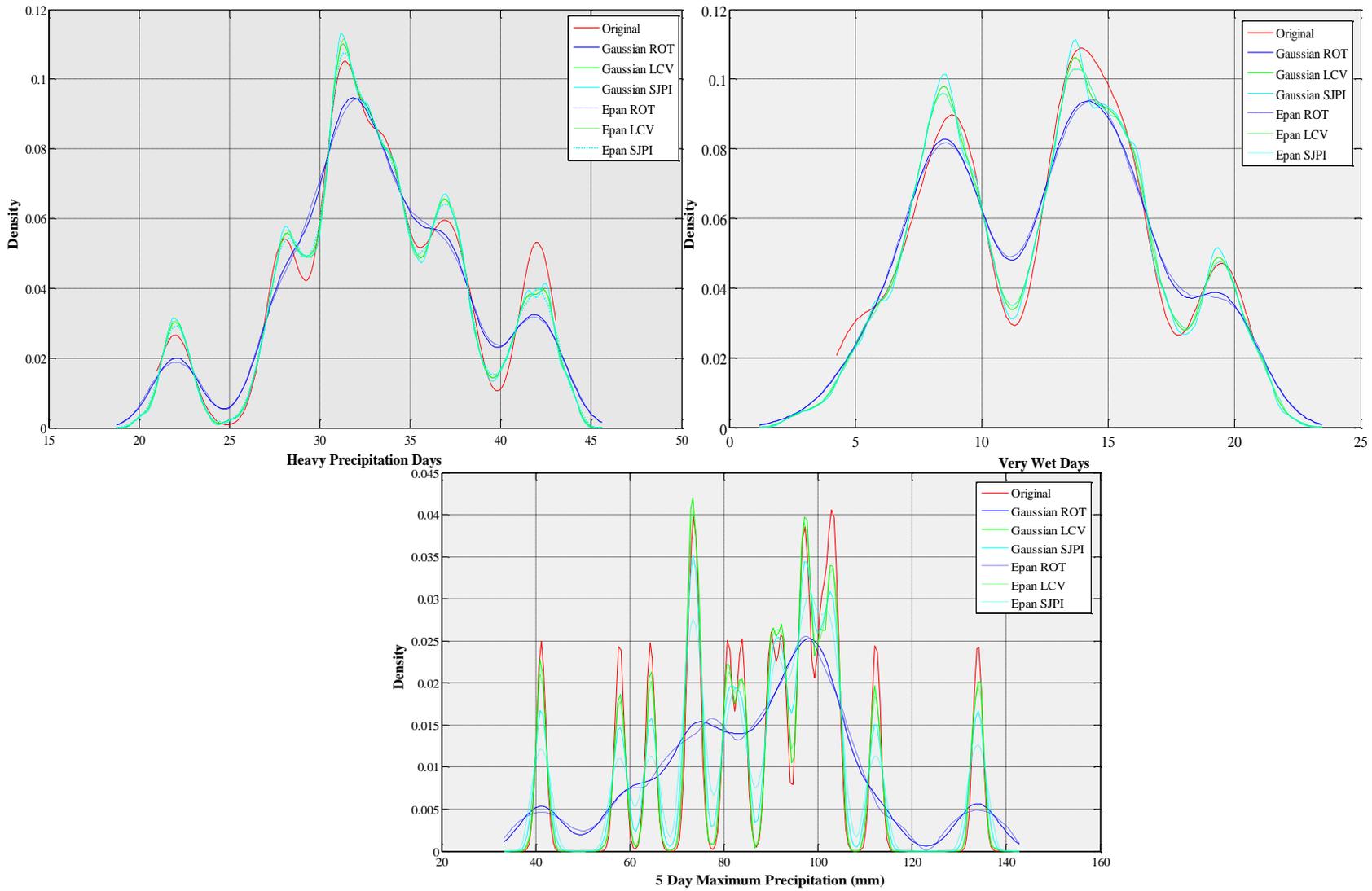
Figure 9: Comparison of Various Bandwidths of Extreme Precipitation Indices

Uncertainty estimation

To examine uncertainties in future extreme precipitation events, the yearly values of the indices from each AOGCMs and scenarios are taken as a set of independent realizations. This set is then used at each time step to establish a PDF by applying the bandwidth values. The CDF values at the upper and lower ranges of each severity class are calculated by numerical integration. The difference between the upper and lower value can thus be considered as the probability of that specific class of extreme precipitation indices for future. Figures 10 through 12 present the probability of heavy precipitation days, very wet days, and 5 day precipitation for three time slices. Both indices show somewhat similar results for the summer and winter seasons. For <25th percentile values, heavy precipitation days show an increase in probability for the later part of the century. For the 25th-50th and 50-75th percentile ranges, probabilities decrease slightly while approaching 2100. However, the higher probability of precipitation days over the time is observed for >75th and >90th percentile range. This trend is supported by the probabilities of very wet day and 5 day precipitation for the summer season. In summary, the increased probability of the high end extreme precipitation events indicates larger chance of high intensity events during the later part of the century. The method explained in this section can be seen as a major improvement over the 'normal' kernel (Silverman, 1986) method applied in other AOGCM and scenario uncertainty studies. The SJPI based kernel estimation method proposed here overcomes the limitations associated with the assumptions of normality in the case of unknown densities/distributions. It is completely data driven; hence, not only is it more robust, flexible, and independent, but and the methodology has been extensively revised by statisticians.

66
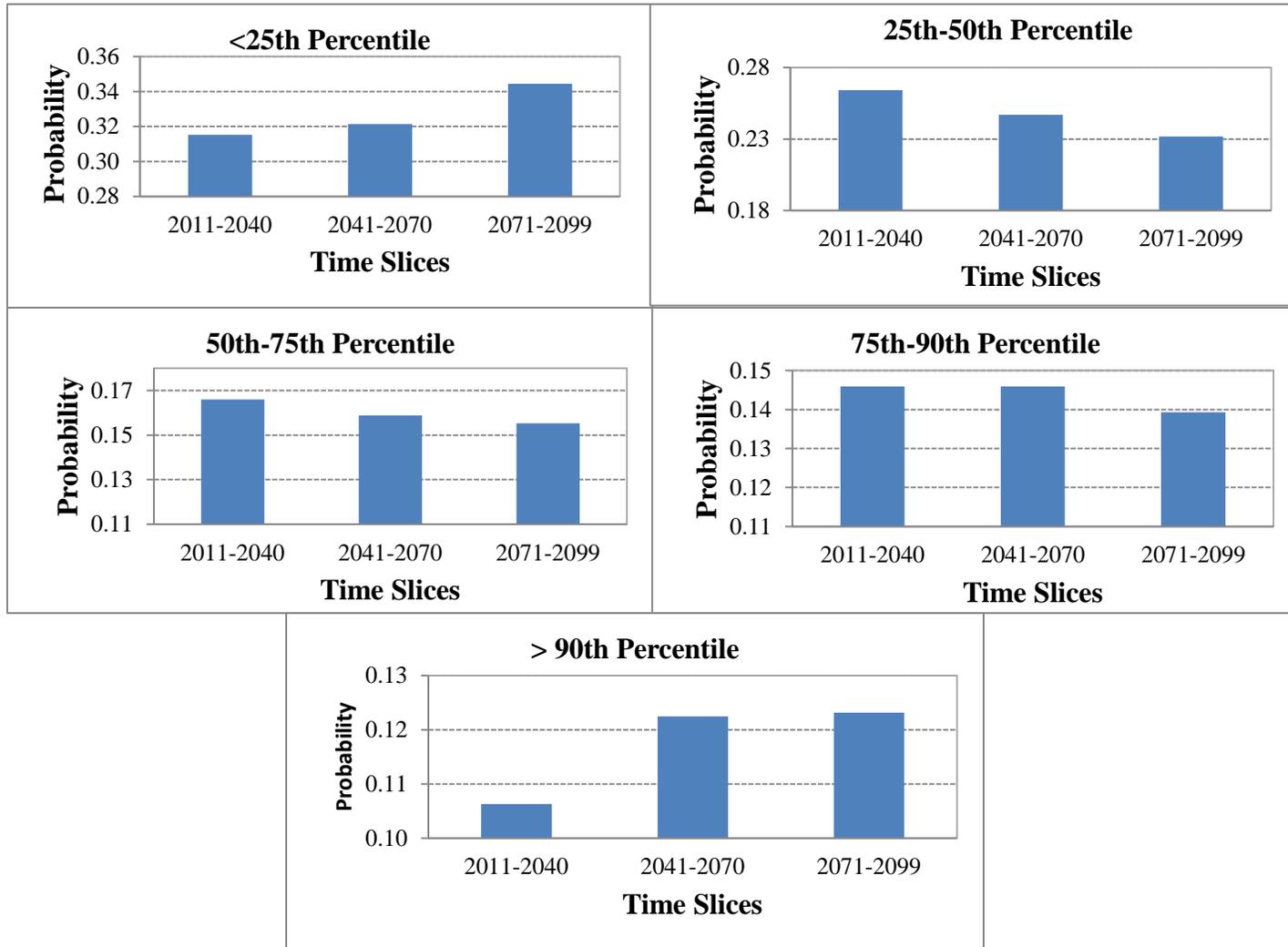
Figure 10 (a): Probability of Heavy Precipitation Days during Summer
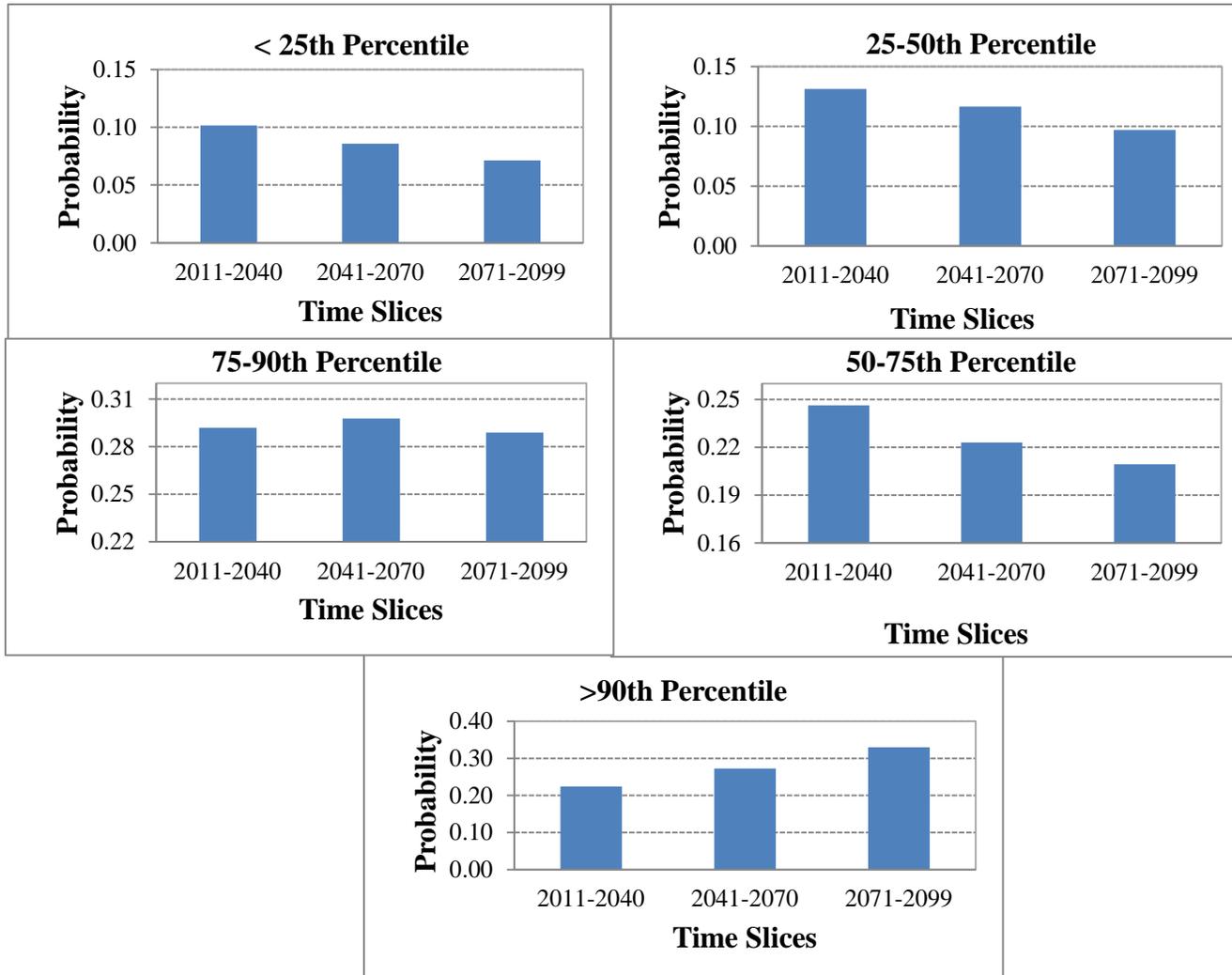
Figure 10 (b): Probability of Heavy Precipitation Days during Winter
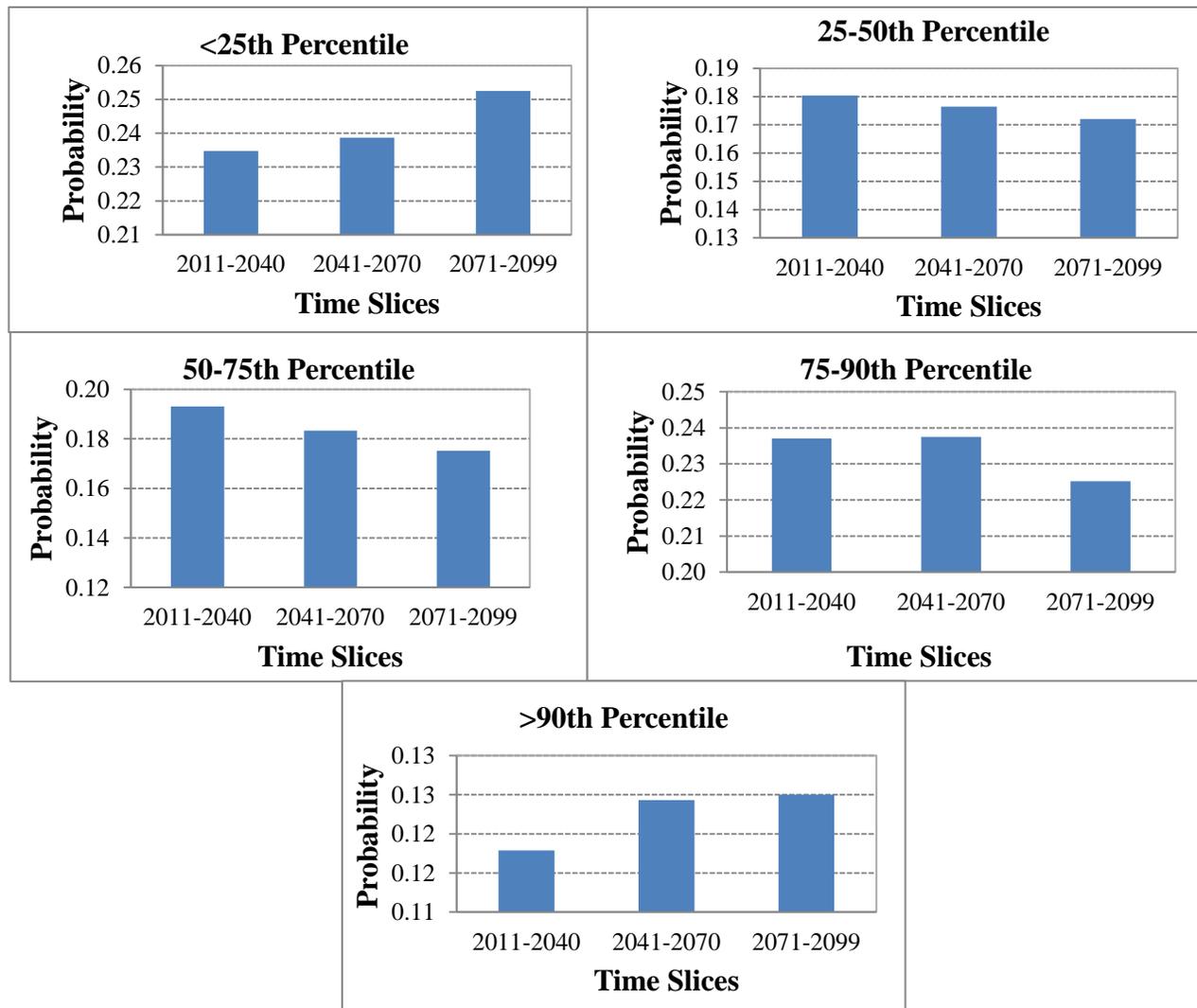
Figure 11 (a): Probability of Very Wet Days during Summer
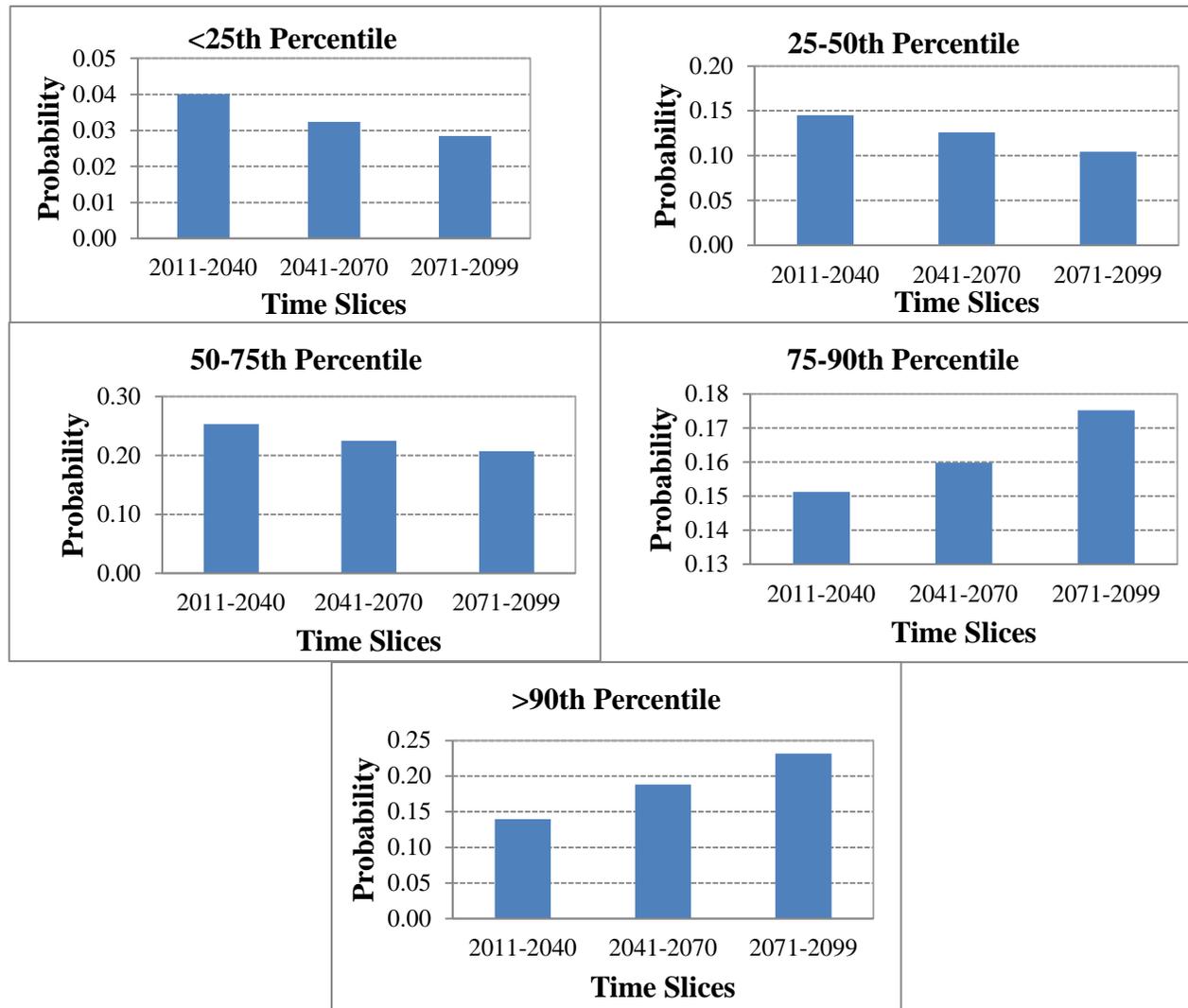
Figure 11 (b): Probability of Very Wet Days during Winter
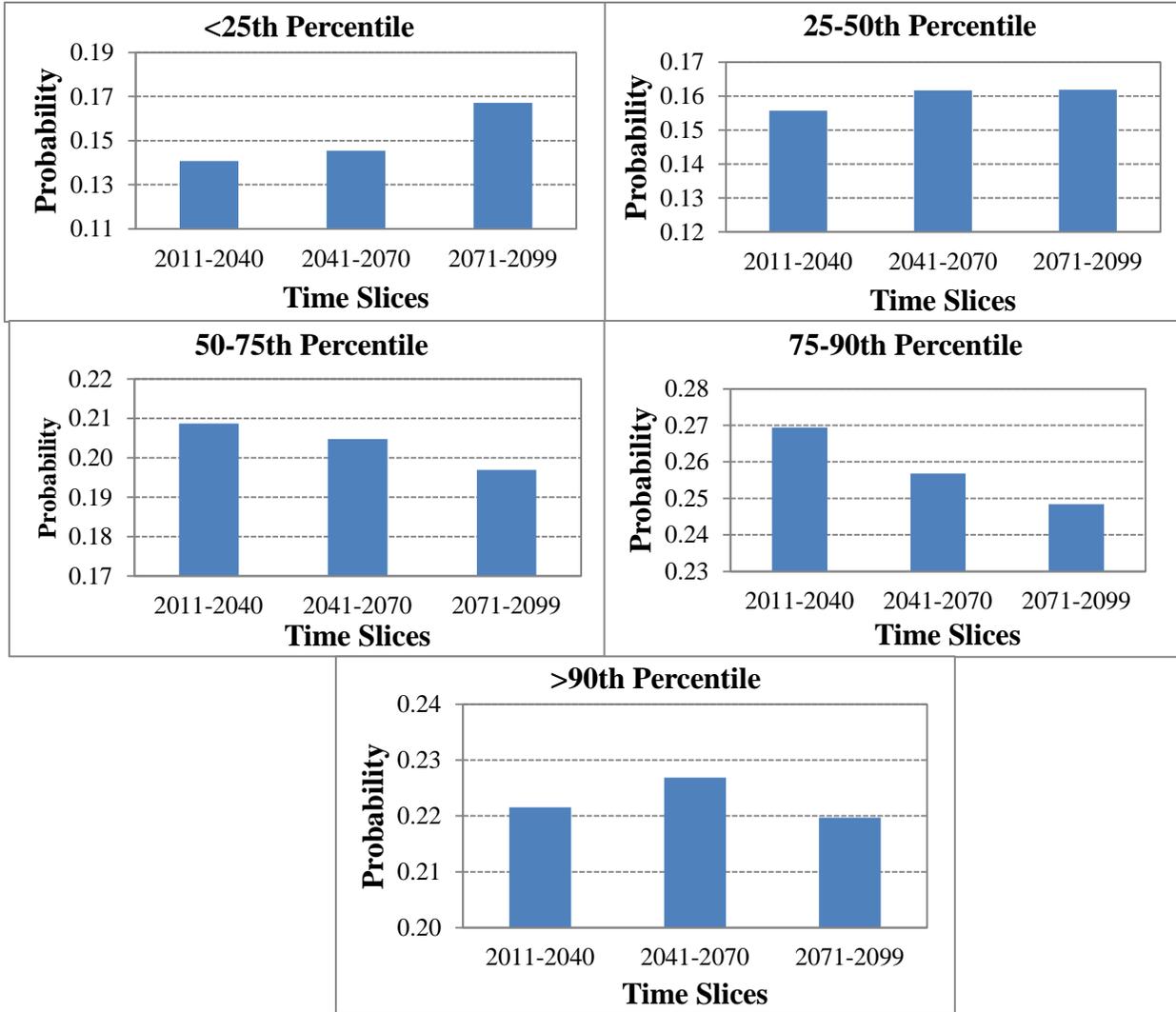
Figure 12 (a): Probability of 5 Day Precipitation during Summer
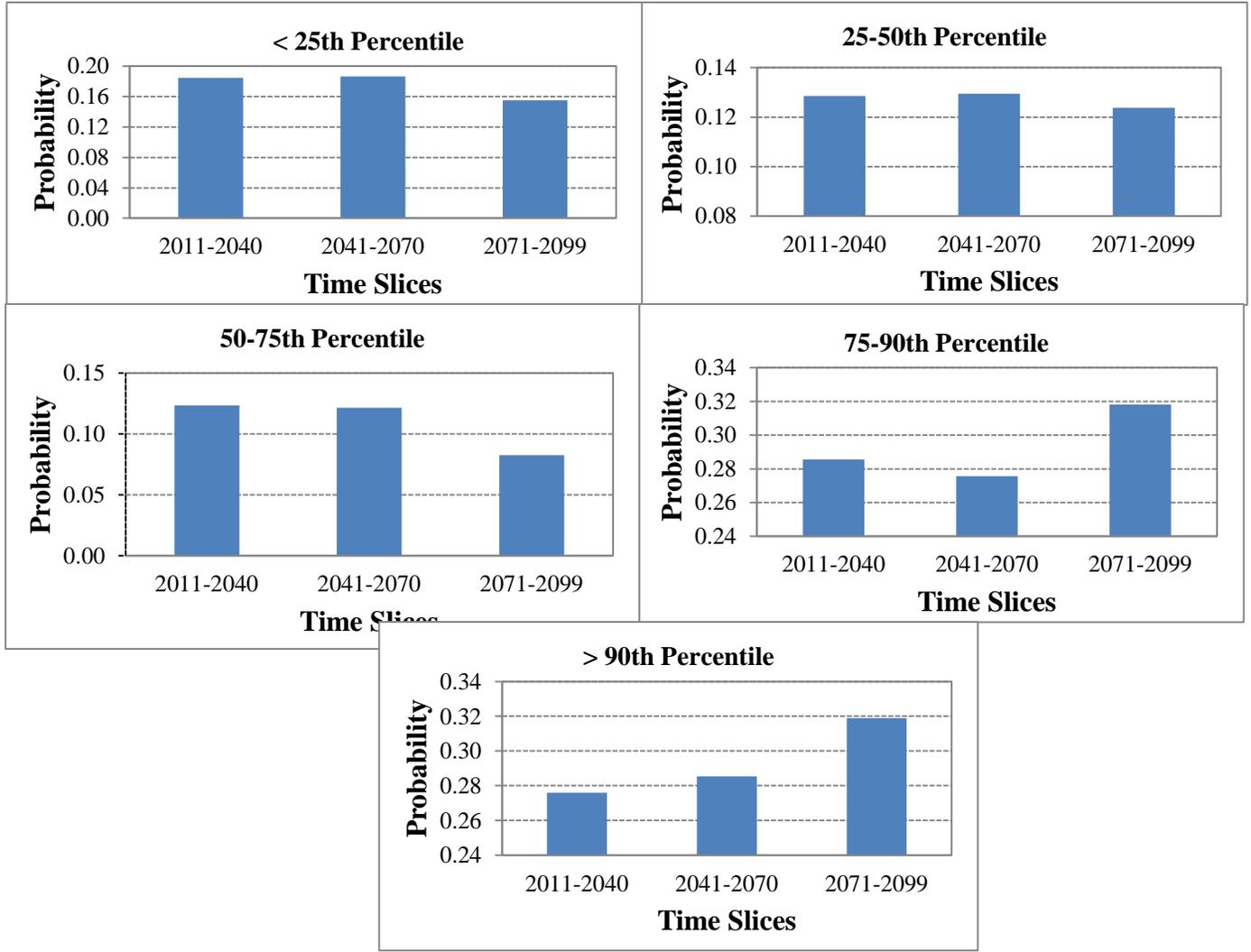
Figure 12 (b): Probability of 5 Day Precipitation during Winter

The Orthomornal method (Efromovich, 1999) proposed by Ghosh and Mujumder (2007) to estimate uncertainties of future droughts provides another important segment of the nonparametric uncertainty estimation technique. However, one major limitation of the orthonormal method is the use of a subset of the Fourier series, which consists of cosine functions without proper justification. The additional benefit of kernel density estimators for estimating AOGCM and scenario uncertainties derives from the fact that the scientific community is now highly confident that the trends in precipitation over future periods are not going to follow the same distribution as in the past. However, it is true for any statistical method that larger samples provide better estimates of any data distribution. It is our expectation that with the advance of more sophisticated global climate models, the kernel method will be applied with more confidence for uncertainty estimation problems.

5. Conclusions

This study deals with the approaches for quantifying AOGCM and scenario uncertainties from the modeled outputs of extreme precipitation events for London, Ontario, Canada. This work is strictly limited to the uncertainties of the outputs from several AOGCMs and scenarios and does not consider the uncertainties due to parameterization or structure of the models.

Two very different multi-model ensemble methods namely, the Bayesian reliability ensemble average (BA-REA) and the downscaling based kernel density estimator are used for uncertainty estimation. A comparison of these two methods reveals that while the BA-REA method can be a good alternative for predicting mean changes in precipitation in any region, it cannot be used in estimating uncertainties of different extreme events occurring at a daily time scale. The capability of the BA-REA method to analyze the climate responses is fairly limited; whereas the downscaled outputs can be obtained in any frequency according to the need of the user. The data-driven kernel estimator is capable of assuming data values at each time step as an independent realization, instead of calculating weights based on the means. It has a significant implication for estimating uncertainties of extreme precipitation events; calculating weights based on the mean can ignore the higher or lower values which may cause an unrealistic representation of climate extremes, such as floods, droughts, etc. However, the kernel estimator has it's limitations too, from the extended chance of over or under-smoothing resulting from wrong selection of bandwidth. The comparison of the best fit curves for different AOGCM scenarios for extreme precipitation indices shows varying agreement and thereby the limited benefits of parametric distribution approach.

The choice of an appropriate bandwidth selection method is a significant step for kernel estimation. The shape of the distribution function is important in determining the performance of the bandwidth. The comparative results of different bandwidth selectors show that the rule of thumb (ROT) method assuming normal kernel suffers from over-smoothing for both indices while the least square cross validation (BLCV) method results in under-smoothed distributions. The SJPI estimator offered a useful compromise between the ROT and the BLCV methods. This trade-off between the distributions of the bandwidths seems to be an intrinsic criterion for assessing the performance of data-driven bandwidth selectors. Using the bandwidths calculated by the SJPI method, the CDFs for different severity classes are calculated for the extreme precipitation indices. This is estimated by the assumptions that the outputs from different AOGCMs are independent realizations; hence, indices have a different PDF at each time step and are not limited to any specific type of distribution. The nonparametric methods can be seen as a major improvement over the parametric methods, which otherwise assume specific distributions for estimating uncertainties. Considering the probabilities obtained, it can be said that the probability of severe and extreme events are going to increase for both summer and winter due to the changes in climate over the next century.

The future scope of the study includes generating probabilistic intensity-duration-frequency (IDF) curves for future extreme precipitation events by incorporating associated uncertainties from AOGCM and scenario outputs for decision making.

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APPENDIX A: SRES Emission Scenarios
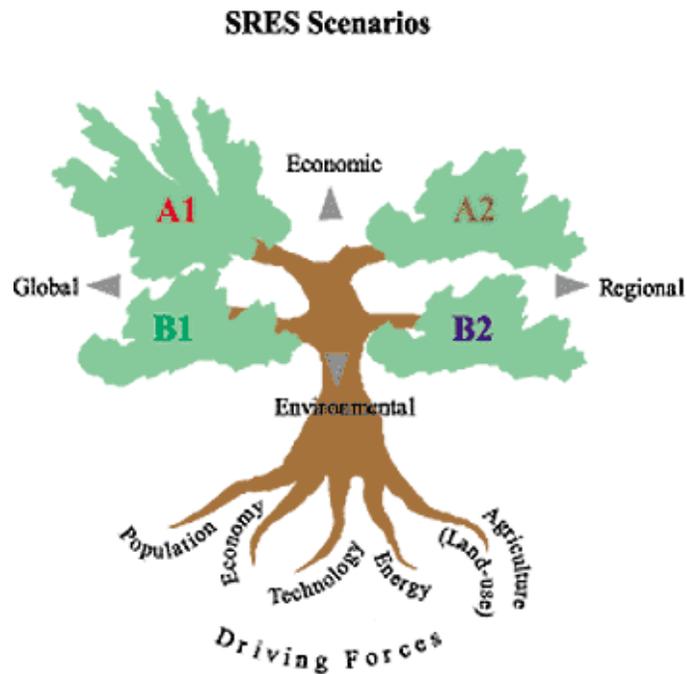
SRES Scenarios

Figure A1: SRES Emission Scenarios (Nakicenovic et al, 2000)

A1B: In scenario A1B, the storyline includes rapid economic expansion and globalization, a population peaking at 9 billion in 2050, and a balanced emphasis on a wide range of energy sources (Nakicenovic et al, 2000).

B1: The storyline for the B1 scenario is much like A1B in terms of population and globalization; however there are changes toward a service and information economy with more resource efficient and clean technologies. Emphasis is put on finding global solutions for sustainability (Nakicenovic et al, 2000).

A2: For scenario A2, the storyline consists of a world of independently operating nations with a constantly increasing population and economic development on a regional

level. Technological advances in this storyline occur more slowly due to the

divisions between nations (Nakicenovic et al, 2000).

APPENDIX B: Comparison of Different Distributions of AOGCM Models and Scenarios for Extreme Precipitation Events

Heavy Precipitation Days during Summer

Historical Perturbed

#	Distribution	Parameters
1	Frechet	α=3.348 β=6.8878
2	Frechet (3P)	α=2.8487 β=6.596 γ=0.34122
3	Gamma	α=9.9813 β=0.8658
4	Gamma (3P)	α=22.302 β=0.57851 γ=-4.26
5	Gen. Extreme Value	k=-0.13731 σ=2.4781 μ=7.5111
6	Gen. Pareto	k=-0.6878 σ=6.9672 μ=4.5138
7	Gumbel Max	σ=2.1327 μ=7.4107
8	Log-Pearson 3	α=4.6933 β=-0.1586 γ=2.8469
9	Normal	σ=2.7353 μ=8.6418
10	Pareto	α=0.47562 β=1
11	Rayleigh	σ=6.8952
12	Rayleigh (2P)	σ=5.7624 γ=0.96377
13	Weibull	α=3.5895 β=9.5744
14	Weibull (3P)	α=3.1727 β=9.0058 γ=0.5737

CGCM3T47 A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16987	11	12.018	9	44.102	9
2	Frechet (3P)	0.15989	10	12.789	10	N/A	
3	Gamma	0.10089	1	2.3797	3	37.705	4
4	Gamma (3P)	0.10828	4	2.3482	2	34.241	3
5	Gen. Extreme Value	0.10341	2	2.2592	1	34.222	2
6	Gen. Pareto	0.11807	7	59.471	13	N/A	
7	Gumbel Max	0.10867	5	4.1899	7	43.081	8
8	Log-Pearson 3	0.11583	6	7.2946	8	N/A	
9	Normal	0.12283	9	3.2854	5	42.033	7
10	Pareto	0.49011	14	111.88	14	632.35	11
11	Rayleigh	0.20474	12	20.491	12	123.66	10
12	Rayleigh (2P)	0.207	13	16.927	11	41.521	5
13	Weibull	0.1196	8	3.4186	6	41.997	6
14	Weibull (3P)	0.10682	3	2.9071	4	33.994	1

#	Distribution	Parameters
1	Frechet	α=2.9855 β=6.7307
2	Frechet (3P)	α=2.2972 β=6.0813 γ=0.65067
3	Gamma	α=9.7743 β=0.8876
4	Gamma (3P)	α=109.49 β=0.26878 γ=-20.752
5	Gen. Extreme Value	k=-0.30128 σ=2.8071 μ=7.7185
6	Gen. Pareto	k=-1.0392 σ=9.765 μ=3.8869
7	Gumbel Max	σ=2.1636 μ=7.4267
8	Log-Pearson 3	α=3.0689 β=-0.21174 γ=2.7498
9	Normal	σ=2.775 μ=8.6756
10	Pareto	α=0.4762 β=1
11	Rayleigh	σ=6.9221
12	Rayleigh (2P)	σ=5.7961 γ=0.9612
13	Weibull	α=3.3471 β=9.6623
14	Weibull (3P)	α=3.5712 β=9.8453 γ=-0.1866

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.22307	13	18.936	11	77.817	9
2	Frechet (3P)	0.19612	12	20.119	12	N/A	
3	Gamma	0.11596	8	4.6346	6	33.736	2
4	Gamma (3P)	0.08929	6	2.3485	5	42.646	7
5	Gen. Extreme Value	0.0779	3	1.9996	2	37.203	3
6	Gen. Pareto	0.10168	7	50.372	13	N/A	
7	Gumbel Max	0.14056	9	9.8432	8	22.831	1
8	Log-Pearson 3	0.07553	1	5.9275	7	N/A	
9	Normal	0.08222	4	2.1826	4	37.411	4
10	Pareto	0.46239	14	108.93	14	472.85	11
11	Rayleigh	0.17626	10	18.678	10	129.42	10
12	Rayleigh (2P)	0.19426	11	15.991	9	56.501	8
13	Weibull	0.08494	5	1.95	1	37.697	6
14	Weibull (3P)	0.07658	2	2.0011	3	37.562	5

#	Distribution	Parameters
1	Frechet	α=2.6711 β=6.1063
2	Frechet (3P)	α=1.7774 β=5.2249 γ=0.86986
3	Gamma	α=7.5391 β=1.0856
4	Gamma (3P)	α=28.546 β=0.55743 γ=-7.7279
5	Gen. Extreme Value	k=-0.16418 σ=2.7476 μ=6.9878
6	Gen. Pareto	k=-0.74304 σ=7.9912 μ=3.5999
7	Gumbel Max	σ=2.3241 μ=6.843
8	Log-Pearson 3	α=2.9593 β=-0.24412 γ=2.7479
9	Normal	σ=2.9808 μ=8.1845
10	Pareto	α=0.49371 β=1
11	Rayleigh	σ=6.5303
12	Rayleigh (2P)	σ=5.5579 γ=0.90973
13	Weibull	α=2.9653 β=9.1644
14	Weibull (3P)	α=2.8584 β=8.8868 γ=0.25874

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.20181	13	16.684	11	34.344	7
2	Frechet (3P)	0.17437	12	25.113	12	N/A	
3	Gamma	0.09222	3	2.3276	5	20.659	1
4	Gamma (3P)	0.08619	2	1.7476	2	21.428	2
5	Gen. Extreme Value	0.08164	1	1.7271	1	21.53	3
6	Gen. Pareto	0.10658	6	56.201	13	N/A	
7	Gumbel Max	0.11297	9	4.154	7	67.104	8
8	Log-Pearson 3	0.11201	8	11.473	9	N/A	
9	Normal	0.11099	7	2.4211	6	22.582	6
10	Pareto	0.45395	14	104.15	14	569.27	11
11	Rayleigh	0.16278	11	12.733	10	122.73	10
12	Rayleigh (2P)	0.16101	10	8.975	8	110.06	9
13	Weibull	0.09886	5	2.0816	4	21.707	5
14	Weibull (3P)	0.09596	4	2.0187	3	21.611	4

#	Distribution	Parameters
1	Frechet	α=3.2482 β=6.2219
2	Frechet (3P)	α=1.9755 β=4.365 γ=1.8425
3	Gamma	α=9.3653 β=0.84119
4	Gamma (3P)	α=24.784 β=0.51728 γ=-4.9422
5	Gen. Extreme Value	k=-0.16663 σ=2.3807 μ=6.8454
6	Gen. Pareto	k=-0.7481 σ=6.9457 μ=3.9047
7	Gumbel Max	σ=2.0071 μ=6.7194
8	Log-Pearson 3	α=7.528 β=-0.12959 γ=2.9814
9	Normal	σ=2.5743 μ=7.878
10	Pareto	α=0.7618 β=2
11	Rayleigh	σ=6.2857
12	Rayleigh (2P)	σ=4.6319 γ=1.8528
13	Weibull	α=3.4916 β=8.7332
14	Weibull (3P)	α=2.7835 β=7.4764 γ=1.2191

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.19311	13	13.315	10	77.324	10
2	Frechet (3P)	0.17462	11	28.25	12	N/A	
3	Gamma	0.0948	5	2.6004	5	20.408	1
4	Gamma (3P)	0.0782	1	2.2261	2	31.726	2
5	Gen. Extreme Value	0.07986	2	2.2087	1	37.509	6
6	Gen. Pareto	0.10597	8	32.361	13	N/A	
7	Gumbel Max	0.12232	9	5.014	8	50.929	9
8	Log-Pearson 3	0.08325	3	2.2662	3	36.82	4
9	Normal	0.10073	7	2.7918	6	38.733	7
10	Pareto	0.42208	14	91.914	14	581.04	12
11	Rayleigh	0.19086	12	18.582	11	189.64	11
12	Rayleigh (2P)	0.14817	10	7.1643	9	41.391	8
13	Weibull	0.09796	6	2.8803	7	33.545	3
14	Weibull (3P)	0.08577	4	2.305	4	36.917	5

#	Distribution	Parameters
1	Frechet	α=2.7182 β=6.5892
2	Frechet (3P)	α=1.9167 β=5.8498 γ=0.80941
3	Gamma	α=9.6944 β=0.89644
4	Gamma (3P)	α=131.09 β=0.24761 γ=-23.746
5	Gen. Extreme Value	k=-0.31582 σ=2.8364 μ=7.7492
6	Gen. Pareto	k=-1.0721 σ=10.062 μ=3.8345
7	Gumbel Max	σ=2.1762 μ=7.4343
8	Log-Pearson 3	α=1.5919 β=-0.31202 γ=2.5941
9	Normal	σ=2.7911 μ=8.6905
10	Pareto	α=0.47679 β=1
11	Rayleigh	σ=6.934
12	Rayleigh (2P)	σ=5.8369 γ=0.92057
13	Weibull	α=3.1419 β=9.7467
14	Weibull (3P)	α=4.1389 β=11.237 γ=-1.5097

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.21083	13	22.399	10	77.95	9
2	Frechet (3P)	0.19047	10	28.417	11	N/A	
3	Gamma	0.13634	8	4.6775	6	45.526	7
4	Gamma (3P)	0.10215	6	2.3258	4	38.857	5
5	Gen. Extreme Value	0.08748	1	2.0688	1	38.161	2
6	Gen. Pareto	0.10143	5	47.121	13	N/A	
7	Gumbel Max	0.16505	9	9.3537	7	44.109	6
8	Log-Pearson 3	0.11238	7	39.959	12	N/A	
9	Normal	0.09475	4	2.2486	3	38.521	4
10	Pareto	0.45839	14	109.91	14	826.2	11
11	Rayleigh	0.19323	11	18.896	9	143.13	10
12	Rayleigh (2P)	0.20139	12	16.769	8	61.988	8
13	Weibull	0.09149	3	2.6003	5	26.173	1
14	Weibull (3P)	0.08885	2	2.1759	2	38.287	3

#	Distribution	Parameters
1	Frechet	α=3.1554 β=6.1602
2	Frechet (3P)	α=1.6822 β=4.1423 γ=1.9163
3	Gamma	α=9.7324 β=0.80548
4	Gamma (3P)	α=58.132 β=0.32951 γ=-11.316
5	Gen. Extreme Value	k=-0.20461 σ=2.3711 μ=6.877
6	Gen. Pareto	k=-0.82785 σ=7.2626 μ=3.866
7	Gumbel Max	σ=1.9593 μ=6.7084
8	Log-Pearson 3	α=4.766 β=-0.16441 γ=2.7846
9	Normal	σ=2.5128 μ=7.8393
10	Pareto	α=0.76459 β=2
11	Rayleigh	σ=6.2548
12	Rayleigh (2P)	σ=4.5934 γ=1.8473
13	Weibull	α=3.4661 β=8.7019
14	Weibull (3P)	α=3.001 β=7.7787 γ=0.88788

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.22992	13	18.209	10	48.554	2
2	Frechet (3P)	0.20961	12	36.262	12	N/A	
3	Gamma	0.12295	2	3.8471	7	32.087	1
4	Gamma (3P)	0.12383	3	3.0407	1	88.251	4
5	Gen. Extreme Value	0.12203	1	3.0711	2	88.54	6
6	Gen. Pareto	0.13095	4	62.463	13	N/A	
7	Gumbel Max	0.1397	7	6.8668	8	52.27	3
8	Log-Pearson 3	0.13816	6	3.4832	6	105.86	10
9	Normal	0.14117	9	3.3693	4	90.149	8
10	Pareto	0.41442	14	91.974	14	633.36	12
11	Rayleigh	0.2021	11	20.407	11	196.07	11
12	Rayleigh (2P)	0.18422	10	9.3306	9	98.603	9
13	Weibull	0.14038	8	3.4351	5	89.482	7
14	Weibull (3P)	0.13235	5	3.238	3	88.401	5

#	Distribution	Parameters
1	Frechet	α=3.694 β=8.7778
2	Frechet (3P)	α=2.5098 β=7.2216 γ=1.4716
3	Gamma	α=11.677 β=0.92035
4	Gamma (3P)	α=33.62 β=0.54149 γ=-7.4581
5	Gen. Extreme Value	k=-0.16933 σ=2.9056 μ=9.4927
6	Gen. Pareto	k=-0.75372 σ=8.5063 μ=5.8966
7	Gumbel Max	σ=2.4521 μ=9.3316
8	Log-Pearson 3	α=6.8946 β=-0.11973 γ=3.1541
9	Normal	σ=3.145 μ=10.747
10	Pareto	α=0.61143 β=2
11	Rayleigh	σ=8.5749
12	Rayleigh (2P)	σ=6.5998 γ=1.9576
13	Weibull	α=3.9571 β=11.833
14	Weibull (3P)	α=3.187 β=10.387 γ=1.4361

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.18793	11	12.156	9	95.526	9
2	Frechet (3P)	0.16632	10	16.03	10	N/A	
3	Gamma	0.09118	3	1.752	3	19.88	1
4	Gamma (3P)	0.07621	1	1.5585	1	46.738	7
5	Gen. Extreme Value	0.08156	2	1.5708	2	46.776	8
6	Gen. Pareto	0.10622	8	43.982	13	N/A	
7	Gumbel Max	0.11581	9	4.2036	8	19.927	2
8	Log-Pearson 3	0.09174	4	2.0038	4	26.095	4
9	Normal	0.0989	6	2.1559	6	26.542	6
10	Pareto	0.45941	14	104.66	14	810.54	12
11	Rayleigh	0.20406	13	25.353	12	165.96	11
12	Rayleigh (2P)	0.19355	12	16.824	11	133.51	10
13	Weibull	0.10368	7	2.7228	7	26.24	5
14	Weibull (3P)	0.09458	5	2.1246	5	26.042	3

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#	Distribution	Parameters
1	Frechet	α=3.4206 β=8.1812
2	Frechet (3P)	α=1.7608 β=6.1828 γ=1.8513
3	Gamma	α=12.808 β=0.79146
4	Gamma (3P)	α=135.82 β=0.24408 γ=-23.017
5	Gen. Extreme Value	k=-0.26092 σ=2.7514 μ=9.1269
6	Gen. Pareto	k=-0.94944 σ=9.0704 μ=5.4841
7	Gumbel Max	σ=2.2085 μ=8.8621
8	Log-Pearson 3	α=2.0536 β=-0.22518 γ=2.7329
9	Normal	σ=2.8325 μ=10.137
10	Pareto	α=0.63398 β=2
11	Rayleigh	σ=8.0881
12	Rayleigh (2P)	σ=6.1453 γ=1.9192
13	Weibull	α=3.8352 β=11.217
14	Weibull (3P)	α=3.8147 β=10.917 γ=0.24808

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.19728	10	19.571	8	69.622	7
2	Frechet (3P)	0.20293	11	35.098	11	N/A	
3	Gamma	0.10677	6	3.106	6	14.328	6
4	Gamma (3P)	0.08475	4	2.0948	2	14.044	4
5	Gen. Extreme Value	0.07874	3	2.1919	3	13.689	1
6	Gen. Pareto	0.11163	8	54.871	13	N/A	
7	Gumbel Max	0.13933	9	6.8362	7	75.714	8
8	Log-Pearson 3	0.10893	7	46.391	12	N/A	
9	Normal	0.07855	2	2.0705	1	14.071	5
10	Pareto	0.46771	14	105.84	14	930.58	11
11	Rayleigh	0.23202	13	28.947	10	167.72	10
12	Rayleigh (2P)	0.22341	12	20.94	9	132.38	9
13	Weibull	0.08627	5	2.6918	5	13.9	3
14	Weibull (3P)	0.07839	1	2.4444	4	13.788	2

#	Distribution	Parameters
1	Frechet	α=3.0556 β=6.9725
2	Frechet (3P)	α=2.3748 β=6.3777 γ=0.5978
3	Gamma	α=9.3055 β=0.96205
4	Gamma (3P)	α=58.561 β=0.38349 γ=-13.507
5	Gen. Extreme Value	k=-0.21398 σ=2.8177 μ=7.8276
6	Gen. Pareto	k=-0.84778 σ=8.7354 μ=4.2249
7	Gumbel Max	σ=2.2882 μ=7.6316
8	Log-Pearson 3	α=3.7003 β=-0.19226 γ=2.8422
9	Normal	σ=2.9347 μ=8.9524
10	Pareto	α=0.46931 β=1
11	Rayleigh	σ=7.143
12	Rayleigh (2P)	σ=6.0196 γ=0.95961
13	Weibull	α=3.3572 β=9.9607
14	Weibull (3P)	α=3.2105 β=9.6171 γ=0.33789

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.18506	12	15.263	10	27.755	7
2	Frechet (3P)	0.16587	10	16.882	11	N/A	
3	Gamma	0.10012	6	2.7804	7	29.172	9
4	Gamma (3P)	0.07937	1	1.9307	2	26.055	1
5	Gen. Extreme Value	0.08202	2	1.8425	1	26.316	3
6	Gen. Pareto	0.11135	8	73.535	13	N/A	
7	Gumbel Max	0.12662	9	6.0212	8	28.892	8
8	Log-Pearson 3	0.10271	7	2.3921	6	26.88	6
9	Normal	0.0927	3	2.1654	5	26.228	2
10	Pareto	0.47359	14	109.59	14	497.25	12
11	Rayleigh	0.17597	11	17.548	12	180.55	11
12	Rayleigh (2P)	0.19021	13	14.462	9	77.434	10
13	Weibull	0.09516	5	2.0028	4	26.52	5
14	Weibull (3P)	0.0945	4	1.9353	3	26.481	4

#	Distribution	Parameters
1	Frechet	α=3.3454 β=7.0438
2	Frechet (3P)	α=1.7878 β=4.9357 γ=1.8744
3	Gamma	α=9.7545 β=0.90739
4	Gamma (3P)	α=26.701 β=0.54915 γ=-5.8116
5	Gen. Extreme Value	k=-0.18497 σ=2.6619 μ=7.733
6	Gen. Pareto	k=-0.78637 σ=7.9498 μ=4.4009
7	Gumbel Max	σ=2.2097 μ=7.5757
8	Log-Pearson 3	α=9.2752 β=-0.11382 γ=3.1805
9	Normal	σ=2.834 μ=8.8512
10	Pareto	α=0.69849 β=2
11	Rayleigh	σ=7.0622
12	Rayleigh (2P)	σ=5.2707 γ=1.9552
13	Weibull	α=3.5938 β=9.7908
14	Weibull (3P)	α=2.8003 β=8.249 γ=1.5052

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.18407	12	13.051	10	26.403	7
2	Frechet (3P)	0.17048	11	18.967	11	159.42	12
3	Gamma	0.10039	8	2.4382	6	30.549	8
4	Gamma (3P)	0.08756	4	1.9627	4	14.841	3
5	Gen. Extreme Value	0.08382	3	1.9106	3	14.762	2
6	Gen. Pareto	0.09939	7	66.695	13	N/A	
7	Gumbel Max	0.12689	9	5.246	8	31.033	9
8	Log-Pearson 3	0.0784	1	1.8693	1	11.45	1
9	Normal	0.09424	6	2.3481	5	17.766	6
10	Pareto	0.42863	14	91.73	14	595.2	13
11	Rayleigh	0.19581	13	19.28	12	152.54	11
12	Rayleigh (2P)	0.14792	10	8.4296	9	33.443	10
13	Weibull	0.09259	5	2.5338	7	16.084	4
14	Weibull (3P)	0.07873	2	1.9019	2	17.354	5

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#	Distribution	Parameters
1	Frechet	$\alpha=2.4777$ $\beta=4.689$
2	Frechet (3P)	$\alpha=1.7435$ $\beta=3.8917$ $\gamma=0.90978$
3	Gamma	$\alpha=7.2445$ $\beta=0.88819$
4	Gamma (3P)	$\alpha=56.425$ $\beta=0.31789$ $\gamma=-11.503$
5	Gen. Extreme Value	$k=-0.21026$ $\sigma=2.2626$ $\mu=5.5253$
6	Gen. Pareto	$k=-0.83986$ $\sigma=6.9811$ $\mu=2.6402$
7	Gumbel Max	$\sigma=1.864$ $\mu=5.3586$
8	Log-Pearson 3	$\alpha=2.4681$ $\beta=-0.28268$ $\gamma=2.4758$
9	Normal	$\sigma=2.3906$ $\mu=6.4345$
10	Pareto	$\alpha=0.56241$ $\beta=1$
11	Rayleigh	$\sigma=5.134$
12	Rayleigh (2P)	$\sigma=4.3111$ $\gamma=0.82442$
13	Weibull	$\alpha=2.7933$ $\beta=7.2409$
14	Weibull (3P)	$\alpha=2.9192$ $\beta=7.2376$ $\gamma=-0.02721$

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.23881	13	22.172	10	108.28	10
2	Frechet (3P)	0.19235	12	37.938	11	N/A	
3	Gamma	0.13338	8	4.2006	6	10.534	2
4	Gamma (3P)	0.10256	2	2.5736	1	32.748	5
5	Gen. Extreme Value	0.10398	3	2.6284	2	32.491	4
6	Gen. Pareto	0.11974	7	64.562	13	N/A	
7	Gumbel Max	0.14994	9	6.7294	7	40.173	7
8	Log-Pearson 3	0.11606	6	37.995	12	N/A	
9	Normal	0.11081	5	2.7542	4	33.124	6
10	Pareto	0.4343	14	101.2	14	473.65	11
11	Rayleigh	0.16931	10	12.43	9	82.33	9
12	Rayleigh (2P)	0.17129	11	8.3887	8	53.446	8
13	Weibull	0.10424	4	2.9366	5	10.292	1
14	Weibull (3P)	0.10125	1	2.7005	3	32.41	3

#	Distribution	Parameters
1	Frechet	α=2.4195 β=4.5386
2	Frechet	α=1.8535 β=4.6601
3	Gamma	α=7.2847 β=0.86082
4	Gamma	α=6.7116 β=0.93992
5	Gen. Extreme Value	k=-0.23555 σ=2.2361 μ=5.4117
6	Gen. Pareto	k=-0.89415 σ=7.13 μ=2.5066
7	Gumbel Max	σ=1.8115 μ=5.2252
8	Normal	σ=2.3234 μ=6.2708
9	Rayleigh	σ=5.0034
10	Rayleigh	σ=4.742
11	Weibull	α=2.5268 β=7.1384
12	Weibull	α=3.0055 β=7.0625
13	Log-Pearson 3	No fit
14	Pareto	No fit

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.23309	12	25.04	11	45.897	3
2	Frechet	0.19552	10	23.87	10	123.05	10
3	Gamma	0.13786	7	8.4441	6	63.19	8
4	Gamma	0.12946	6	8.0668	5	49.623	4
5	Gen. Extreme Value	0.10472	2	2.8504	1	51.46	5
6	Gen. Pareto	0.12229	5	53.637	12	N/A	
7	Gumbel Max	0.16022	8	7.3873	4	34.055	2
8	Normal	0.10661	3	2.8943	2	51.71	7
9	Rayleigh	0.17282	9	16.597	8	66.919	9
10	Rayleigh	0.2062	11	19.319	9	188.01	11
11	Weibull	0.11392	4	8.6176	7	29.909	1
12	Weibull	0.10057	1	6.7504	3	51.612	6
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

#	Distribution	Parameters
1	Frechet	α=2.8937 β=4.9312
2	Frechet (3P)	α=1.8484 β=3.9355 γ=0.88703
3	Gamma	α=7.4721 β=0.86691
4	Gamma (3P)	α=13.055 β=0.65882 γ=-2.1236
5	Gen. Extreme Value	k=-0.14005 σ=2.152 μ=5.5003
6	Gen. Pareto	k=-0.69338 σ=6.0712 μ=2.8923
7	Gumbel Max	σ=1.8477 μ=5.4111
8	Log-Pearson 3	α=8.7192 β=-0.13518 γ=2.974
9	Normal	σ=2.3697 μ=6.4776
10	Pareto	α=0.55702 β=1
11	Rayleigh	σ=5.1684
12	Rayleigh (2P)	σ=4.2441 γ=0.96169
13	Weibull	α=3.1052 β=7.2172
14	Weibull (3P)	α=2.5988 β=6.4638 γ=0.73814

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.20016	13	13.13	11	63.707	10
2	Frechet (3P)	0.1727	11	18.184	12	N/A	
3	Gamma	0.0995	4	3.2921	5	15.431	2
4	Gamma (3P)	0.08986	2	2.9241	4	15.544	3
5	Gen. Extreme Value	0.08983	1	2.8894	3	15.605	5
6	Gen. Pareto	0.10143	6	38.758	13	N/A	
7	Gumbel Max	0.11615	8	5.2835	8	15.575	4
8	Log-Pearson 3	0.0918	3	2.7366	1	15.266	1
9	Normal	0.12315	9	3.7103	7	35.667	9
10	Pareto	0.45741	14	96.511	14	486.33	12
11	Rayleigh	0.17821	12	12.563	10	87.947	11
12	Rayleigh (2P)	0.14546	10	6.8792	9	27.581	6
13	Weibull	0.11249	7	3.4216	6	33.907	8
14	Weibull (3P)	0.09991	5	2.8052	2	33.6	7

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#	Distribution	Parameters
1	Frechet	α=3.1545 β=5.7738
2	Frechet (3P)	α=1.6139 β=3.6941 γ=1.9367
3	Gamma	α=9.2624 β=0.79506
4	Gamma (3P)	α=36.941 β=0.39757 γ=-7.3222
5	Gen. Extreme Value	k=-0.18727 σ=2.2484 μ=6.4235
6	Gen. Pareto	k=-0.79121 σ=6.7347 μ=3.6043
7	Gumbel Max	σ=1.8866 μ=6.2752
8	Log-Pearson 3	α=6.2108 β=-0.14552 γ=2.8405
9	Normal	σ=2.4197 μ=7.3642
10	Pareto	α=0.80415 β=2
11	Rayleigh	σ=5.8758
12	Rayleigh (2P)	σ=4.2625 γ=1.8414
13	Weibull	α=3.4342 β=8.1688
14	Weibull (3P)	α=2.7478 β=6.958 γ=1.1657

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.21834	12	18.41	10	39.65	8
2	Frechet (3P)	0.23018	13	37.227	12	N/A	
3	Gamma	0.11756	7	3.6693	7	34.813	5
4	Gamma (3P)	0.10481	1	2.818	1	34.705	4
5	Gen. Extreme Value	0.10616	2	2.896	2	34.631	3
6	Gen. Pareto	0.14744	9	72.449	13	N/A	
7	Gumbel Max	0.13297	8	6.586	8	40.535	9
8	Log-Pearson 3	0.11007	3	3.1031	4	34.612	1
9	Normal	0.11278	5	3.1248	5	39.611	7
10	Pareto	0.40197	14	87.423	14	597.78	12
11	Rayleigh	0.21226	11	19.288	11	123.35	11
12	Rayleigh (2P)	0.18465	10	7.5124	9	60.77	10
13	Weibull	0.11066	4	3.2003	6	39.353	6
14	Weibull (3P)	0.11361	6	3.0405	3	34.631	2

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#	Distribution	Parameters
1	Frechet	α=2.4123 β=4.8275
2	Frechet	α=1.82 β=4.8753
3	Gamma	α=6.8235 β=0.98255
4	Gamma	α=6.1038 β=1.1019
5	Gen. Extreme Value	k=-0.23003 σ=2.4565 μ=5.7513
6	Gen. Pareto	k=-0.88223 σ=7.7765 μ=2.5729
7	Gumbel Max	σ=2.0012 μ=5.5493
8	Normal	σ=2.5666 μ=6.7044
9	Rayleigh	σ=5.3493
10	Rayleigh	σ=5.0832
11	Weibull	α=2.599 β=7.5794
12	Weibull	α=2.8534 β=7.544
13	Log-Pearson 3	No fit
14	Pareto	No fit

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.23569	12	22.183	11	96.587	9
2	Frechet	0.1863	11	20.501	10	197.18	11
3	Gamma	0.1267	7	6.1823	6	16.217	1
4	Gamma	0.12667	6	5.9103	5	25.332	7
5	Gen. Extreme Value	0.09	3	2.3211	2	16.326	2
6	Gen. Pareto	0.11812	5	57.296	12	N/A	
7	Gumbel Max	0.14754	8	6.8164	7	20.414	3
8	Normal	0.08673	1	2.2818	1	20.654	6
9	Rayleigh	0.15266	9	12.382	8	108.81	10
10	Rayleigh	0.18412	10	14.646	9	41.918	8
11	Weibull	0.10244	4	5.019	4	20.52	5
12	Weibull	0.08802	2	4.2661	3	20.485	4
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

Very Wet Days for Summer

Historical Perturbed

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.23286	12	28.442	12	26.716	9
2	Frechet	0.19049	11	24.034	10	29.307	10
3	Gamma	0.12824	2	15.499	8	9.664	5
4	Gamma	0.13866	6	15.632	9	9.6502	3
5	Gen. Extreme Value	0.13191	4	5.1633	1	8.7896	1
6	Gen. Pareto	0.14058	7	25.505	11	N/A	
7	Gumbel Max	0.14076	8	6.4451	2	9.385	2
8	Normal	0.17149	10	6.822	3	61.264	11
9	Rayleigh	0.12575	1	14.22	5	9.8852	7
10	Rayleigh	0.13223	5	14.237	6	9.8356	6
11	Weibull	0.12942	3	14.159	4	9.6508	4
12	Weibull	0.14726	9	15.001	7	20.071	8
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.23023	12	37.67	11	51.019	3
2	Frechet	0.17264	11	32.467	10	66.38	10
3	Gamma	0.12654	5	21.661	4	32.257	2
4	Gamma	0.12484	4	22.606	6	59.14	7
5	Gen. Extreme Value	0.10974	1	3.6624	2	58.203	4
6	Gen. Pareto	0.15023	9	110.95	12	N/A	
7	Gumbel Max	0.11063	2	3.5774	1	60.989	8
8	Normal	0.1517	10	8.6756	3	78.852	11
9	Rayleigh	0.11528	3	21.941	5	59.047	5
10	Rayleigh	0.13733	7	23.801	8	64.815	9
11	Weibull	0.14791	8	24.399	9	29.361	1
12	Weibull	0.12759	6	22.849	7	59.063	6
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.21554	12	24.351	11	51.479	8
2	Frechet	0.20147	11	19.203	10	52.116	9
3	Gamma	0.11925	5	8.2887	3	42.611	2
4	Gamma	0.10511	2	8.4582	4	49.422	3
5	Gen. Extreme Value	0.10684	3	4.095	1	33.123	1
6	Gen. Pareto	0.14593	8	137.35	12	N/A	
7	Gumbel Max	0.1048	1	4.293	2	50.989	7
8	Normal	0.16973	10	12.114	8	105.55	11
9	Rayleigh	0.13442	7	11.116	7	49.462	6
10	Rayleigh	0.16083	9	13.252	9	71.493	10
11	Weibull	0.11349	4	9.2221	5	49.439	5
12	Weibull	0.12175	6	9.4191	6	49.426	4
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.20978	12	29.078	11	23.118	1
2	Frechet	0.17391	11	24.46	10	34.937	2
3	Gamma	0.1099	3	15.029	4	52.587	7
4	Gamma	0.11188	4	15.655	5	52.473	6
5	Gen. Extreme Value	0.09735	1	3.7661	1	53.358	8
6	Gen. Pareto	0.132	7	137.09	12	N/A	
7	Gumbel Max	0.1036	2	3.9428	2	54.723	9
8	Normal	0.17201	10	10.751	3	100.3	11
9	Rayleigh	0.13595	8	17.528	8	49.442	5
10	Rayleigh	0.16908	9	20.835	9	55.227	10
11	Weibull	0.11303	5	15.667	6	45.113	3
12	Weibull	0.12857	6	16.157	7	45.387	4
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.24343	12	33.308	12	40.525	3
2	Frechet	0.20718	11	27.636	10	53.343	6
3	Gamma	0.13266	5	15.683	4	60.615	11
4	Gamma	0.11189	1	16.415	7	11.49	2
5	Gen. Extreme Value	0.12099	3	4.3168	2	10.044	1
6	Gen. Pareto	0.15132	8	32.402	11	N/A	
7	Gumbel Max	0.11331	2	4.262	1	47.507	4
8	Normal	0.1831	9	11.05	3	58.701	8
9	Rayleigh	0.14453	7	20.144	8	56.485	7
10	Rayleigh	0.18593	10	24.476	9	59.572	9
11	Weibull	0.12873	4	15.924	5	60.372	10
12	Weibull	0.13361	6	16.356	6	50.241	5
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.19463	12	31.922	11	68.121	9
2	Frechet	0.14991	10	27.34	10	84.711	11
3	Gamma	0.08687	1	17.821	4	42.146	2
4	Gamma	0.11477	5	18.808	7	42.232	3
5	Gen. Extreme Value	0.09915	2	3.2441	1	43.694	6
6	Gen. Pareto	0.11431	4	109.39	12	N/A	
7	Gumbel Max	0.10282	3	3.3036	2	43.836	7
8	Normal	0.1532	11	7.4317	3	79.394	10
9	Rayleigh	0.12094	7	18.938	8	42.615	5
10	Rayleigh	0.14156	9	20.381	9	64.942	8
11	Weibull	0.11975	6	18.689	6	27.364	1
12	Weibull	0.12274	8	18.619	5	42.536	4
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.23238	12	31.59	11	28.476	6
2	Frechet	0.18435	11	26.07	10	93.046	11
3	Gamma	0.11952	7	13.073	4	15.454	3
4	Gamma	0.10506	1	13.29	5	15.421	2
5	Gen. Extreme Value	0.10999	3	3.2081	2	21.703	4
6	Gen. Pareto	0.12926	8	116.96	12	N/A	
7	Gumbel Max	0.10796	2	3.1522	1	21.914	5
8	Normal	0.1534	10	7.6059	3	80.914	10
9	Rayleigh	0.11699	5	13.317	6	54.202	9
10	Rayleigh	0.1344	9	14.221	9	48.118	7
11	Weibull	0.11388	4	13.57	8	15.302	1
12	Weibull	0.11767	6	13.337	7	48.146	8
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

MIROC3HIRES A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.22939	9	64.42	6	49.539	2
2	Frechet	0.23789	10	74.635	10	170.9	7
3	Gamma	0.14483	2	55.361	4	66.348	4
4	Gamma	0.22697	8	67.722	8	190.36	9
5	Gen. Extreme Value	0.1314	1	6.2737	1	65.394	3
6	Gen. Pareto	0.15269	3	132.08	12	N/A	
7	Gumbel Max	0.15526	4	7.0954	2	79.432	5
8	Normal	0.20522	6	15.44	3	217.13	10
9	Rayleigh	0.24498	11	73.619	9	228.01	11
10	Rayleigh	0.33095	12	105.05	11	185.79	8
11	Weibull	0.17936	5	59.481	5	24.56	1
12	Weibull	0.21876	7	64.425	7	95.516	6
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.2386	11	64.136	9	48.729	4
2	Frechet	0.20874	10	69.994	10	89.909	7
3	Gamma	0.14789	3	51.139	4	25.353	1
4	Gamma	0.20614	8	60.977	8	96.878	8
5	Gen. Extreme Value	0.12529	1	5.2489	2	31.223	3
6	Gen. Pareto	0.15837	4	121.34	12	N/A	
7	Gumbel Max	0.13189	2	5.0641	1	64.585	6
8	Normal	0.17828	5	11.264	3	50.251	5
9	Rayleigh	0.20755	9	59.813	7	96.9	10
10	Rayleigh	0.27254	12	78.674	11	141.06	11
11	Weibull	0.19498	6	56.712	5	26.189	2
12	Weibull	0.19824	7	58.239	6	96.894	9
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.23405	12	45.73	11	57.296	7
2	Frechet	0.17101	10	42.477	10	56.214	6
3	Gamma	0.12285	3	29.764	4	34.443	3
4	Gamma	0.13243	4	32.49	7	59.534	10
5	Gen. Extreme Value	0.10958	2	4.1611	2	29.642	2
6	Gen. Pareto	0.13479	5	61.943	12	N/A	
7	Gumbel Max	0.1044	1	4.0301	1	28.008	1
8	Normal	0.16351	9	9.3052	3	68.93	11
9	Rayleigh	0.14333	7	33.502	8	47.171	5
10	Rayleigh	0.19006	11	38.973	9	47.169	4
11	Weibull	0.14833	8	31.669	6	58.827	8
12	Weibull	0.14247	6	31.525	5	59.52	9
13	Log-Pearson 3	No fit					
14	Pareto	No fit					

Maximum 5 Day Precipitation for Summer

Historical Perturbed

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.09865	12	4.8269	10	25.889	10
2	Frechet (3P)	0.05439	6	0.81711	5	11.666	5
3	Gamma	0.04901	4	0.86025	7	17.876	7
4	Gamma (3P)	0.04488	3	0.3974	1	7.8193	1
5	Gen. Extreme Value	0.05473	7	0.71692	4	8.8665	2
6	Gen. Pareto	0.04147	1	46.115	13	N/A	
7	Gumbel Max	0.05897	8	0.81934	6	11.212	4
8	Log-Pearson 3	0.05053	5	0.58761	2	9.2007	3
9	Normal	0.08427	11	4.9003	11	32.462	11
10	Pareto	0.33278	14	60.52	14	325.59	13
11	Rayleigh	0.11077	13	5.9558	12	47.381	12
12	Rayleigh (2P)	0.07516	9	2.0133	8	18.495	8
13	Weibull	0.0821	10	4.4517	9	25.433	9
14	Weibull (3P)	0.04149	2	0.67756	3	13.125	6

CGCM3T47 A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.11946	13	7.5539	12	47.569	12
2	Frechet (3P)	0.03737	4	0.34758	3	11.597	5
3	Gamma	0.03678	3	0.5383	6	15.72	8
4	Gamma (3P)	0.03802	5	0.39965	5	14.168	7
5	Gen. Extreme Value	0.03425	2	0.30862	2	8.9775	4
6	Gen. Pareto	0.06748	10	58.927	13	N/A	
7	Gumbel Max	0.03289	1	0.30772	1	8.1029	2
8	Log-Pearson 3	0.03832	6	0.35633	4	14.154	6
9	Normal	0.08038	11	4.2416	10	18.3	9
10	Pareto	0.33409	14	64.117	14	376.45	13
11	Rayleigh	0.1024	12	7.3477	11	37.621	11
12	Rayleigh (2P)	0.04727	8	1.1421	8	8.3358	3
13	Weibull	0.06078	9	3.1338	9	7.578	1
14	Weibull (3P)	0.04529	7	0.79483	7	18.483	10

CGCM3T47 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.06209	8	2.4964	8	13.594	7
2	Frechet (3P)	0.03962	4	0.48276	4	4.9843	3
3	Gamma	0.06244	9	2.1445	7	19.628	9
4	Gamma (3P)	0.02808	1	0.29936	1	2.9673	1
5	Gen. Extreme Value	0.03561	2	0.48117	3	6.5182	4
6	Gen. Pareto	0.04003	5	49.37	14	N/A	
7	Gumbel Max	0.04784	7	1.3596	6	8.4505	5
8	Log-Pearson 3	0.03632	3	0.37449	2	3.0631	2
9	Normal	0.10977	12	7.7881	11	36.419	11
10	Pareto	0.27978	14	46.199	13	209.26	13
11	Rayleigh	0.13418	13	8.6246	12	69.864	12
12	Rayleigh (2P)	0.09552	10	4.8893	9	16.912	8
13	Weibull	0.09665	11	7.4249	10	31.897	10
14	Weibull (3P)	0.04488	6	0.85226	5	12.52	6

CGCM3T63 A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.08453	11	5.8268	11	21.308	10
2	Frechet (3P)	0.02235	1	0.17314	2	2.1288	1
3	Gamma	0.04727	6	0.9258	6	11.276	7
4	Gamma (3P)	0.03472	5	0.2857	4	7.1087	6
5	Gen. Extreme Value	0.02474	2	0.15775	1	2.9035	2
6	Gen. Pareto	0.06174	8	64.652	13	N/A	
7	Gumbel Max	0.0343	4	0.2923	5	6.7601	5
8	Log-Pearson 3	0.02587	3	0.18835	3	4.7142	3
9	Normal	0.10465	12	5.0577	10	21.354	11
10	Pareto	0.33843	14	65.189	14	424.26	13
11	Rayleigh	0.11478	13	8.634	12	56.738	12
12	Rayleigh (2P)	0.07414	9	1.5463	8	6.2446	4
13	Weibull	0.08285	10	3.7422	9	12.76	8
14	Weibull (3P)	0.0505	7	1.1575	7	15.05	9

CGCM3T63 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.07263	9	3.1291	8	10.382	4
2	Frechet (3P)	0.04458	3	1.0827	2	8.7403	1
3	Gamma	0.05754	7	1.8878	6	22.413	7
4	Gamma (3P)	0.05041	5	1.1681	4	14.589	5
5	Gen. Extreme Value	0.04597	4	1.13	3	9.9243	3
6	Gen. Pareto	0.04187	1	38.595	13	N/A	
7	Gumbel Max	0.05741	6	1.6183	5	15.952	6
8	Log-Pearson 3	0.04291	2	0.9633	1	9.2111	2
9	Normal	0.11224	12	7.04	12	59.677	12
10	Pareto	0.35929	14	64.557	14	374.26	13
11	Rayleigh	0.11904	13	6.1874	10	52.159	11
12	Rayleigh (2P)	0.09121	10	3.5115	9	26.57	9
13	Weibull	0.10212	11	6.7765	11	49.514	10
14	Weibull (3P)	0.05978	8	1.9076	7	22.567	8

CSIROMK3.5 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.07008	9	3.8384	9	12.694	9
2	Frechet (3P)	0.02968	1	0.2117	2	5.8264	3
3	Gamma	0.05942	7	1.773	7	10.123	6
4	Gamma (3P)	0.04044	4	0.52008	4	9.8172	5
5	Gen. Extreme Value	0.03061	2	0.211	1	5.8188	2
6	Gen. Pareto	0.06068	8	65.643	14	N/A	
7	Gumbel Max	0.04923	5	0.94475	5	5.4315	1
8	Log-Pearson 3	0.03087	3	0.23905	3	6.243	4
9	Normal	0.11939	13	7.6916	11	49.995	11
10	Pareto	0.3279	14	57.908	13	321.52	13
11	Rayleigh	0.10834	12	7.9516	12	51.577	12
12	Rayleigh (2P)	0.0967	10	3.7371	8	12.524	7
13	Weibull	0.09932	11	6.5248	10	21.426	10
14	Weibull (3P)	0.05724	6	1.4672	6	12.604	8

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GISSAOM A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.05892	4	1.822	4	6.7481	1
2	Frechet (3P)	0.04533	3	0.50944	2	8.6888	3
3	Gamma	0.09391	9	6.3198	8	52.475	10
4	Gamma (3P)	0.08094	6	2.2562	5	18.229	5
5	Gen. Extreme Value	0.03617	1	0.43075	1	8.4709	2
6	Gen. Pareto	0.07738	5	69.075	14	N/A	
7	Gumbel Max	0.08884	7	5.1963	7	40.608	7
8	Log-Pearson 3	0.04406	2	0.63913	3	8.8179	4
9	Normal	0.15773	13	13.576	11	96.852	12
10	Pareto	0.34446	14	61.95	13	355.9	13
11	Rayleigh	0.11883	10	10.674	10	80.788	11
12	Rayleigh (2P)	0.15478	12	9.3525	9	47.601	9
13	Weibull	0.1357	11	13.741	12	46.941	8
14	Weibull (3P)	0.08986	8	4.669	6	36.916	6

MIROC3HIRES A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.07365	9	4.0735	8	21.772	9
2	Frechet (3P)	0.02612	3	0.2488	2	7.3694	3
3	Gamma	0.05796	7	1.9909	7	12.922	7
4	Gamma (3P)	0.03657	4	0.52474	4	6.4062	2
5	Gen. Extreme Value	0.02312	1	0.22726	1	7.8755	4
6	Gen. Pareto	0.06348	8	57.745	14	N/A	
7	Gumbel Max	0.04801	5	1.1406	6	4.285	1
8	Log-Pearson 3	0.0258	2	0.25019	3	9.9934	6
9	Normal	0.11857	13	7.984	12	34.437	11
10	Pareto	0.28151	14	43.811	13	216.28	13
11	Rayleigh	0.11242	12	7.7731	11	45.612	12
12	Rayleigh (2P)	0.10081	11	4.3268	9	17.774	8
13	Weibull	0.09701	10	6.324	10	24.338	10
14	Weibull (3P)	0.04816	6	1.035	5	9.0675	5

MIROC3MEDRES A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.08988	11	5.5072	10	24.56	10
2	Frechet (3P)	0.12728	13	13.846	12	N/A	
3	Gamma	0.02819	2	0.50191	5	2.052	5
4	Gamma (3P)	0.02135	1	0.1501	1	0.84473	1
5	Gen. Extreme Value	0.02855	3	0.29943	3	1.2312	3
6	Gen. Pareto	0.04303	7	49.826	13	N/A	
7	Gumbel Max	0.0312	5	0.35287	4	1.1646	2
8	Log-Pearson 3	0.02907	4	0.22374	2	1.3856	4
9	Normal	0.08477	10	4.6111	9	21.052	9
10	Pareto	0.33277	14	65.09	14	370.83	12
11	Rayleigh	0.09814	12	5.6451	11	39.479	11
12	Rayleigh (2P)	0.05614	8	1.442	7	4.0636	7
13	Weibull	0.06907	9	3.6757	8	10.178	8
14	Weibull (3P)	0.03215	6	0.58351	6	3.1704	6

MIROC3MEDRES A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.09503	11	5.2666	10	19.971	10
2	Frechet (3P)	0.03072	1	0.25289	2	8.6777	4
3	Gamma	0.06121	6	1.1562	6	9.9615	5
4	Gamma (3P)	0.04698	4	0.46191	4	7.4673	2
5	Gen. Extreme Value	0.0327	2	0.24722	1	11.871	6
6	Gen. Pareto	0.06131	7	61.907	14	N/A	
7	Gumbel Max	0.04811	5	0.54785	5	6.6364	1
8	Log-Pearson 3	0.03705	3	0.28363	3	7.6551	3
9	Normal	0.11538	13	6.611	11	30.239	11
10	Pareto	0.32259	14	60.844	13	337.98	13
11	Rayleigh	0.09848	12	6.7472	12	44.558	12
12	Rayleigh (2P)	0.08832	10	2.6526	8	12.423	7
13	Weibull	0.07895	9	5.2347	9	17.131	9
14	Weibull (3P)	0.06474	8	1.2337	7	12.909	8

Heavy Precipitation Days for Winter

Historical Perturbed

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.23165	12	24.742	11	111.15	11
2	Frechet (3P)	0.14206	8	4.8674	7	39.694	8
3	Gamma	0.13962	7	4.8635	6	28.74	7
4	Gamma (3P)	0.10318	5	2.1561	2	8.8333	1
5	Gen. Extreme Value	0.09742	3	2.1851	3	23.497	4
6	Gen. Pareto	0.11762	6	67.599	12	N/A	
7	Gumbel Max	0.15898	11	7.2577	9	28.738	6
8	Normal	0.08881	1	2.1515	1	23.76	5
9	Pareto	0.42406	13	97.36	13	340.4	12
10	Rayleigh	0.14508	9	8.7659	10	50.43	10
11	Rayleigh (2P)	0.14901	10	6.7126	8	41.849	9
12	Weibull	0.10041	4	3.1013	5	15.212	2
13	Weibull (3P)	0.09661	2	2.1992	4	23.202	3

CGCM3T47 A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.15834	4	12.939	3	148.78	3
2	Frechet (3P)	0.14421	3	10.369	2	99.039	1
3	Gamma	0.35192	9	58.032	7	697.79	9
4	Gamma (3P)	0.27363	6	35.363	4	359.7	5
5	Gen. Extreme Value	0.14013	1	9.312	1	100.96	2
6	Gen. Pareto	0.1403	2	70.841	10	N/A	
7	Gumbel Max	0.3211	8	58.884	8	793.65	10
8	Normal	0.38848	11	71.269	11	1043.9	11
9	Pareto	0.37544	10	69.916	9	449.21	7
10	Rayleigh	0.44165	13	157.47	13	381.94	6
11	Rayleigh (2P)	0.43642	12	84.198	12	594.23	8
12	Weibull	0.29677	7	48.776	6	267.0	4
13	Weibull (3P)	0.2543	5	36.566	5	N/A	

CGCM3T47 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.1451	4	11.31	3	147.41	3
2	Frechet (3P)	0.13522	1	9.3961	2	55.982	1
3	Gamma	0.31565	9	48.398	7	526.62	7
4	Gamma (3P)	0.26404	6	32.856	4	262.6	4
5	Gen. Extreme Value	0.13801	2	9.1502	1	56.342	2
6	Gen. Pareto	0.14228	3	84.408	12	N/A	
7	Gumbel Max	0.3112	8	54.46	8	774.96	11
8	Normal	0.37777	11	69.334	10	691.13	10
9	Pareto	0.36251	10	66.862	9	535.16	8
10	Rayleigh	0.42952	13	145.64	13	354.85	5
11	Rayleigh (2P)	0.42147	12	81.438	11	639.77	9
12	Weibull	0.2813	7	46.728	6	399.65	6
13	Weibull (3P)	0.24055	5	37.681	5	N/A	

CGCM3T47 B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16325	4	13.571	3	114.52	1
2	Frechet (3P)	0.14561	1	13.231	1	N/A	
3	Gamma	0.33218	9	52.683	7	541.48	5
4	Gamma (3P)	0.29632	6	40.477	4	321.44	4
5	Gen. Extreme Value	0.14954	3	13.335	2	N/A	
6	Gen. Pareto	0.14629	2	105.68	12	N/A	
7	Gumbel Max	0.30993	8	57.114	8	862.23	7
8	Normal	0.3755	10	71.433	9	879.0	8
9	Pareto	0.45159	13	97.665	11	930.01	9
10	Rayleigh	0.44313	12	148.57	13	315.89	3
11	Rayleigh (2P)	0.4265	11	84.163	10	800.31	6
12	Weibull	0.30342	7	49.581	6	257.67	2
13	Weibull (3P)	0.27473	5	42.027	5	N/A	

CGCM3T63 A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16266	4	12.808	3	140.59	3
2	Frechet (3P)	0.16022	3	11.423	2	127.12	2
3	Gamma	0.35138	10	57.697	7	616.12	8
4	Gamma (3P)	0.24677	6	32.536	4	256.39	5
5	Gen. Extreme Value	0.15749	2	10.709	1	114.75	1
6	Gen. Pareto	0.1543	1	63.316	9	N/A	
7	Gumbel Max	0.31984	8	58.844	8	820.36	10
8	Normal	0.38574	11	72.86	11	794.86	9
9	Pareto	0.33807	9	69.994	10	585.34	7
10	Rayleigh	0.46842	13	169.05	13	420.28	6
11	Rayleigh (2P)	0.43841	12	83.919	12	852.8	11
12	Weibull	0.30132	7	47.211	5	252.45	4
13	Weibull (3P)	0.2329	5	56.358	6	N/A	

CGCM3T63 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16778	4	15.907	3	152.41	2
2	Frechet	0.15324	1	12.19	1	81.494	1
3	Gamma	0.36313	9	62.245	8	536.54	7
4	Gamma	0.31903	7	47.092	5	299.87	4
5	Gen. Extreme Value	0.15939	3	14.08	2	N/A	
6	Gen. Pareto	0.15479	2	109.96	10	N/A	
7	Gumbel Max	0.31966	8	61.299	7	1117.5	8
8	Normal	0.38436	10	73.791	9	1215.6	9
9	Rayleigh	0.48871	11	189.88	11	411.61	5
10	Rayleigh	0.66019	12	348.41	12	1317.4	10
11	Weibull	0.30603	6	48.677	6	265.5	3
12	Weibull	0.28422	5	42.45	4	434.18	6
13	Pareto	No fit					

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.17778	3	14.396	2	156.86	2
2	Frechet (3P)	0.14629	1	22.365	3	N/A	
3	Gamma	0.3606	9	59.657	7	913.68	9
4	Gamma (3P)	0.3008	6	46.718	5	N/A	
5	Gen. Extreme Value	0.18535	4	12.73	1	122.81	1
6	Gen. Pareto	0.177	2	98.528	12	N/A	
7	Gumbel Max	0.34256	8	62.501	8	894.02	8
8	Normal	0.40536	11	75.216	9	818.82	7
9	Pareto	0.40448	10	79.559	10	603.06	6
10	Rayleigh	0.52913	13	227.89	13	549.02	5
11	Rayleigh (2P)	0.46311	12	90.385	11	965.08	10
12	Weibull	0.31752	7	49.507	6	222.96	3
13	Weibull (3P)	0.27546	5	34.961	4	392.57	4

CSIROMK3.5 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.18636	4	18.264	3	159.48	3
2	Frechet (3P)	0.15889	1	12.707	1	89.102	1
3	Gamma	0.3896	10	66.47	8	945.04	12
4	Gamma (3P)	0.32898	7	47.006	5	374.03	6
5	Gen. Extreme Value	0.18415	3	14.984	2	139.76	2
6	Gen. Pareto	0.17797	2	100.33	12	N/A	
7	Gumbel Max	0.34955	9	66.922	9	906.99	11
8	Normal	0.41249	11	79.27	10	407.92	8
9	Pareto	0.34924	8	63.377	7	390.47	7
10	Rayleigh	0.54638	13	257.79	13	585.28	10
11	Rayleigh (2P)	0.47071	12	96.495	11	583.18	9
12	Weibull	0.32836	6	55.865	6	342.61	4
13	Weibull (3P)	0.27705	5	37.963	4	356.57	5

CSIROMK3.5 B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.17881	4	18.471	3	146.71	3
2	Frechet (3P)	0.16656	2	13.601	1	119.31	1
3	Gamma	0.37853	10	65.942	7	907.57	10
4	Gamma (3P)	0.30533	6	49.182	5	N/A	
5	Gen. Extreme Value	0.17828	3	14.017	2	120.05	2
6	Gen. Pareto	0.16627	1	74.785	10	N/A	
7	Gumbel Max	0.33582	8	66.332	8	951.43	11
8	Normal	0.40139	11	79.123	11	453.3	6
9	Pareto	0.36675	9	67.72	9	552.65	7
10	Rayleigh	0.52836	13	241.28	13	583.94	8
11	Rayleigh (2P)	0.45593	12	95.746	12	609.36	9
12	Weibull	0.31605	7	55.599	6	417.51	5
13	Weibull (3P)	0.27292	5	39.162	4	340.58	4

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.17186	3	14.45	2	169.73	2
2	Frechet (3P)	0.15979	1	15.094	3	N/A	
3	Gamma	0.37816	9	63.364	8	749.26	8
4	Gamma (3P)	0.32398	7	47.831	5	N/A	
5	Gen. Extreme Value	0.17597	4	12.859	1	125.0	1
6	Gen. Pareto	0.17062	2	84.364	11	N/A	
7	Gumbel Max	0.3461	8	63.336	7	920.34	9
8	Normal	0.41047	11	76.79	9	514.57	4
9	Pareto	0.40974	10	79.568	10	702.41	6
10	Rayleigh	0.52116	13	226.77	13	526.96	5
11	Rayleigh (2P)	0.46709	12	90.349	12	719.03	7
12	Weibull	0.31178	6	50.964	6	268.45	3
13	Weibull (3P)	0.26841	5	39.836	4	N/A	

GISSAOM B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16703	4	15.139	2	135.95	2
2	Frechet (3P)	0.1405	1	17.914	3	N/A	
3	Gamma	0.40048	10	69.535	8	860.4	9
4	Gamma (3P)	0.30128	6	50.667	5	N/A	
5	Gen. Extreme Value	0.16597	3	12.917	1	126.15	1
6	Gen. Pareto	0.16282	2	94.809	11	N/A	
7	Gumbel Max	0.34921	8	67.381	7	793.11	8
8	Normal	0.41386	11	79.372	9	580.95	5
9	Pareto	0.39865	9	79.917	10	770.41	7
10	Rayleigh	0.54373	13	276.85	13	700.42	6
11	Rayleigh (2P)	0.47115	12	95.907	12	483.3	4
12	Weibull	0.30645	7	51.497	6	292.88	3
13	Weibull (3P)	0.27014	5	45.694	4	N/A	

MIROC3HIRES A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.15431	3	12.063	2	101.82	2
2	Frechet	0.16128	4	12.179	3	126.89	3
3	Gamma	0.33971	9	56.533	8	477.27	8
4	Gamma	0.28959	7	36.308	5	219.33	4
5	Gen. Extreme Value	0.14228	2	8.5059	1	80.98	1
6	Gen. Pareto	0.13991	1	134.84	10	N/A	
7	Gumbel Max	0.30077	8	55.568	7	794.51	10
8	Normal	0.36694	10	69.549	9	696.17	9
9	Rayleigh	0.44864	11	152.74	11	379.77	7
10	Rayleigh	0.63082	12	308.6	12	1055.1	11
11	Weibull	0.27369	6	38.002	6	227.08	5
12	Weibull	0.2587	5	33.647	4	315.91	6
13	Pareto	No fit					

MIROC3HIRES B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16949	4	12.723	3	202.3	3
2	Frechet (3P)	0.16415	1	11.226	2	96.628	2
3	Gamma	0.39112	10	69.309	8	718.34	10
4	Gamma (3P)	0.29896	6	36.846	5	312.62	6
5	Gen. Extreme Value	0.16772	3	10.922	1	90.806	1
6	Gen. Pareto	0.16468	2	72.544	9	N/A	
7	Gumbel Max	0.33619	8	64.507	7	836.98	11
8	Normal	0.40024	11	77.304	11	544.36	9
9	Pareto	0.38384	9	73.966	10	519.6	8
10	Rayleigh	0.52406	13	226.1	13	513.9	7
11	Rayleigh (2P)	0.46277	12	89.856	12	884.33	12
12	Weibull	0.30747	7	47.007	6	256.89	4
13	Weibull (3P)	0.26405	5	32.283	4	310.19	5

MIROC3MEDRES A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.12973	1	7.3736	3	122.56	3
2	Frechet (3P)	0.13577	2	6.9739	1	99.394	2
3	Gamma	0.30573	9	45.37	7	443.67	6
4	Gamma (3P)	0.23671	6	37.483	6	N/A	
5	Gen. Extreme Value	0.13866	4	6.9829	2	99.351	1
6	Gen. Pareto	0.13666	3	75.455	11	N/A	
7	Gumbel Max	0.2997	8	51.914	8	519.52	8
8	Normal	0.36678	10	66.243	9	523.42	9
9	Pareto	0.37219	11	73.438	10	474.86	7
10	Rayleigh	0.43129	13	157.58	13	312.7	5
11	Rayleigh (2P)	0.41216	12	76.634	12	626.05	10
12	Weibull	0.26366	7	36.965	5	200.62	4
13	Weibull (3P)	0.22653	5	36.106	4	N/A	

MIROC3MEDRES A2

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.14444	2	13.027	3	141.65	3
2	Frechet	0.14834	3	11.135	2	86.251	1
3	Gamma	0.36173	9	58.77	8	490.51	7
4	Gamma	0.30065	7	43.094	5	372.95	6
5	Gen. Extreme Value	0.15213	4	9.6001	1	105.33	2
6	Gen. Pareto	0.14423	1	52.39	7	N/A	
7	Gumbel Max	0.32663	8	59.853	9	1016.7	10
8	Normal	0.39262	10	72.879	10	682.59	9
9	Rayleigh	0.48876	11	204.44	11	525.36	8
10	Rayleigh	0.66922	12	371.6	12	1327.3	11
11	Weibull	0.28098	6	44.28	6	299.98	4
12	Weibull	0.26916	5	38.158	4	361.03	5
13	Pareto	No fit					

MIROC3MEDRES B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.1623	3	14.583	3	189.85	3
2	Frechet	0.1693	4	13.048	2	120.37	2
3	Gamma	0.3509	9	58.291	7	512.2	8
4	Gamma	0.31607	7	43.556	5	368.44	6
5	Gen. Extreme Value	0.16047	2	10.954	1	50.514	1
6	Gen. Pareto	0.15909	1	60.891	9	N/A	
7	Gumbel Max	0.33105	8	59.366	8	1052.6	9
8	Normal	0.39562	10	72.323	10	1201.7	10
9	Rayleigh	0.47772	11	186.69	11	346.87	4
10	Rayleigh	0.66892	12	347.16	12	1305.8	11
11	Weibull	0.29614	6	45.488	6	352.15	5
12	Weibull	0.28474	5	39.12	4	464.04	7
13	Pareto	No fit					

Very Wet Days for Winter

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Historical Perturbed

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.25088	8	71.968	8	39.441	3
2	Frechet	0.31567	12	93.945	12	313.52	11
3	Gamma	0.18065	5	63.069	5	23.644	1
4	Gamma	0.29397	11	84.742	11	280.94	10
5	Gen. Extreme Value	0.15165	2	7.6571	1	79.875	4
6	Gen. Pareto	0.15143	1	48.424	4	N/A	
7	Gumbel Max	0.15381	3	9.0244	3	107.39	7
8	Normal	0.17389	4	8.3467	2	105.76	5
9	Rayleigh	0.2321	7	66.445	6	109.85	9
10	Rayleigh	0.27746	10	82.863	10	107.32	6
11	Weibull	0.20909	6	69.704	7	37.359	2
12	Weibull	0.26946	9	80.181	9	107.47	8
13	Pareto	No fit					

CGCM3T47 A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.17079	3	23.109	3	61.424	2
2	Frechet	0.12682	1	22.633	2	45.503	1
3	Gamma	0.40027	10	81.649	9	547.9	9
4	Gamma	0.28854	7	60.085	7	422.39	8
5	Gen. Extreme Value	0.17611	4	16.527	1	122.67	3
6	Gen. Pareto	0.16061	2	42.435	4	N/A	
7	Gumbel Max	0.34784	8	74.608	8	384.8	7
8	Normal	0.38786	9	87.268	10	256.94	4
9	Rayleigh	0.59198	11	470.31	11	1184.0	10
10	Rayleigh	0.74098	12	793.65	12	2118.6	11
11	Weibull	0.23137	5	48.302	6	289.68	5
12	Weibull	0.23225	6	47.329	5	290.58	6
13	Pareto	No fit					

CGCM3T47 A2

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16601	3	38.947	2	64.085	2
2	Frechet	0.12832	1	42.048	3	39.948	1
3	Gamma	0.34622	9	77.058	8	407.03	9
4	Gamma	0.29246	7	73.108	7	325.35	7
5	Gen. Extreme Value	0.16638	4	15.252	1	154.71	4
6	Gen. Pareto	0.15342	2	85.59	10	N/A	
7	Gumbel Max	0.33311	8	70.022	6	369.31	8
8	Normal	0.38194	10	85.359	9	293.35	6
9	Rayleigh	0.58288	11	487.15	11	1089.1	10
10	Rayleigh	0.72779	12	811.86	12	2075.5	11
11	Weibull	0.18995	5	53.865	4	123.42	3
12	Weibull	0.23753	6	59.125	5	180.25	5
13	Pareto	No fit					

CGCM3T47 B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.15175	2	21.728	3	47.15	1
2	Frechet	0.11399	1	21.313	2	59.086	2
3	Gamma	0.36639	9	72.977	8	670.28	9
4	Gamma	0.29474	7	57.749	7	365.02	7
5	Gen. Extreme Value	0.17328	4	15.381	1	75.515	3
6	Gen. Pareto	0.15399	3	41.316	4	N/A	
7	Gumbel Max	0.33554	8	73.002	9	658.07	8
8	Normal	0.38105	10	87.757	10	264.24	5
9	Rayleigh	0.58395	11	459.69	11	1345.1	10
10	Rayleigh	0.72514	12	751.19	12	2056.1	11
11	Weibull	0.22758	5	46.296	6	275.73	6
12	Weibull	0.2393	6	45.408	5	263.23	4
13	Pareto	No fit					

CGCM3T63 A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.17306	2	48.681	3	49.754	1
2	Frechet	0.16071	1	53.907	4	111.81	2
3	Gamma	0.39763	10	96.203	10	241.51	7
4	Gamma	0.32411	7	87.787	8	248.11	8
5	Gen. Extreme Value	0.18614	4	17.751	2	138.53	3
6	Gen. Pareto	0.17579	3	16.889	1	179.04	6
7	Gumbel Max	0.3596	8	76.51	7	293.23	10
8	Normal	0.39704	9	90.884	9	274.07	9
9	Rayleigh	0.63607	11	563.6	11	1459.8	11
10	Rayleigh	0.76199	12	977.73	12	2278.9	12
11	Weibull	0.20386	5	63.335	5	173.62	5
12	Weibull	0.26298	6	70.669	6	160.48	4
13	Pareto	No fit					

CGCM3T63 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.18428	4	51.387	2	104.75	2
2	Frechet	0.14466	1	54.926	3	78.882	1
3	Gamma	0.38217	9	98.184	9	508.48	9
4	Gamma	0.32531	7	89.869	7	327.98	8
5	Gen. Extreme Value	0.18408	3	16.34	1	166.17	3
6	Gen. Pareto	0.17083	2	112.2	10	N/A	
7	Gumbel Max	0.35763	8	77.351	6	221.26	4
8	Normal	0.39557	10	90.281	8	284.34	6
9	Rayleigh	0.62646	11	536.82	11	1376.1	10
10	Rayleigh	0.76054	12	958.5	12	2319.2	11
11	Weibull	0.20092	5	65.281	4	315.05	7
12	Weibull	0.26416	6	72.641	5	281.23	5
13	Pareto	No fit					

CGCM3T63 B1

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.1674	1	68.907	3	96.976	1
2	Frechet	0.2168	4	84.448	6	164.46	6
3	Gamma	0.35503	8	102.59	9	154.8	5
4	Gamma	0.33825	7	117.94	10	180.4	7
5	Gen. Extreme Value	0.19504	3	20.092	2	122.7	4
6	Gen. Pareto	0.17988	2	17.703	1	111.22	3
7	Gumbel Max	0.3653	9	78.417	4	231.94	8
8	Normal	0.40601	10	91.621	7	307.72	10
9	Rayleigh	0.65204	11	642.0	11	1633.1	11
10	Rayleigh	0.78003	12	1170.8	12	2363.6	12
11	Weibull	0.23668	5	80.316	5	279.36	9
12	Weibull	0.27432	6	95.229	8	105.1	2
13	Pareto	No fit					

CSIROMK3.5 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.18854	2	51.702	3	86.859	2
2	Frechet	0.15139	1	55.547	4	69.868	1
3	Gamma	0.38249	9	96.676	10	476.97	10
4	Gamma	0.33151	7	93.836	9	351.86	9
5	Gen. Extreme Value	0.21691	5	23.264	2	313.95	8
6	Gen. Pareto	0.20006	3	20.298	1	142.74	3
7	Gumbel Max	0.36535	8	80.691	7	212.68	4
8	Normal	0.40958	10	93.698	8	303.4	6
9	Rayleigh	0.66574	11	665.7	11	1658.5	11
10	Rayleigh	0.78047	12	1099.3	12	2305.6	12
11	Weibull	0.20335	4	67.018	5	306.22	7
12	Weibull	0.26783	6	74.665	6	232.18	5
13	Pareto	No fit					

CSIROMK3.5 B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.15501	2	24.578	3	55.888	2
2	Frechet	0.11777	1	24.47	2	53.799	1
3	Gamma	0.41214	10	83.343	9	431.56	9
4	Gamma	0.31018	7	64.9	7	351.93	8
5	Gen. Extreme Value	0.19734	4	20.916	1	91.016	3
6	Gen. Pareto	0.17847	3	50.152	6	N/A	
7	Gumbel Max	0.36054	8	80.039	8	213.43	4
8	Normal	0.40135	9	93.471	10	281.01	7
9	Rayleigh	0.64286	11	603.48	11	1671.5	10
10	Rayleigh	0.76668	12	956.49	12	2283.2	11
11	Weibull	0.22921	5	49.841	5	240.09	5
12	Weibull	0.24312	6	49.349	4	266.74	6
13	Pareto	No fit					

GISSAOM A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.17333	1	68.339	3	74.764	1
2	Frechet	0.20963	4	83.4	6	169.13	6
3	Gamma	0.36817	8	104.86	9	112.56	2
4	Gamma	0.33277	7	117.47	10	180.96	7
5	Gen. Extreme Value	0.201	3	21.791	2	150.79	5
6	Gen. Pareto	0.18517	2	19.166	1	132.85	4
7	Gumbel Max	0.37097	9	79.081	4	213.97	8
8	Normal	0.40353	10	93.18	7	303.35	10
9	Rayleigh	0.65329	11	665.67	11	1619.3	11
10	Rayleigh	0.78188	12	1203.6	12	2329.7	12
11	Weibull	0.23768	5	79.868	5	286.61	9
12	Weibull	0.2717	6	94.619	8	126.05	3
13	Pareto	No fit					

GISSAOM B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.17607	2	50.881	3	79.652	1
2	Frechet	0.16686	1	55.889	4	93.792	2
3	Gamma	0.42833	10	103.98	10	750.15	10
4	Gamma	0.33745	7	95.061	8	269.34	7
5	Gen. Extreme Value	0.21466	4	24.647	2	188.29	5
6	Gen. Pareto	0.19716	3	21.75	1	151.24	3
7	Gumbel Max	0.37794	8	83.955	7	218.26	6
8	Normal	0.41591	9	96.163	9	311.08	8
9	Rayleigh	0.6843	11	711.68	11	1865.6	11
10	Rayleigh	0.79655	12	1190.6	12	2355.0	12
11	Weibull	0.2231	5	67.313	5	174.0	4
12	Weibull	0.26636	6	74.754	6	402.78	9
13	Pareto	No fit					

MIROC3HIRES A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.17447	3	66.224	3	35.101	1
2	Frechet	0.20992	4	81.187	6	147.77	5
3	Gamma	0.37036	9	105.11	9	503.44	10
4	Gamma	0.31283	7	109.58	10	201.14	6
5	Gen. Extreme Value	0.1574	2	12.957	2	130.65	4
6	Gen. Pareto	0.14538	1	12.178	1	92.446	2
7	Gumbel Max	0.36247	8	72.962	4	202.9	7
8	Normal	0.38247	10	87.085	7	252.18	8
9	Rayleigh	0.60331	11	513.36	11	1199.2	11
10	Rayleigh	0.75463	12	1023.1	12	2203.7	12
11	Weibull	0.22627	5	76.38	5	293.44	9
12	Weibull	0.25671	6	89.692	8	128.57	3
13	Pareto	No fit					

MIROC3HIRES B1

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16967	1	68.64	3	26.348	1
2	Frechet	0.24072	4	85.095	6	265.62	7
3	Gamma	0.40808	10	114.13	9	413.56	10
4	Gamma	0.33929	7	119.23	10	237.83	5
5	Gen. Extreme Value	0.2031	3	19.746	2	170.6	3
6	Gen. Pareto	0.18425	2	17.51	1	86.045	2
7	Gumbel Max	0.38199	8	81.121	5	205.08	4
8	Normal	0.40438	9	96.209	8	277.95	8
9	Rayleigh	0.6632	11	667.48	11	1785.7	11
10	Rayleigh	0.7913	12	1250.7	12	2384.6	12
11	Weibull	0.25037	5	80.185	4	265.01	6
12	Weibull	0.27363	6	95.417	7	320.63	9
13	Pareto	No fit					

MIROC3MEDRES A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16191	1	72.91	3	12.575	1
2	Frechet	0.25829	5	95.879	7	295.7	9
3	Gamma	0.34113	8	101.27	8	387.71	10
4	Gamma	0.33439	7	125.64	10	235.0	6
5	Gen. Extreme Value	0.19164	3	18.145	2	121.41	4
6	Gen. Pareto	0.17417	2	15.952	1	118.63	2
7	Gumbel Max	0.35729	9	73.989	4	228.58	5
8	Normal	0.38102	10	88.066	6	252.71	7
9	Rayleigh	0.62851	11	592.07	11	1503.2	11
10	Rayleigh	0.75041	12	1118.6	12	2177.8	12
11	Weibull	0.25163	4	83.725	5	120.84	3
12	Weibull	0.27796	6	102.93	9	268.84	8
13	Pareto	No fit					

MIROC3MEDRES A2

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.16007	1	70.757	3	27.586	1
2	Frechet	0.24879	5	90.274	6	281.4	8
3	Gamma	0.36222	8	104.47	9	431.61	10
4	Gamma	0.34296	7	122.22	10	232.22	6
5	Gen. Extreme Value	0.19904	3	18.673	2	150.87	4
6	Gen. Pareto	0.17992	2	16.493	1	98.552	2
7	Gumbel Max	0.36662	9	77.364	4	196.14	5
8	Normal	0.39492	10	90.532	7	283.34	9
9	Rayleigh	0.65336	11	626.49	11	1460.5	11
10	Rayleigh	0.77096	12	1174.9	12	2267.7	12
11	Weibull	0.24844	4	81.783	5	139.92	3
12	Weibull	0.28147	6	98.911	8	275.01	7
13	Pareto	No fit					

MIROC3MEDRES B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.17216	1	69.939	3	15.315	1
2	Frechet	0.24068	4	87.176	6	257.27	7
3	Gamma	0.37534	9	105.16	9	459.8	10
4	Gamma	0.3467	7	119.51	10	231.71	6
5	Gen. Extreme Value	0.19967	3	20.265	2	134.12	2
6	Gen. Pareto	0.18189	2	17.953	1	143.89	3
7	Gumbel Max	0.3654	8	77.753	4	201.71	5
8	Normal	0.40169	10	90.764	7	299.81	8
9	Rayleigh	0.65448	11	617.17	11	1532.4	11
10	Rayleigh	0.77534	12	1146.1	12	2247.4	12
11	Weibull	0.25231	5	81.259	5	182.42	4
12	Weibull	0.28421	6	97.068	8	302.79	9
13	Pareto	No fit					

5 day Maximum Precipitation for Winter 2050s

Historical Perturbed

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.0793	8	4.2667	8	10.82	4
2	Frechet (3P)	0.03326	2	0.39863	2	6.7692	2
3	Gamma	0.06303	7	1.7426	5	18.584	7
4	Gamma (3P)	0.04863	4	0.89717	4	12.155	5
5	Gen. Extreme Value	0.0285	1	0.35671	1	6.2318	1
6	Gen. Pareto	0.05803	5	61.224	13	N/A	
7	Gumbel Max	0.04658	3	0.74695	3	10.428	3
8	Normal	0.1172	11	7.1049	10	51.529	10
9	Pareto	0.33889	13	58.834	12	324.7	12
10	Rayleigh	0.14119	12	10.511	11	74.229	11
11	Rayleigh (2P)	0.08575	9	2.7994	7	22.705	8
12	Weibull	0.09612	10	6.7304	9	31.224	9
13	Weibull (3P)	0.06235	6	1.9084	6	15.199	6

CGCM3T47 A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.0968	11	3.9445	8	10.917	6
2	Frechet (3P)	0.03842	4	0.158	2	4.6848	1
3	Gamma	0.05483	6	1.7596	6	11.826	7
4	Gamma (3P)	0.03632	1	0.36909	3	5.6521	3
5	Gen. Extreme Value	0.03671	2	0.14608	1	5.2047	2
6	Gen. Pareto	0.05609	7	58.054	13	N/A	
7	Gumbel Max	0.03788	3	0.61193	4	7.9889	4
8	Normal	0.09585	10	6.2798	10	35.44	10
9	Pareto	0.29388	13	49.97	12	290.63	12
10	Rayleigh	0.14446	12	13.009	11	84.356	11
11	Rayleigh (2P)	0.07667	8	2.5765	7	9.3639	5
12	Weibull	0.09114	9	5.8244	9	23.741	9
13	Weibull (3P)	0.05094	5	1.1197	5	12.599	8

CGCM3T47 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.06384	6	4.363	8	21.2	8
2	Frechet (3P)	0.03264	1	0.33948	1	1.7522	1
3	Gamma	0.06148	5	2.0595	6	12.814	6
4	Gamma (3P)	0.04782	3	0.73874	3	6.6843	3
5	Gen. Extreme Value	0.03293	2	0.34114	2	1.7558	2
6	Gen. Pareto	0.0688	8	72.459	13	N/A	
7	Gumbel Max	0.04794	4	0.97002	4	9.2696	4
8	Normal	0.10848	11	7.1428	10	38.643	10
9	Pareto	0.31874	13	50.909	12	270.96	12
10	Rayleigh	0.13346	12	10.963	11	74.198	11
11	Rayleigh (2P)	0.08825	9	3.2788	7	12.545	5
12	Weibull	0.10079	10	6.1224	9	21.294	9
13	Weibull (3P)	0.06516	7	1.5373	5	16.14	7

CGCM3T47 B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.07655	8	3.0899	7	15.156	5
2	Frechet (3P)	0.02914	1	0.19282	1	3.5026	1
3	Gamma	0.06658	6	2.7105	6	24.985	8
4	Gamma (3P)	0.04305	3	0.63675	3	7.969	3
5	Gen. Extreme Value	0.03049	2	0.19678	2	4.0029	2
6	Gen. Pareto	0.06963	7	61.135	13	N/A	
7	Gumbel Max	0.04852	4	1.2171	4	13.367	4
8	Normal	0.11884	11	7.6352	9	40.206	10
9	Pareto	0.302	13	51.289	12	265.82	12
10	Rayleigh	0.16442	12	14.761	11	94.968	11
11	Rayleigh (2P)	0.09583	9	3.52	8	18.714	6
12	Weibull	0.09638	10	9.1369	10	28.35	9
13	Weibull (3P)	0.05599	5	1.8282	5	18.81	7

CGCM3T63 A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.07169	8	3.9815	8	12.372	6
2	Frechet (3P)	0.03747	3	0.39337	3	2.1107	2
3	Gamma	0.0498	7	1.0924	6	12.95	7
4	Gamma (3P)	0.0258	1	0.1845	1	2.007	1
5	Gen. Extreme Value	0.0331	2	0.35071	2	2.2295	3
6	Gen. Pareto	0.04807	6	57.529	13	N/A	
7	Gumbel Max	0.03984	4	0.5051	4	7.3627	5
8	Normal	0.10334	11	5.3168	9	35.053	10
9	Pareto	0.304	13	51.716	12	271.03	12
10	Rayleigh	0.12668	12	9.9044	11	64.458	11
11	Rayleigh (2P)	0.08171	9	2.2674	7	13.143	8
12	Weibull	0.09622	10	5.5201	10	30.922	9
13	Weibull (3P)	0.0401	5	0.51736	5	4.1031	4

CGCM3T63 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.08497	9	4.1957	8	25.368	9
2	Frechet (3P)	0.03129	3	0.40418	3	9.5201	5
3	Gamma	0.04434	6	1.0889	6	12.294	6
4	Gamma (3P)	0.02949	2	0.18221	1	3.4215	1
5	Gen. Extreme Value	0.02659	1	0.32555	2	6.7966	3
6	Gen. Pareto	0.05008	7	53.64	13	N/A	
7	Gumbel Max	0.03422	4	0.5079	5	6.5869	2
8	Normal	0.09716	11	5.7404	10	26.245	10
9	Pareto	0.276	13	50.414	12	250.79	12
10	Rayleigh	0.12602	12	9.2114	11	57.478	11
11	Rayleigh (2P)	0.0784	8	2.6493	7	12.398	7
12	Weibull	0.09004	10	5.6244	9	20.935	8
13	Weibull (3P)	0.03803	5	0.4992	4	8.6786	4

CGCM3T63 B1

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.09261	9	5.2165	8	21.422	8
2	Frechet (3P)	0.03992	1	0.30604	2	9.0072	4
3	Gamma	0.0569	6	1.2899	6	8.613	2
4	Gamma (3P)	0.04931	4	0.56625	4	10.633	5
5	Gen. Extreme Value	0.04052	2	0.30289	1	8.7138	3
6	Gen. Pareto	0.07941	7	76.231	13	N/A	
7	Gumbel Max	0.04124	3	0.42767	3	7.6241	1
8	Normal	0.10996	11	5.8454	10	28.914	10
9	Pareto	0.2915	13	49.003	12	257.89	12
10	Rayleigh	0.13307	12	11.704	11	66.644	11
11	Rayleigh (2P)	0.08252	8	2.1923	7	11.709	6
12	Weibull	0.09953	10	5.5929	9	22.646	9
13	Weibull (3P)	0.05324	5	1.0781	5	13.867	7

CSIROMK3.5 A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.09292	9	4.1955	8	14.739	6
2	Frechet (3P)	0.03414	2	0.25307	2	5.0096	2
3	Gamma	0.06874	7	1.7735	6	13.424	5
4	Gamma (3P)	0.04878	3	0.41707	3	9.6423	3
5	Gen. Extreme Value	0.03207	1	0.23262	1	4.5815	1
6	Gen. Pareto	0.05333	4	58.352	13	N/A	
7	Gumbel Max	0.05779	5	1.0796	5	12.468	4
8	Normal	0.12319	12	7.7614	11	43.527	11
9	Pareto	0.29729	13	51.381	12	273.05	12
10	Rayleigh	0.09893	10	6.6604	10	40.162	10
11	Rayleigh (2P)	0.10069	11	4.1297	7	19.425	8
12	Weibull	0.08002	8	5.8662	9	28.662	9
13	Weibull (3P)	0.06421	6	1.0672	4	16.794	7

CSIROMK3.5 B1

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#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.07504	6	3.0263	4	12.129	3
2	Frechet (3P)	0.09697	8	9.7897	10	N/A	
3	Gamma	0.07017	5	3.8601	5	25.184	5
4	Gamma (3P)	0.05796	3	1.2478	2	6.6916	2
5	Gen. Extreme Value	0.02771	1	0.19424	1	2.1058	1
6	Gen. Pareto	0.06902	4	75.416	13	N/A	
7	Gumbel Max	0.05785	2	2.3822	3	16.977	4
8	Normal	0.12832	11	9.6111	9	62.004	9
9	Pareto	0.38036	13	75.226	12	519.86	11
10	Rayleigh	0.13701	12	12.239	11	86.433	10
11	Rayleigh (2P)	0.10165	10	4.6407	7	29.209	7
12	Weibull	0.09931	9	7.1182	8	27.694	6
13	Weibull (3P)	0.07855	7	4.3016	6	29.523	8

GISSAOM A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.07415	8	3.8331	8	18.853	8
2	Frechet (3P)	0.02681	2	0.27328	2	5.4249	3
3	Gamma	0.06084	6	1.7303	6	10.837	5
4	Gamma (3P)	0.03972	3	0.34032	3	5.84	4
5	Gen. Extreme Value	0.02523	1	0.24202	1	5.1837	2
6	Gen. Pareto	0.06769	7	61.542	13	N/A	
7	Gumbel Max	0.04373	4	0.71482	4	4.3038	1
8	Normal	0.10438	11	6.5335	10	37.324	10
9	Pareto	0.29422	13	52.343	12	283.14	12
10	Rayleigh	0.13205	12	11.203	11	62.614	11
11	Rayleigh (2P)	0.08429	9	2.9934	7	16.712	7
12	Weibull	0.09274	10	6.0477	9	28.369	9
13	Weibull (3P)	0.05719	5	1.0422	5	11.021	6

GISSAOM B1

138

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.05055	2	1.5675	4	9.5827	3
2	Frechet (3P)	0.04998	1	0.56353	1	6.2295	1
3	Gamma	0.0717	7	3.5031	7	33.37	7
4	Gamma (3P)	0.06083	4	1.2164	3	14.583	4
5	Gen. Extreme Value	0.05248	3	0.63434	2	7.9955	2
6	Gen. Pareto	0.06214	5	60.788	13	N/A	
7	Gumbel Max	0.07273	8	2.4029	6	22.665	5
8	Normal	0.12735	11	10.098	10	72.969	10
9	Pareto	0.31317	13	52.814	12	254.22	12
10	Rayleigh	0.13892	12	10.454	11	91.539	11
11	Rayleigh (2P)	0.12136	9	6.5339	8	35.18	8
12	Weibull	0.12363	10	10.064	9	51.07	9
13	Weibull (3P)	0.06367	6	2.3893	5	24.475	6

MIROC3HIRES A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.08901	10	4.8365	9	19.474	9
2	Frechet (3P)	0.03419	3	0.35314	3	5.6369	3
3	Gamma	0.04281	6	0.67219	6	6.8235	5
4	Gamma (3P)	0.0247	1	0.12343	1	4.4541	1
5	Gen. Extreme Value	0.02832	2	0.28865	2	4.6348	2
6	Gen. Pareto	0.05259	7	53.539	12	N/A	
7	Gumbel Max	0.03708	4	0.39158	4	5.7821	4
8	Normal	0.09533	11	4.9745	10	24.413	10
9	Pareto	0.30858	13	58.51	13	293.68	12
10	Rayleigh	0.10919	12	6.8961	11	42.012	11
11	Rayleigh (2P)	0.07458	8	1.8592	7	8.1986	6
12	Weibull	0.08706	9	4.412	8	16.629	8
13	Weibull (3P)	0.03843	5	0.49158	5	9.0492	7

MIROC3HIRES B1

139

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.07056	9	2.5037	5	14.539	5
2	Frechet (3P)	0.06857	8	7.4849	10	N/A	
3	Gamma	0.05918	5	2.3151	4	11.61	4
4	Gamma (3P)	0.04427	3	1.0111	2	10.991	3
5	Gen. Extreme Value	0.03204	1	0.25491	1	9.7435	1
6	Gen. Pareto	0.04664	4	54.04	12	N/A	
7	Gumbel Max	0.04284	2	1.1184	3	10.443	2
8	Normal	0.10626	11	7.4386	9	45.496	9
9	Pareto	0.39246	13	78.362	13	508.98	11
10	Rayleigh	0.14802	12	11.954	11	83.175	10
11	Rayleigh (2P)	0.06646	7	3.2887	6	17.571	6
12	Weibull	0.09617	10	7.0287	8	32.169	8
13	Weibull (3P)	0.06591	6	3.3006	7	23.743	7

MIROC3MEDRES A1B

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.06788	8	3.4402	7	18.196	5
2	Frechet (3P)	0.04976	5	0.73236	4	13.246	3
3	Gamma	0.04405	3	1.4861	6	26.074	8
4	Gamma (3P)	0.03289	1	0.2452	1	9.2242	2
5	Gen. Extreme Value	0.05002	6	0.6325	3	17.349	4
6	Gen. Pareto	0.04458	4	53.438	13	N/A	
7	Gumbel Max	0.0505	7	0.90555	5	21.241	7
8	Normal	0.09838	11	6.0297	9	35.138	10
9	Pareto	0.27006	13	42.438	12	214.97	12
10	Rayleigh	0.13119	12	9.616	11	60.515	11
11	Rayleigh (2P)	0.08084	9	3.4576	8	21.016	6
12	Weibull	0.0865	10	6.067	10	32.082	9
13	Weibull (3P)	0.03509	2	0.37392	2	6.8233	1

MIROC3MEDRES A2

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.08335	9	3.9929	8	14.713	8
2	Frechet (3P)	0.03428	2	0.38007	3	4.2913	3
3	Gamma	0.04242	5	0.93229	6	13.051	6
4	Gamma (3P)	0.02681	1	0.23708	1	5.3681	4
5	Gen. Extreme Value	0.03478	3	0.34882	2	4.247	2
6	Gen. Pareto	0.04409	7	60.492	13	N/A	
7	Gumbel Max	0.03919	4	0.43606	4	3.9414	1
8	Normal	0.09142	11	4.8772	9	27.956	10
9	Pareto	0.32019	13	55.186	12	316.09	12
10	Rayleigh	0.14395	12	10.795	11	70.028	11
11	Rayleigh (2P)	0.06552	8	1.6489	7	13.54	7
12	Weibull	0.08778	10	5.1108	10	27.841	9
13	Weibull (3P)	0.04314	6	0.63663	5	7.2541	5

MIROC3MEDRES B1

#	Distribution	Kolmogorov Smirnov		Anderson Darling		Chi-Squared	
		Statistic	Rank	Statistic	Rank	Statistic	Rank
1	Frechet	0.07868	8	2.9553	7	9.2039	6
2	Frechet (3P)	0.18908	12	25.277	11	N/A	
3	Gamma	0.05494	5	1.2914	4	9.0745	4
4	Gamma (3P)	0.03839	3	0.41503	2	5.8228	1
5	Gen. Extreme Value	0.0278	1	0.29076	1	11.69	7
6	Gen. Pareto	0.04316	4	56.811	12	N/A	
7	Gumbel Max	0.038	2	0.52042	3	6.2876	2
8	Normal	0.10601	10	5.8091	8	42.222	9
9	Pareto	0.34483	13	64.173	13	342.81	11
10	Rayleigh	0.15294	11	12.092	10	74.21	10
11	Rayleigh (2P)	0.06999	7	1.7907	6	8.9554	3
12	Weibull	0.09868	9	6.518	9	30.824	8
13	Weibull (3P)	0.05694	6	1.4057	5	9.1681	5

APPENDIX C: Distribution Fit of Extreme Precipitation Indices

Table G-1: Heavy Precipitation Days for 2050s Summer

AOGCM Models/Scenarios	Distribution Fit	Parameters					
		k	σ	μ	α	β	γ
Historical Perturbed	GEV III	0.14	2.48	7.511	-	-	-
CGCM3T47 A1B	GEV III	0.15	2.58	7.34	-	-	-
CGCM3T47 A2	GEV III	0.30	2.81	7.72	-	-	-
CGCM3T47 B1	GEV III	0.16	2.75	6.99	-	-	-
CGCM3T63 A1B	Gamma 3P	-	-	-	24.78	0.52	-4.94
CGCM3T63 A2	GEV III	0.32	2.84	7.75	-	-	-
CGCM3T63 B1	GEV III	-0.20	2.37	6.88	-	-	-
CSIROMK3.5 A2	Gamma	-	-	-	11.68	0.92	11.68
CSIROMK3.5 B1	GEV III	0.26	2.75	9.13	-	-	-
GISSAOM A1B	Gamma 3P	-	-	-	58.56	0.38	-13.51
GISSAOM B1	Log-Pearson 3	-	-	-	9.27	0.11	3.18
MIROC3HIRES A1B	GEV III	0.21	2.26	5.53	-	-	-
MIROC3HIRES B1	GEV III	0.24	2.23	5.41	-	-	-
MIROC3MEDRES A1B	Log-Pearson 3	-	-	-	8.72	0.14	2.97
MIROC3MEDRES A2	Gamma 3P	-	-	-	36.94	0.39	7.32
MIROC3MEDRES B1	GEV III	0.23	2.46	5.75	-	-	-

Table G-2: Heavy Precipitation Days for Winter

AOGCM Models/Scenarios	Distribution Fit	Parameters		
		k	σ	μ
Historical Perturbed	Normal	-	2.64	6.68
CGCM3T47 A1B	GEV Type II	0.62	4.46	8.19
CGCM3T47 A2	GEV Type II	0.59	4.58	7.85
CGCM3T47 B1	GEV Type II	0.60	4.81	8.86
CGCM3T63 A1B	GEV Type II	0.61	4.35	7.27
CGCM3T63 A2	GEV Type II	0.63	4.41	7.43
CGCM3T63 B1	GEV Type II	0.64	4.26	6.36
CSIROMK3.5 A2	GEV Type II	0.66	5.13	7.95
CSIROMK3.5 B1	GEV Type II	0.66	5.09	8.38
GISSAOM A1B	GEV Type II	0.64	4.40	6.58
GISSAOM B1	GEV Type II	0.67	4.58	6.59
MIROC3HIRES A1B	GEV Type II	0.60	3.84	6.06
MIROC3HIRES B1	GEV Type II	0.65	3.76	5.64
MIROC3MEDRES A1B	GEV Type II	0.58	3.91	5.71
MIROC3MEDRES A2	GEV Type II	0.63	3.83	5.68
MIROC3MEDRES B1	GEV Type II	0.62	3.63	5.64

Table G-3: Very Wet Days for Summer

AOGCM Models/Scenarios	Distribution Fit	Parameters				
		α	B	k	σ	μ
Historical Perturbed	GEV III			0.06	1.24	1.40
CGCM3T47 A1B	Frechet	0.99	2.57	-	-	-
CGCM3T47 A2	Frechet	0.92	2.14	-	-	-
CGCM3T47 B1	Frechet	0.99	2.74	-	-	-
CGCM3T63 A1B	Frechet	0.89	1.80	-	-	-
CGCM3T63 A2	Frechet	0.90	2.02	-	-	-
CGCM3T63 B1	Frechet	0.82	1.43	-	-	-
CSIROMK3.5 A2	Frechet	0.83	1.98	-	-	-
CSIROMK3.5 B1	Frechet	0.90	2.45	-	-	-
GISSAOM A1B	Frechet	0.81	1.43	-	-	-
GISSAOM B1	Frechet	0.84	1.66	-	-	-
MIROC3HIRES A1B	Gen. Pareto	-	-	0.63	3.52	-0.15
MIROC3HIRES B1	Gen. Pareto	-	-	0.68	3.41	-0.29
MIROC3MEDRES A1B	Gen. Pareto	-	-	0.64	3.33	-0.33
MIROC3MEDRES A2	Frechet	0.83	1.29	-	-	-
MIROC3MEDRES B1	Gen. Pateto	-	-	0.65	0.85	0.25

Table G-4: Very Wet Days for Winter

AOGCM Models/Scenarios	Distribution Fit	Parameters				
		K	σ	μ	α	β
Historical Perturbed	GEV II	-0.070	1.52	2.59	-	-
CGCM3T47 A1B	Gumbel Max	-	2.17	3.40	-	-
CGCM3T47 A2	GEV II	0.10	2.04	3.34	-	-
CGCM3T47 B1	Gamma	-	-	-	2.61	1.81
CGCM3T63 A1B	GEV III	-0.14	1.58	2.61	-	-
CGCM3T63 A2	GEV III	0.14	1.72	2.99	-	-
CGCM3T63 B1	GEV III	0.15	1.53	2.55	-	-
CSIROMK3.5 A2	Weibull	-	-	-	2.57	6.09
CSIROMK3.5 B1	GEV III	-0.16	1.98	3.98	-	-
GISSAOM A1B	GEV III	-0.17	1.77	3.20	-	-
GISSAOM B1	GEV III	-0.22	1.82	3.32	-	-
MIROC3HIRES A1B	GEV III	-0.03	1.18	1.5	-	-
MIROC3HIRES B1	Gumbel Max	-	1.16	1.69	-	-
MIROC3MEDRES A1B	Gumbel Max	-	1.15	1.68	-	-
MIROC3MEDRES A2	GEV III	-0.20	1.46	2.30	-	-
MIROC3MEDRES B1	GEV III	-0.09	1.30	1.88	-	-

Table G-5: Maximum 5 Day Precipitation for Summer

AOGCM Models/Scenarios	Distribution Fit	Parameters		
		k	σ	μ
Historical Perturbed	GEV II	0.026	23.30	54.71
CGCM3T47 A1B	Gumbel Max	-	23.14	55.98
CGCM3T47 A2	GEV II	0.11	21.71	55.99
CGCM3T47 B1	GEV II	0.038	23.40	57.89
CGCM3T63 A1B	GEV II	0.036	21.57	54.43
CGCM3T63 A2	GEV II	0.07	24.55	57.71
CGCM3T63 B1	GEV II	0.061	21.66	57.58
CSIROMK3.5 A2	GEV II	0.093	30.01	75.01
CSIROMK3.5 B1	GEV II	0.097	27.75	70.83
GISSAOM A1B	GEV II	0.20	21.75	58.17
GISSAOM B1	GEV II	0.044	24.6	60.57
MIROC3HIRES A1B	GEV II	0.10	16.78	41.65
MIROC3HIRES B1	GEV II	0.09	19.07	42.95
MIROC3MEDRES A1B	GEV II	0.02	18.77	43.61
MIROC3MEDRES A2	GEV II	0.061	20.83	49.79
MIROC3MEDRES B1	GEV II	0.09	17.3	45.12

Table G-6: Maximum 5 Day Precipitation for Winter

AOGCM Models/Scenarios	Distribution Fit	Parameters					
		K	σ	μ	α	β	γ
Historical Perturbed	GEV II	0.07	15.85	42.45	-	-	-
CGCM3T47 A1B	GEV II	0.07	18.93	54.03	-	-	-
CGCM3T47 A2	GEV II	0.08	18.64	50.48	-	-	-
CGCM3T47 B1	GEV II	0.09	18.14	54.38	-	-	-
CGCM3T63 A1B	GEV II	0.04	17.46	46.26	-	-	-
CGCM3T63 A2	GEV II	0.05	18.58	48.35	-	-	-
CGCM3T63 B1	GEV II	0.05	15.65	43.05	-	-	-
CSIROMK3.5 A2	GEVII	0.098	21.17	50.56	-	-	-
CSIROMK3.5 B1	GEV II	0.13	18.57	52.01	-	-	-
GISSAOM A1B	GEV II	0.07	15.24	41.70	-	-	-
GISSAOM B1	Frechet 3P	-	-	-	6.25	97.63	-54.53
MIROC3HIRES A1B	Gamma 3P	-	-	-	3.01	13.28	13.23
MIROC3HIRES B1	GEV II	0.1	13.83	38.85	-	-	-
MIROC3MEDRES A1B	Gamma 3P	-	-	-	2.27	13.45	17.68
MIROC3MEDRES A2	Gamma 3P	-	-	-	3.26	10.843	14.15
MIROC3MEDRES B1	Gumbel Max	-	14.12	38.78	-	-	-

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